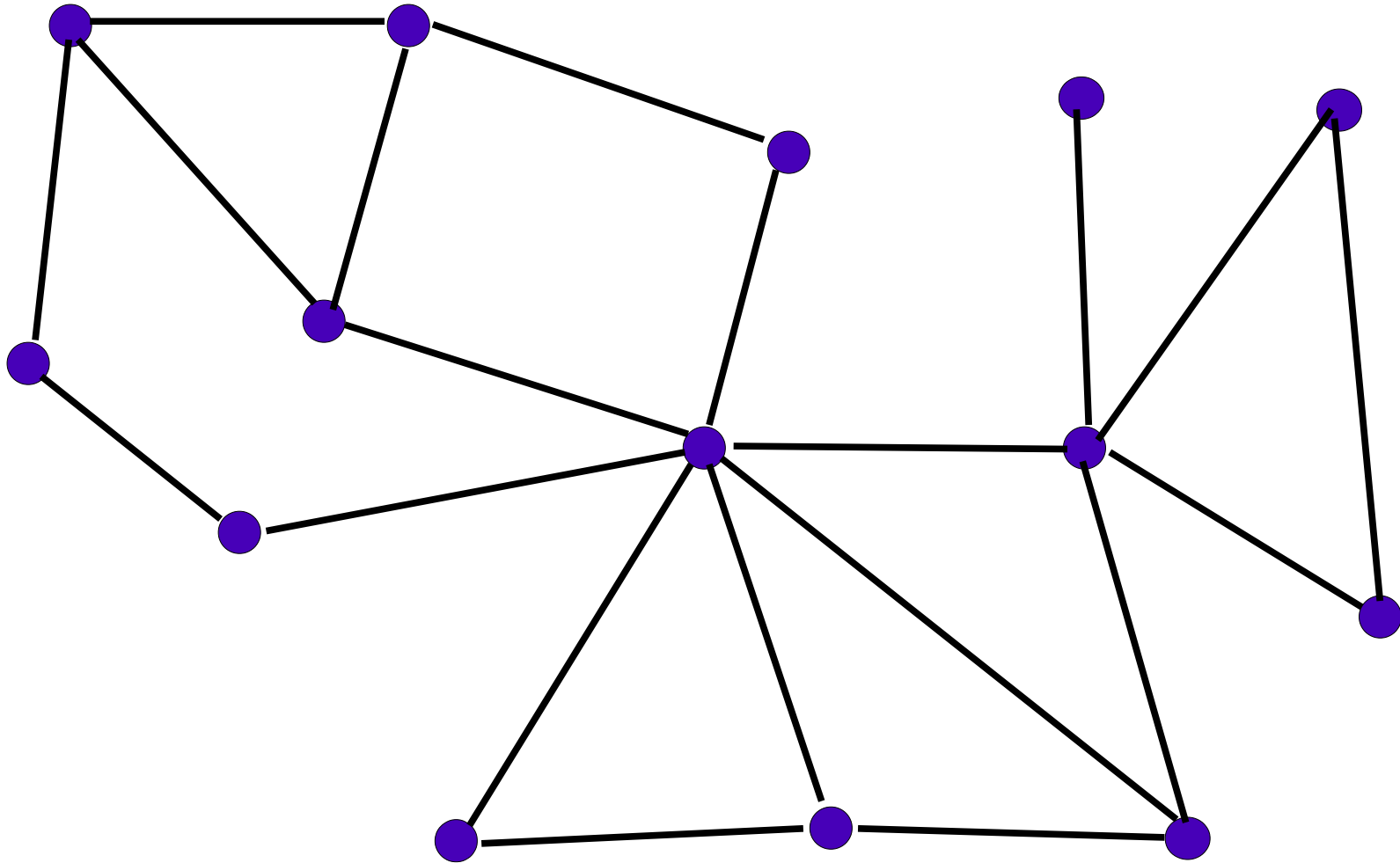
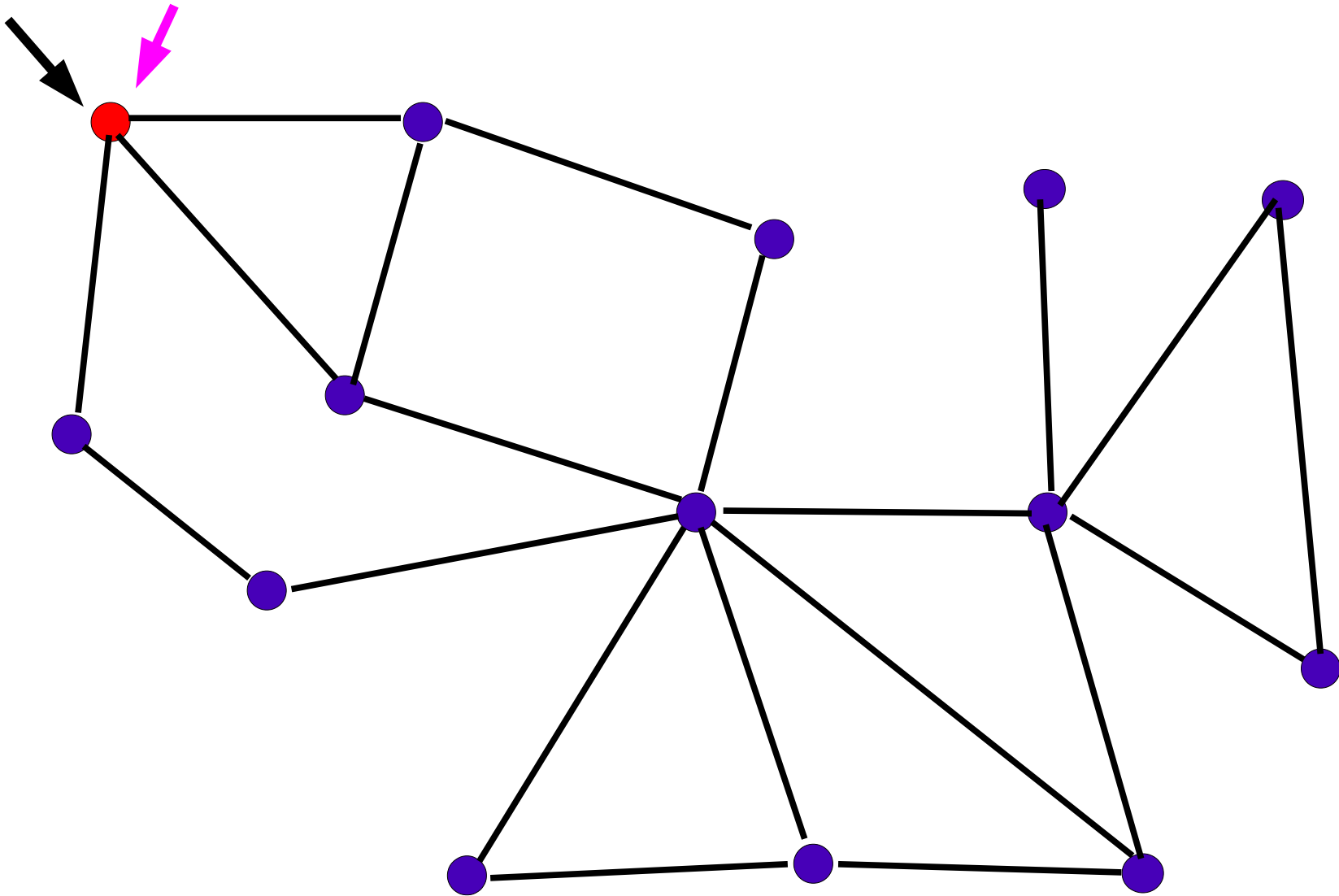


# Biconnected Components

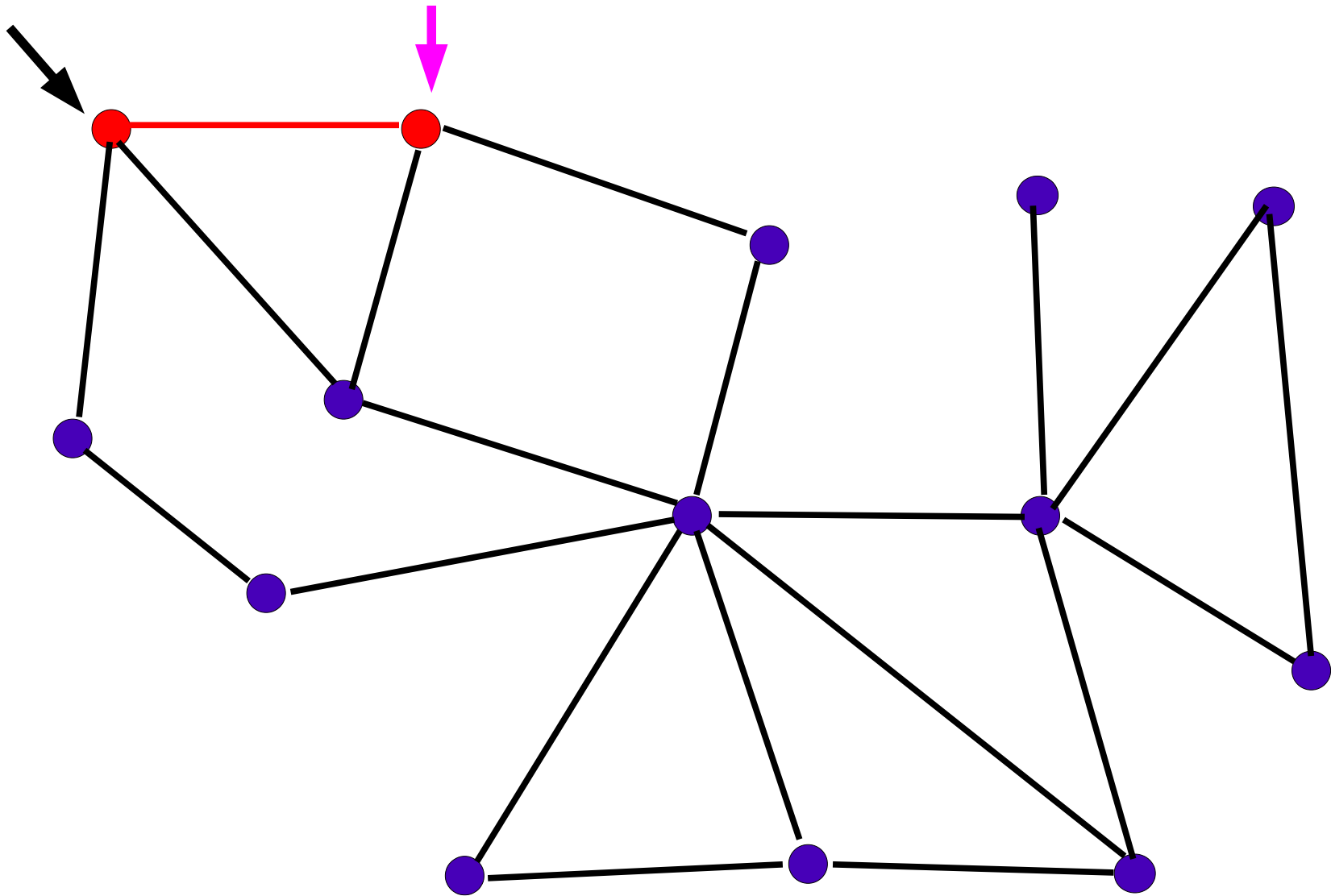
# Biconnected Components



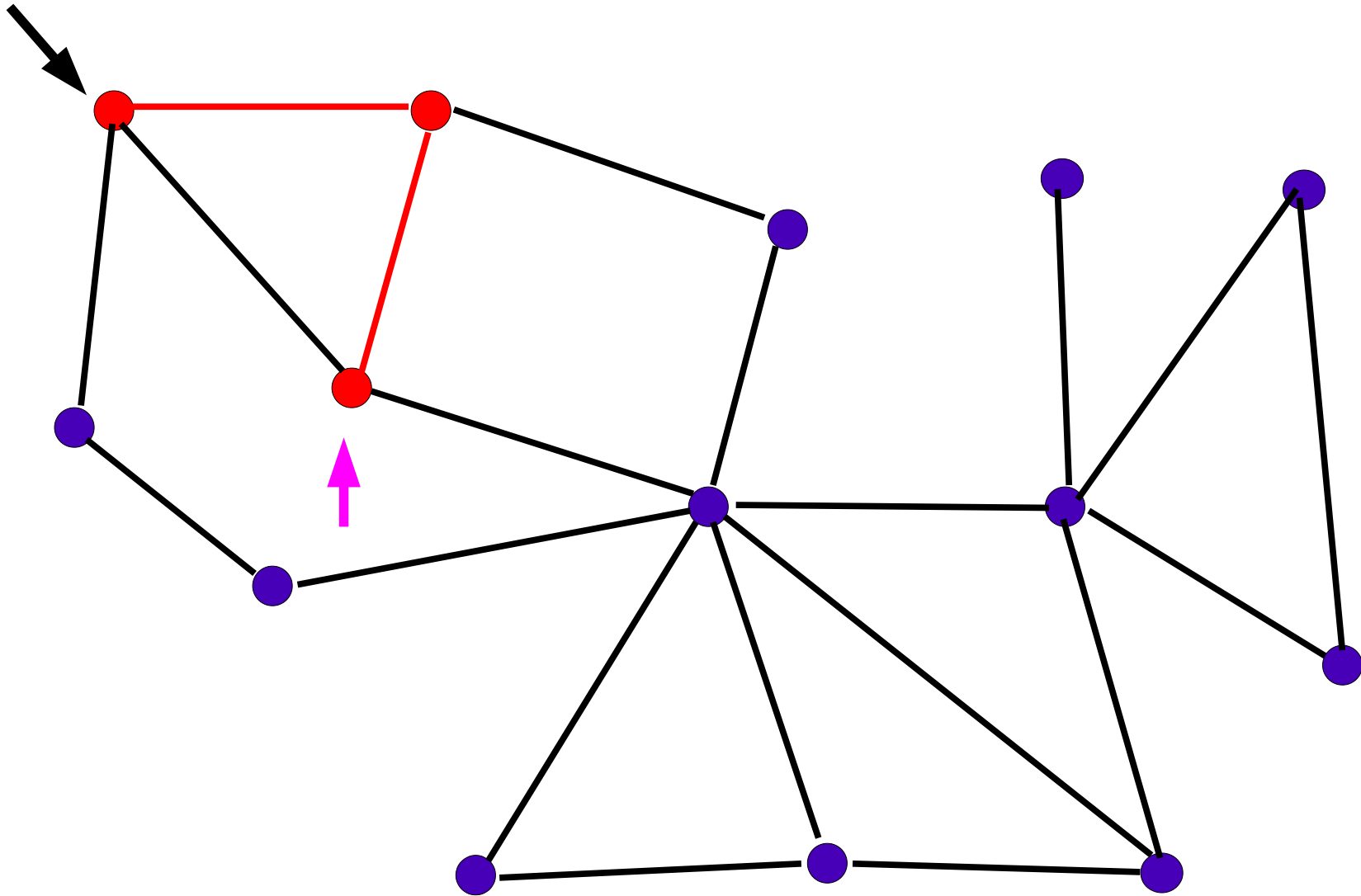
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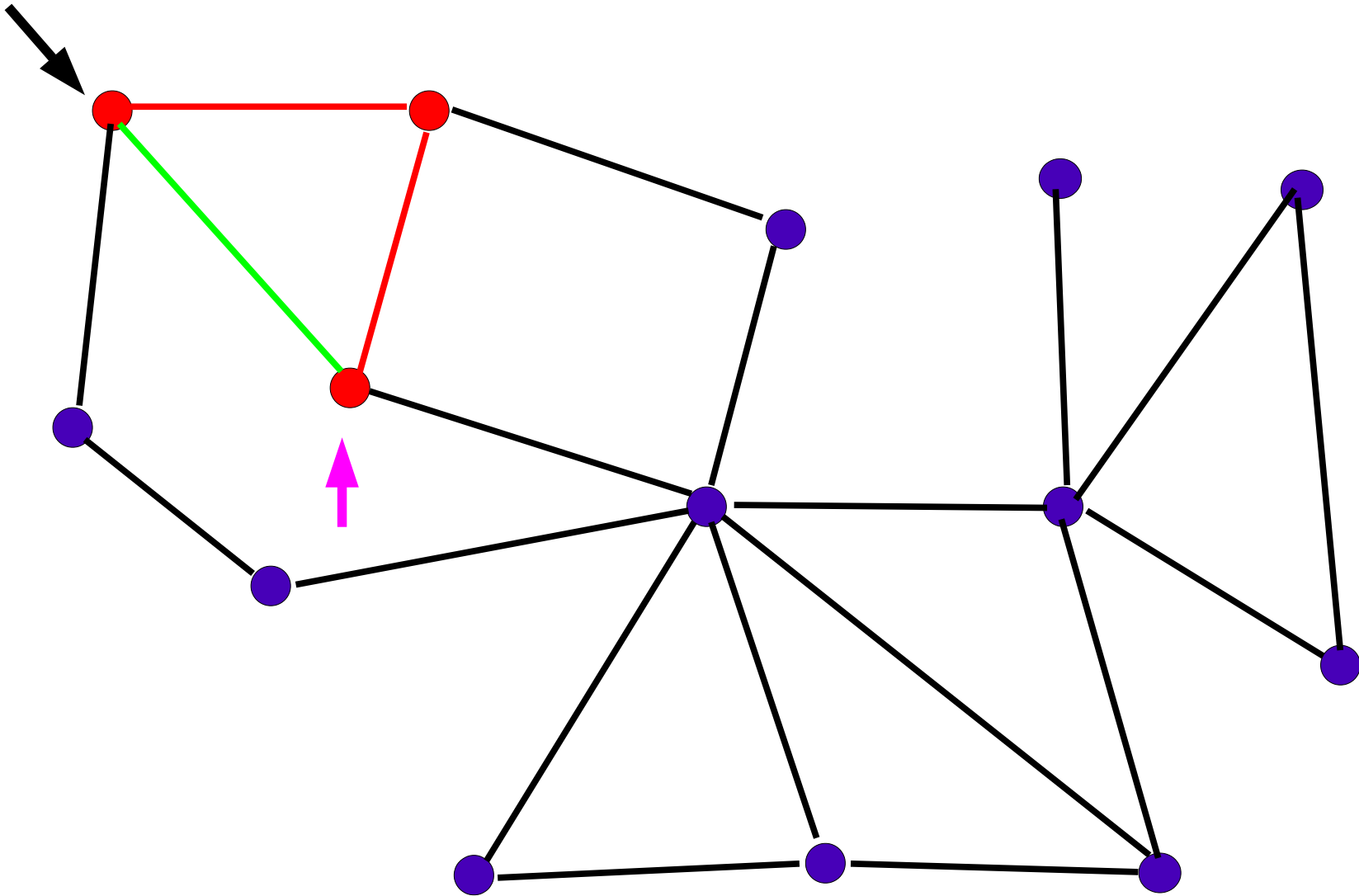
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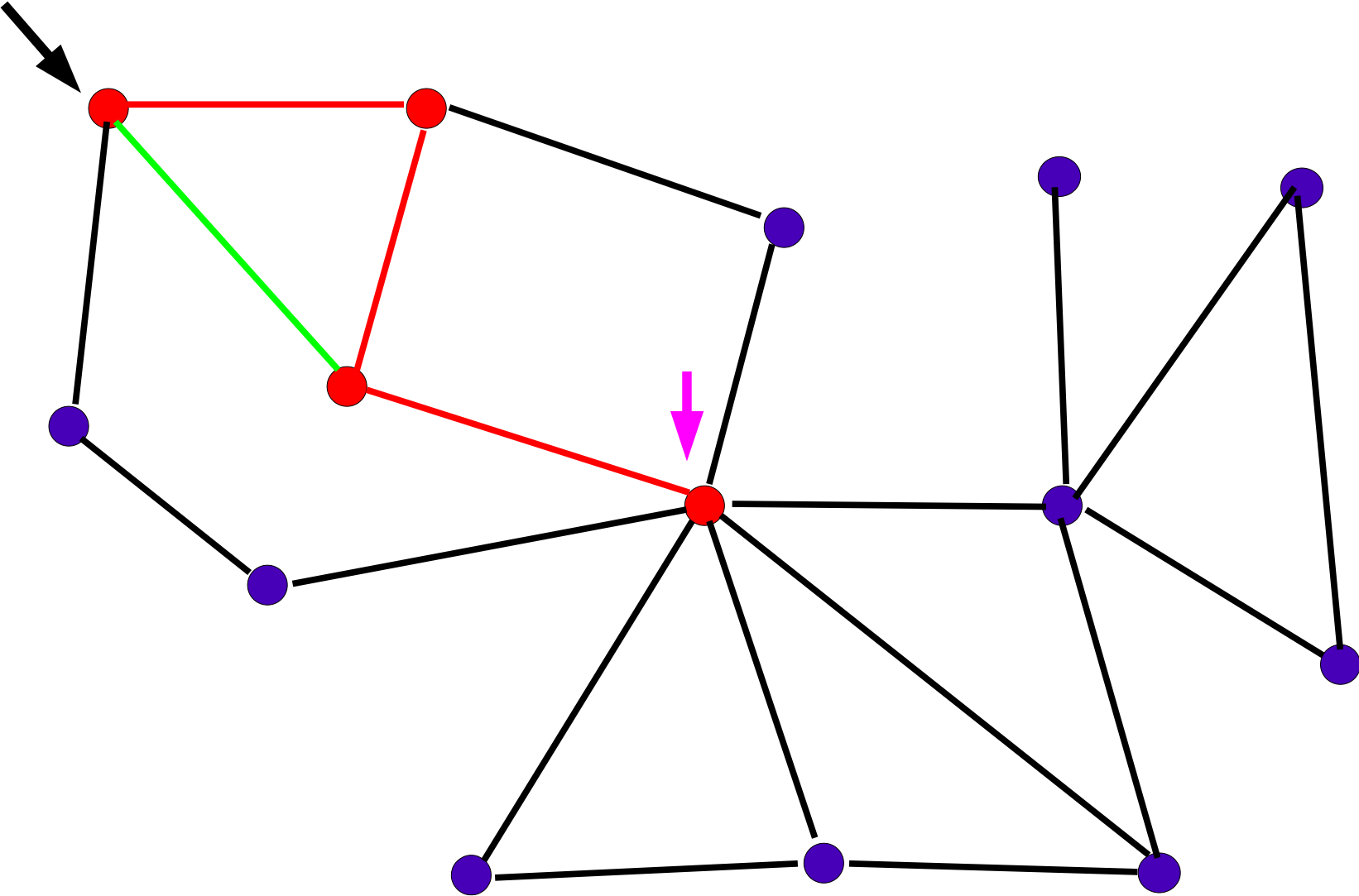
# Biconnected Components



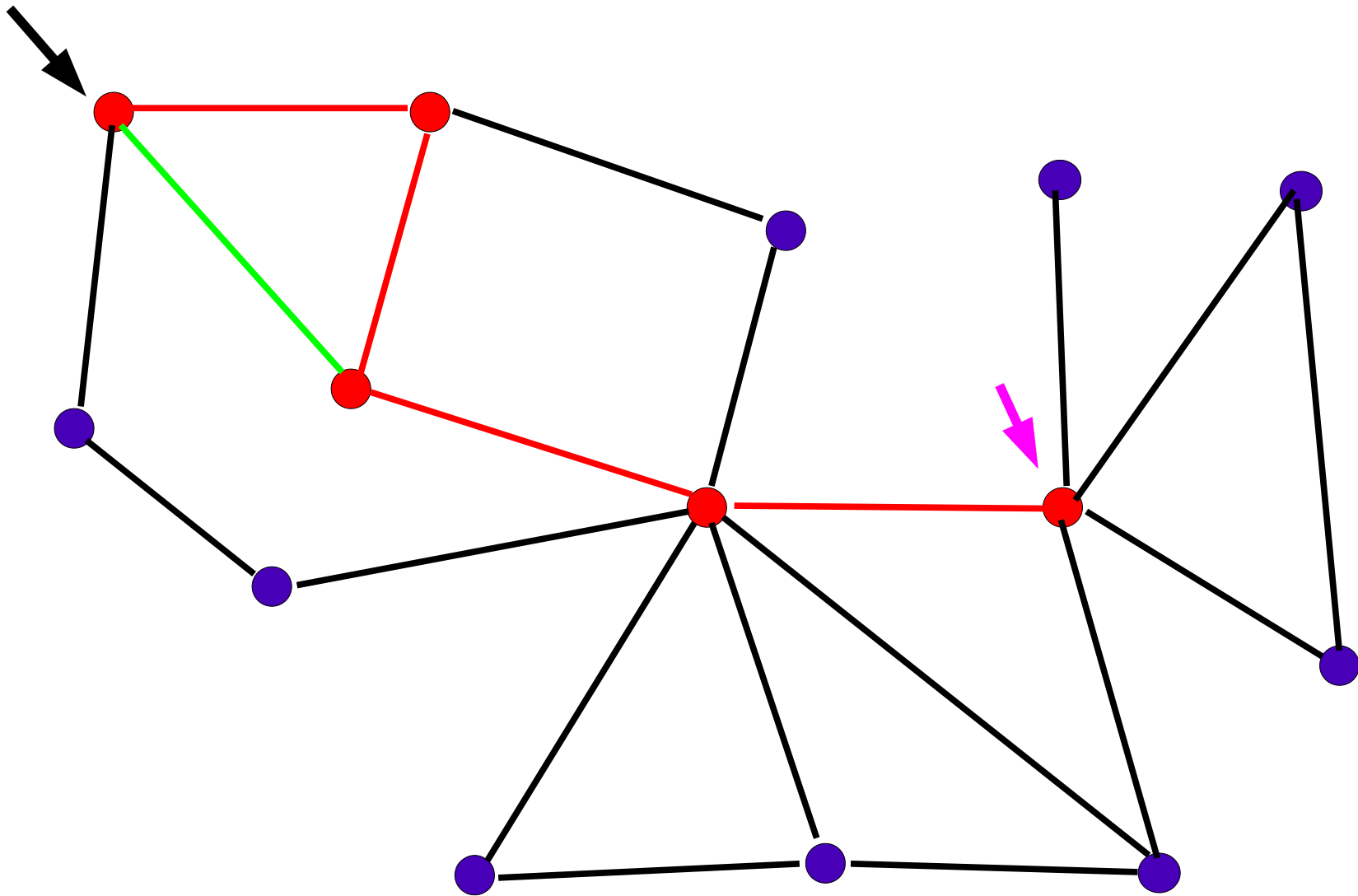
# Biconnected Components



# Biconnected Components

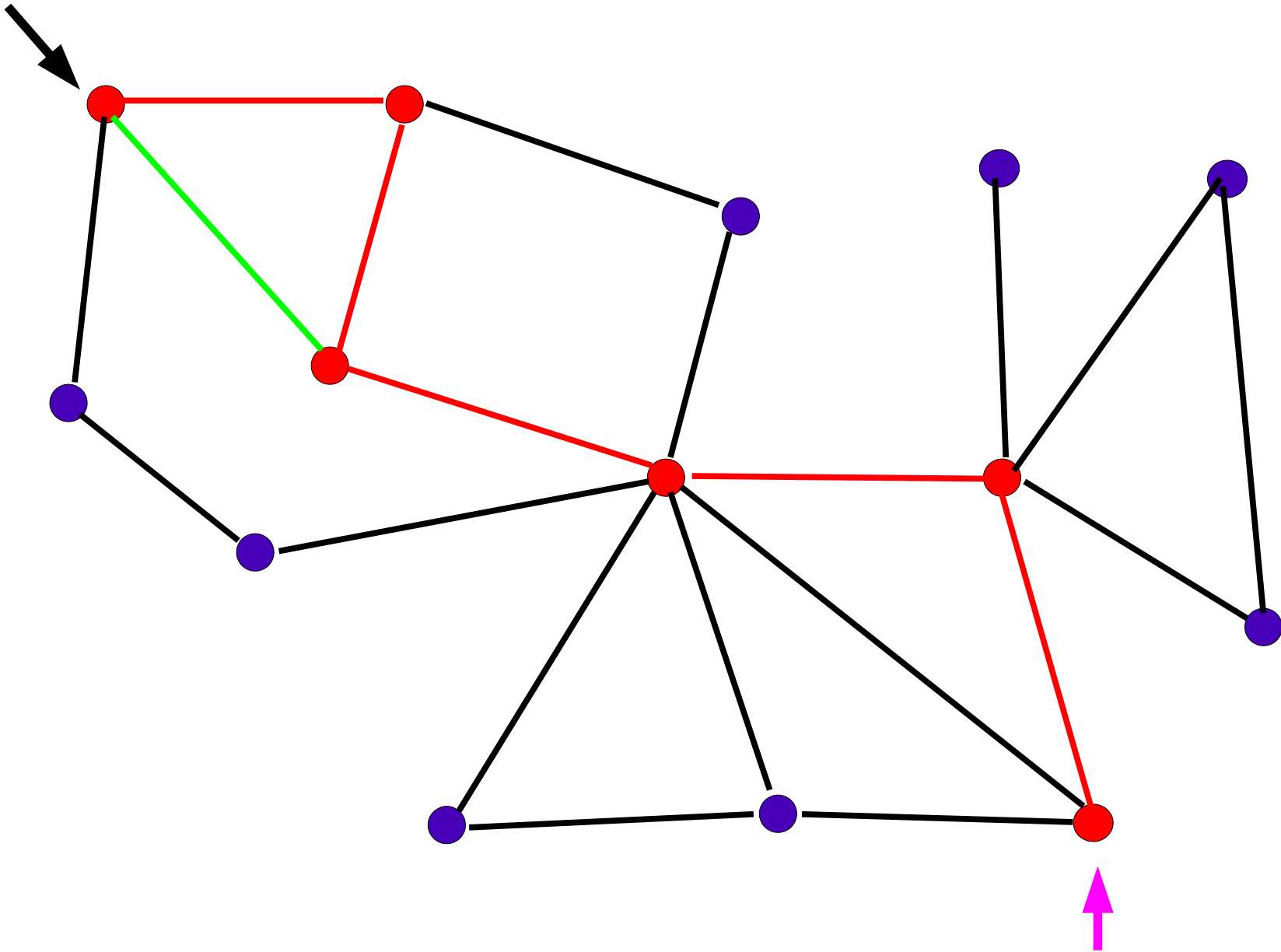


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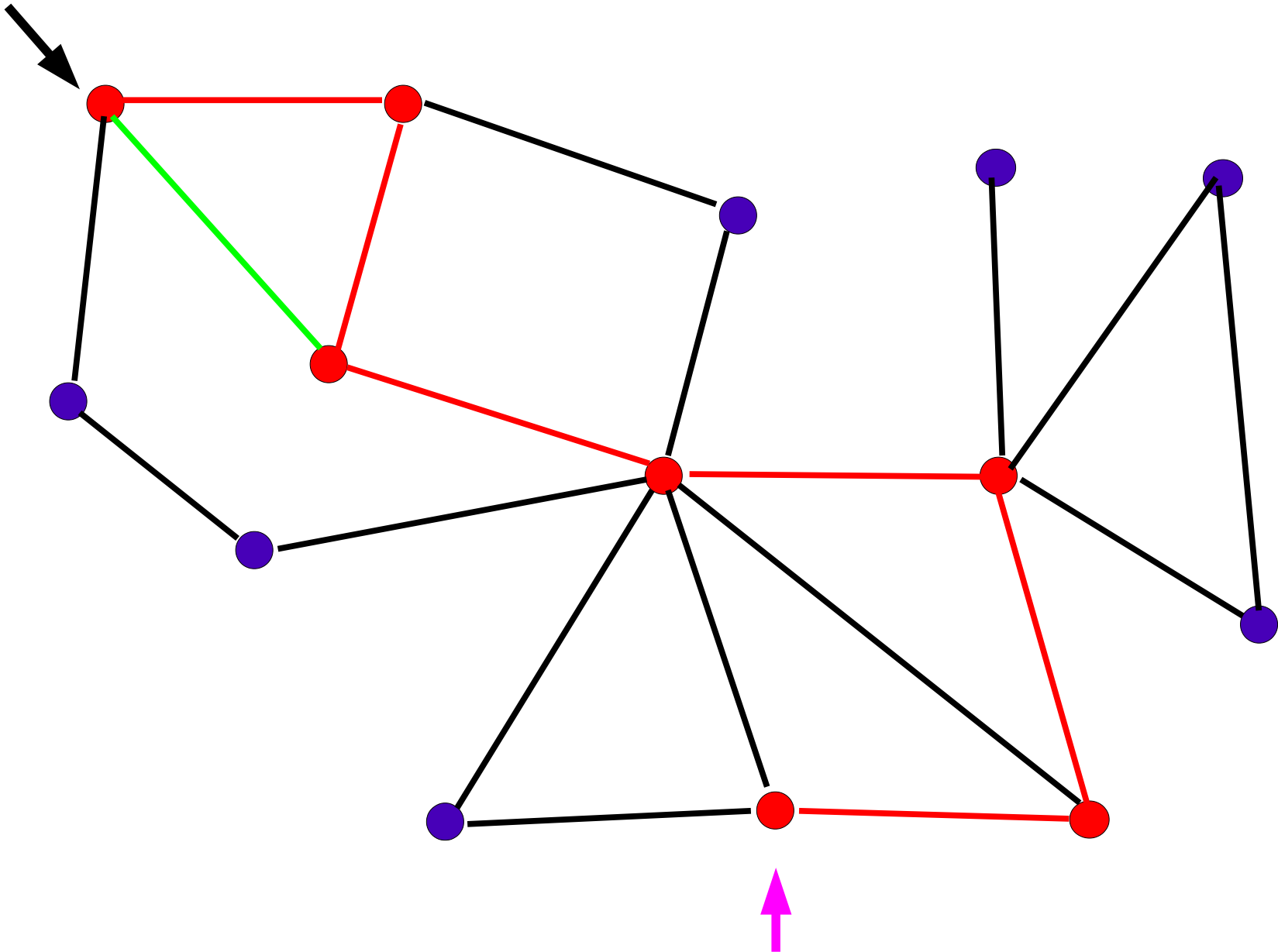




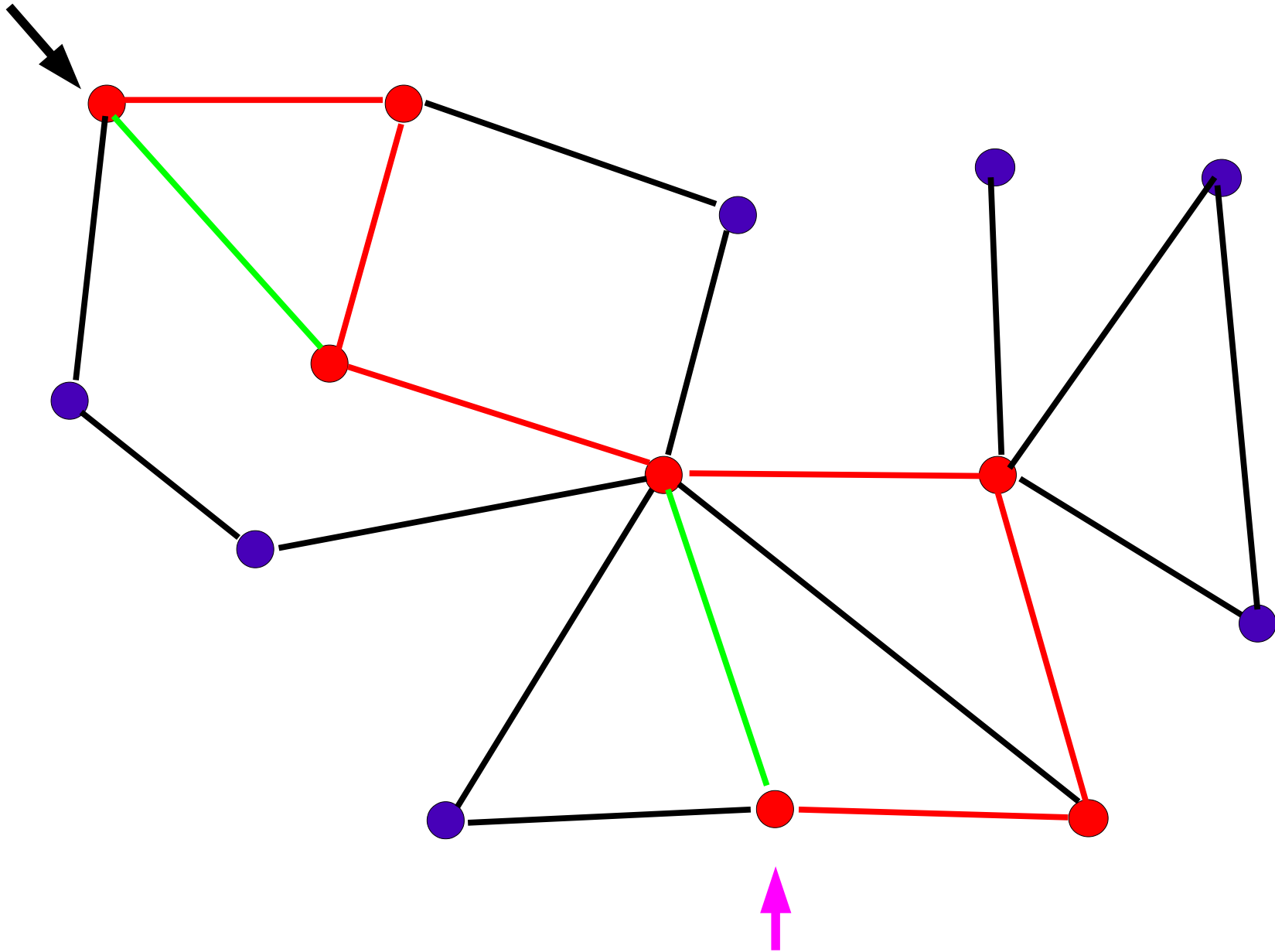
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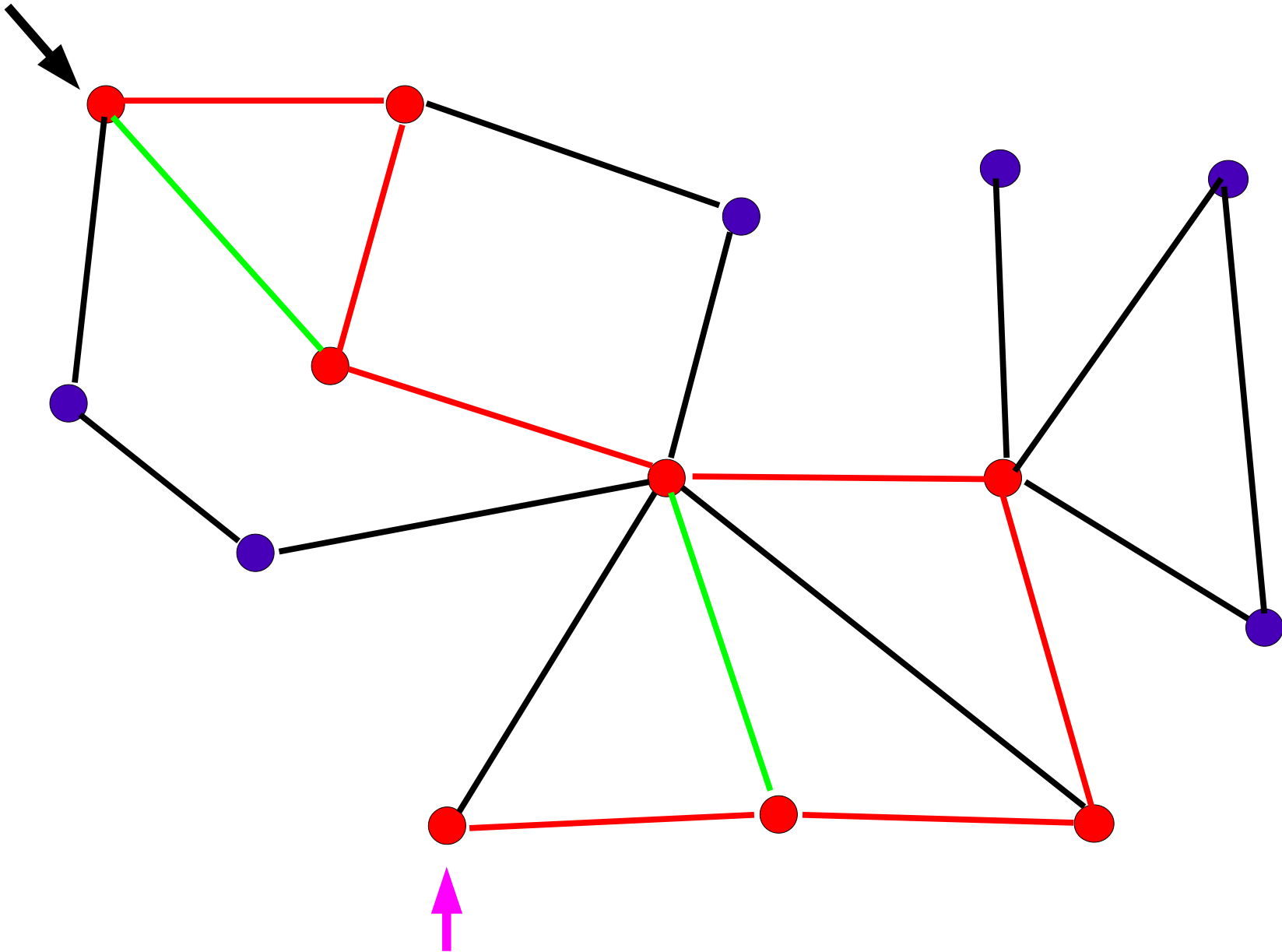
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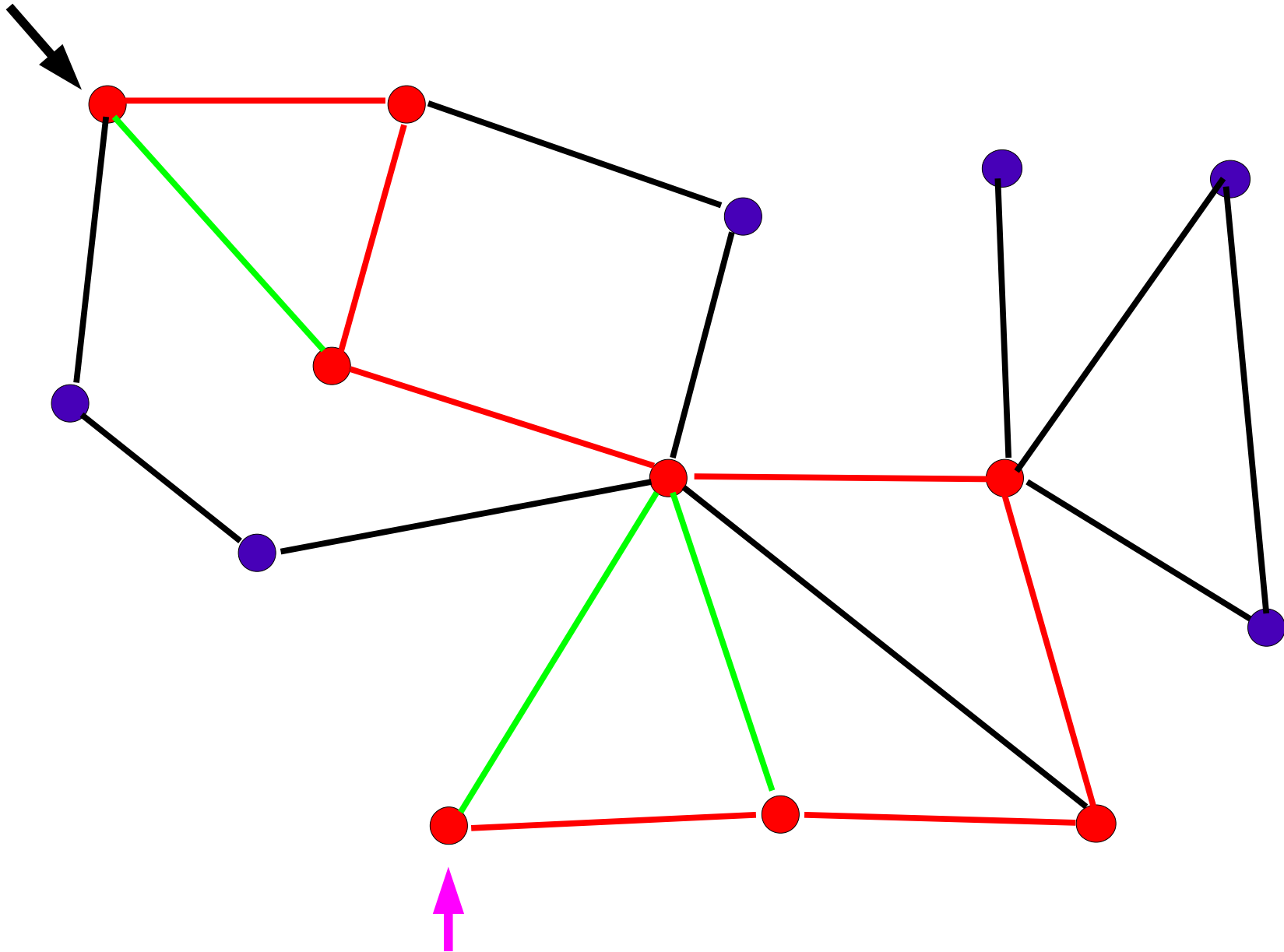
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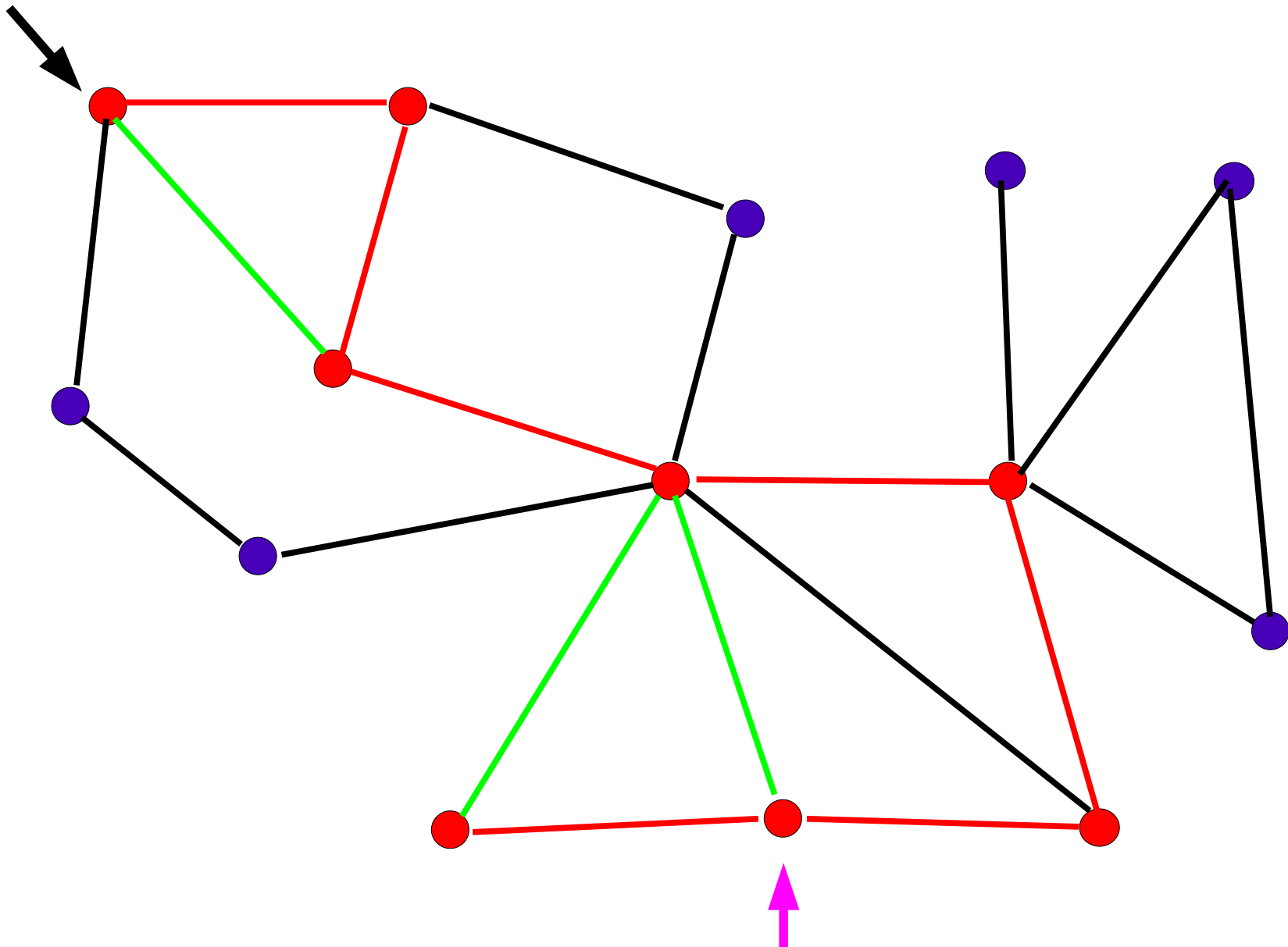
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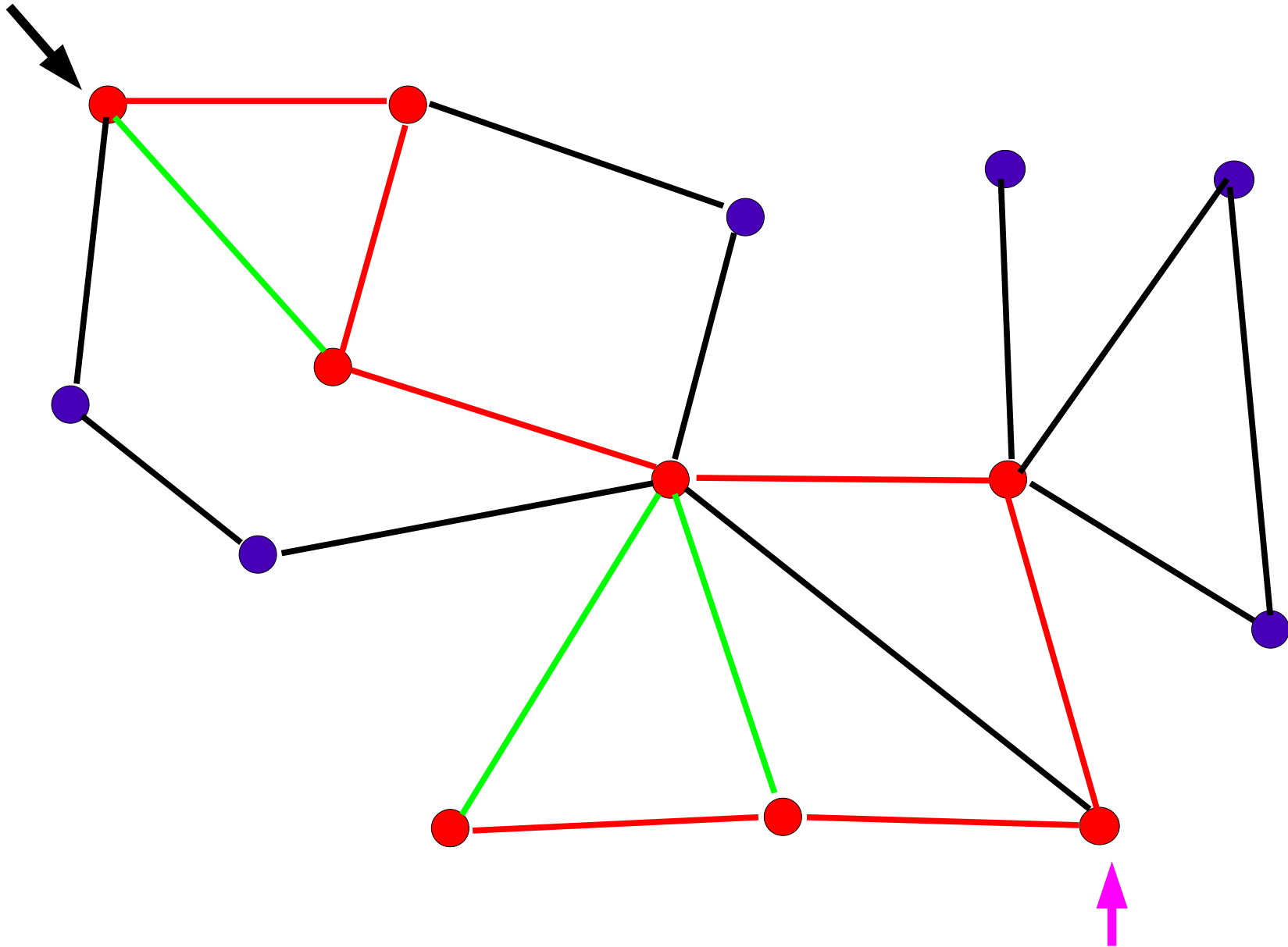
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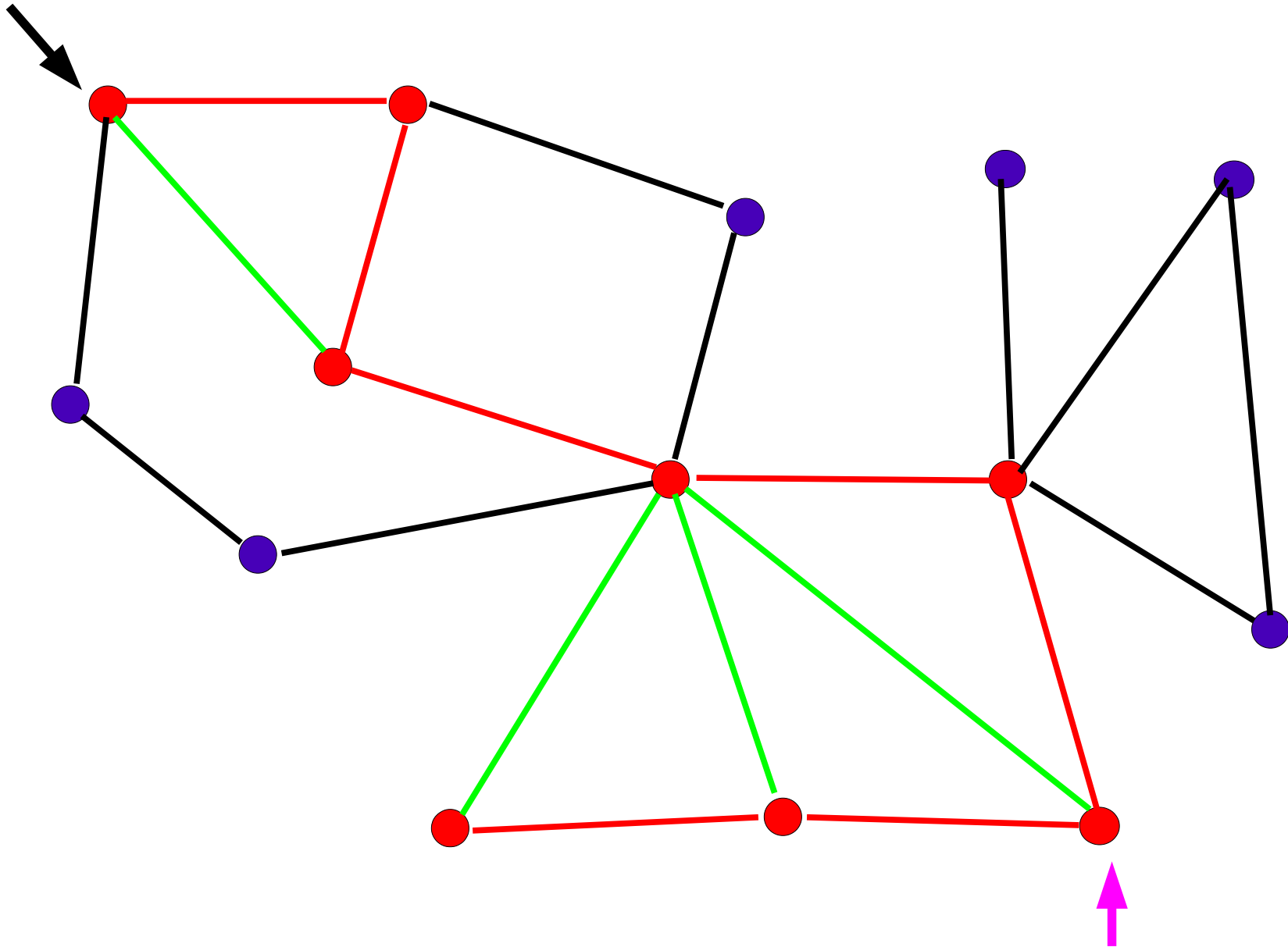
# Biconnected Components



# Biconnected Components

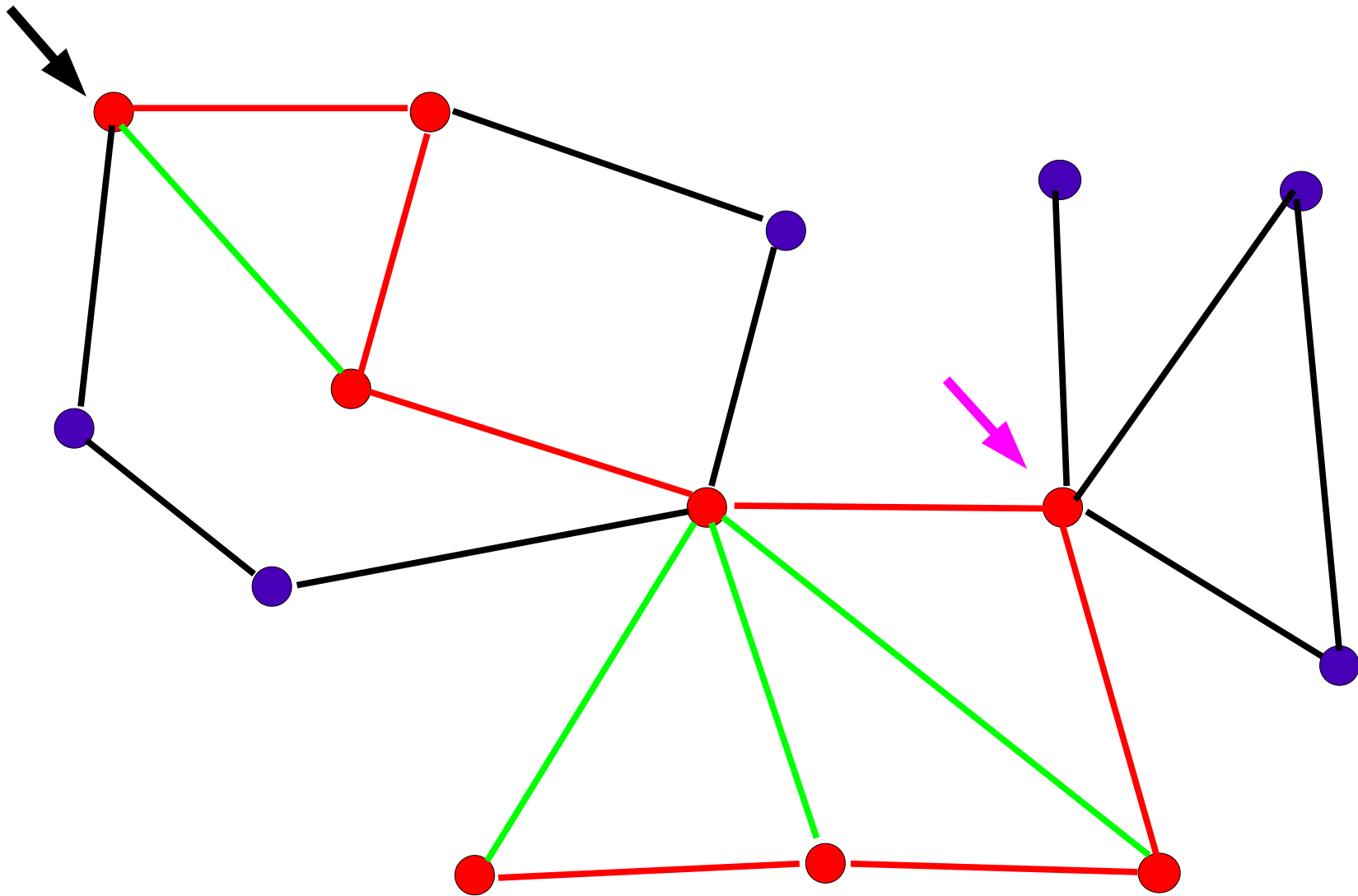


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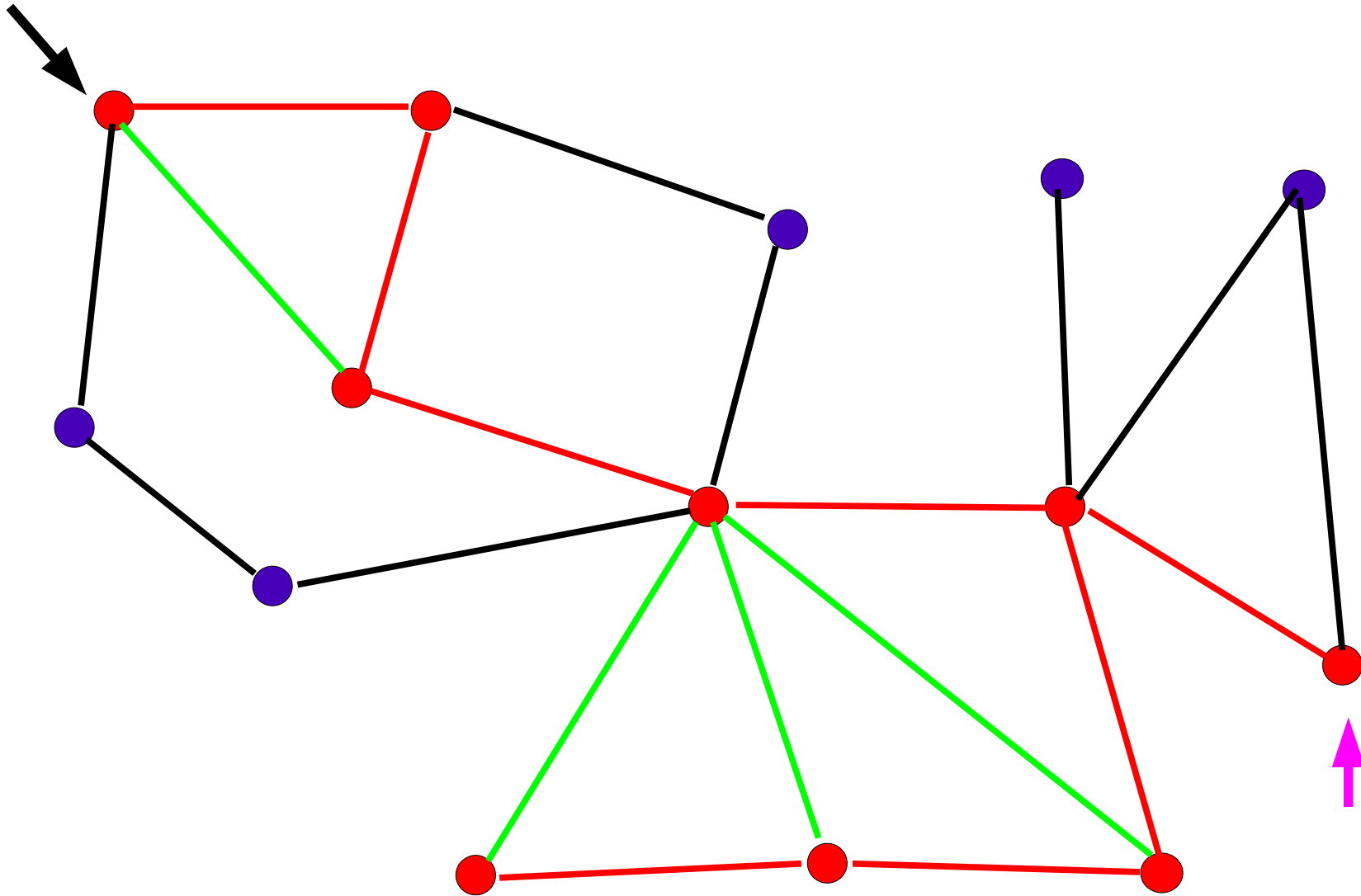




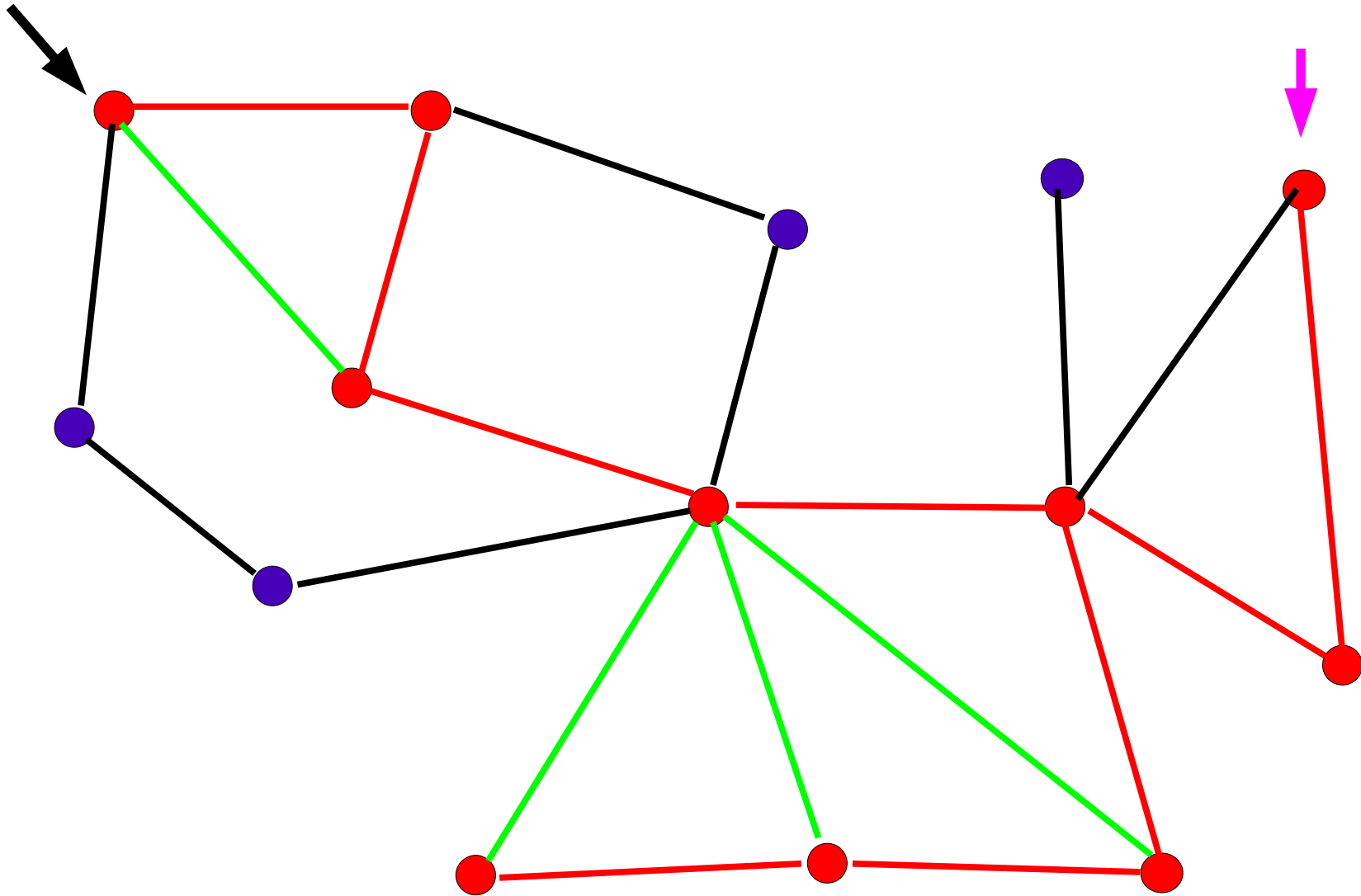
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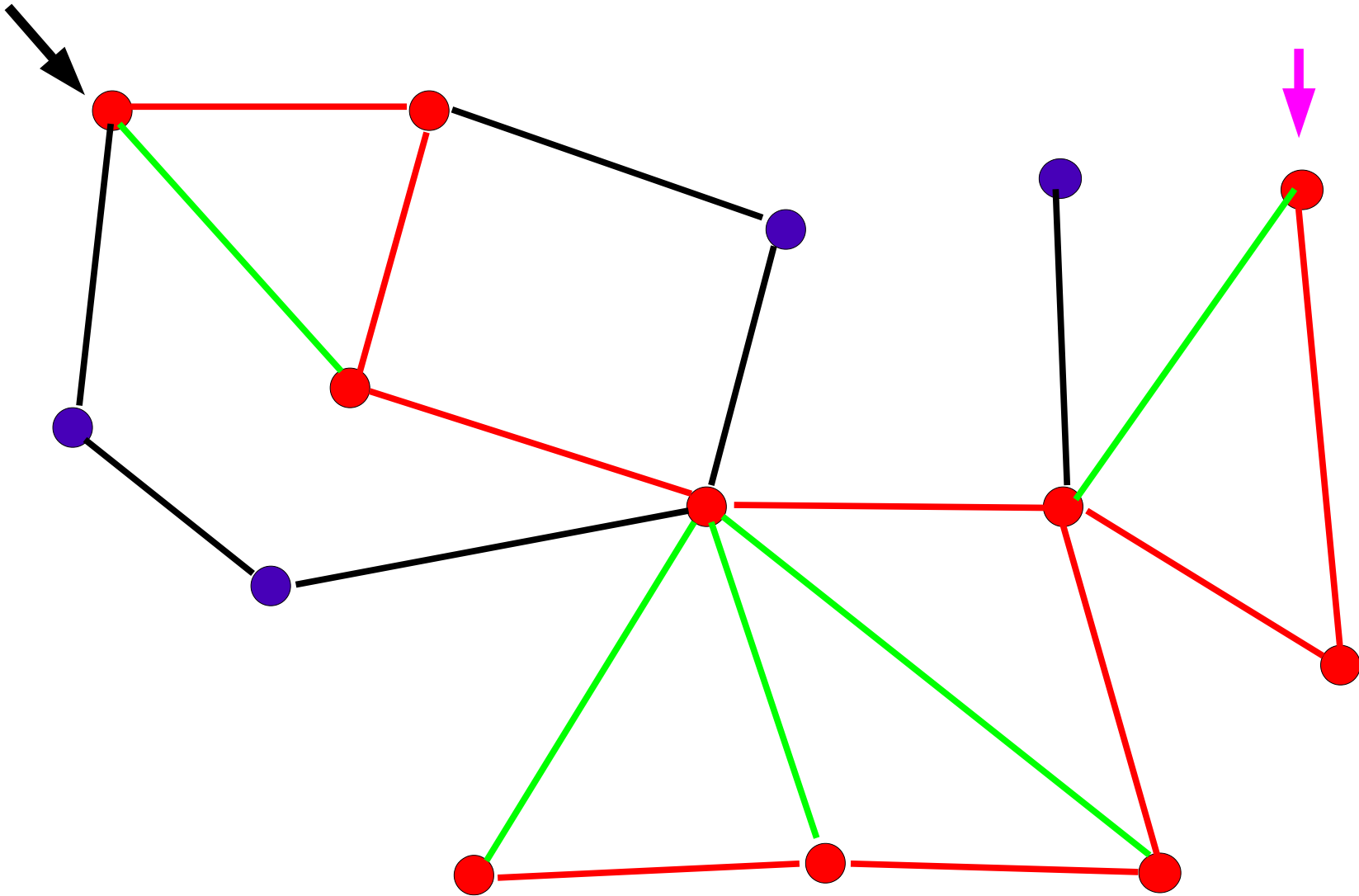
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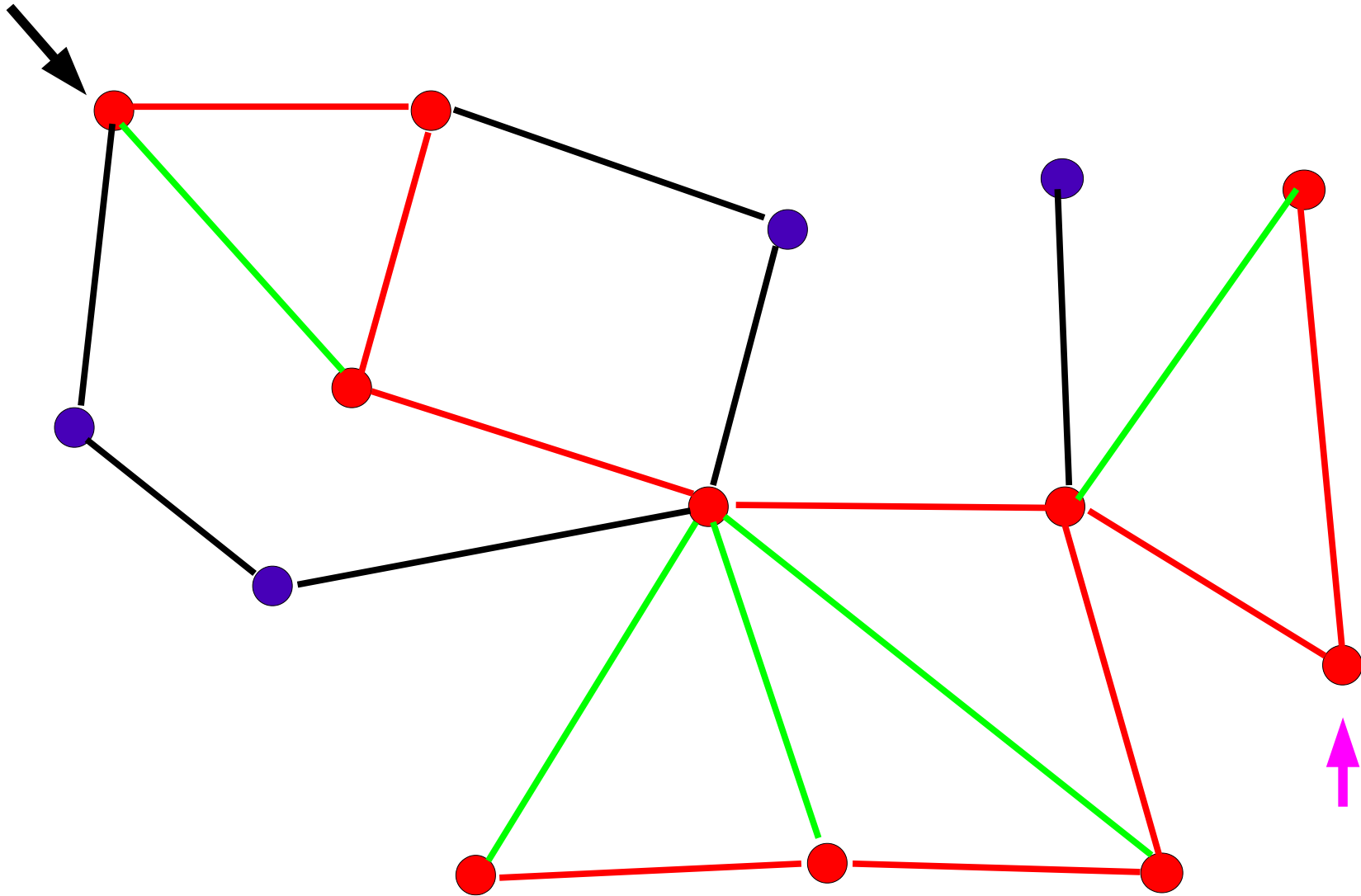
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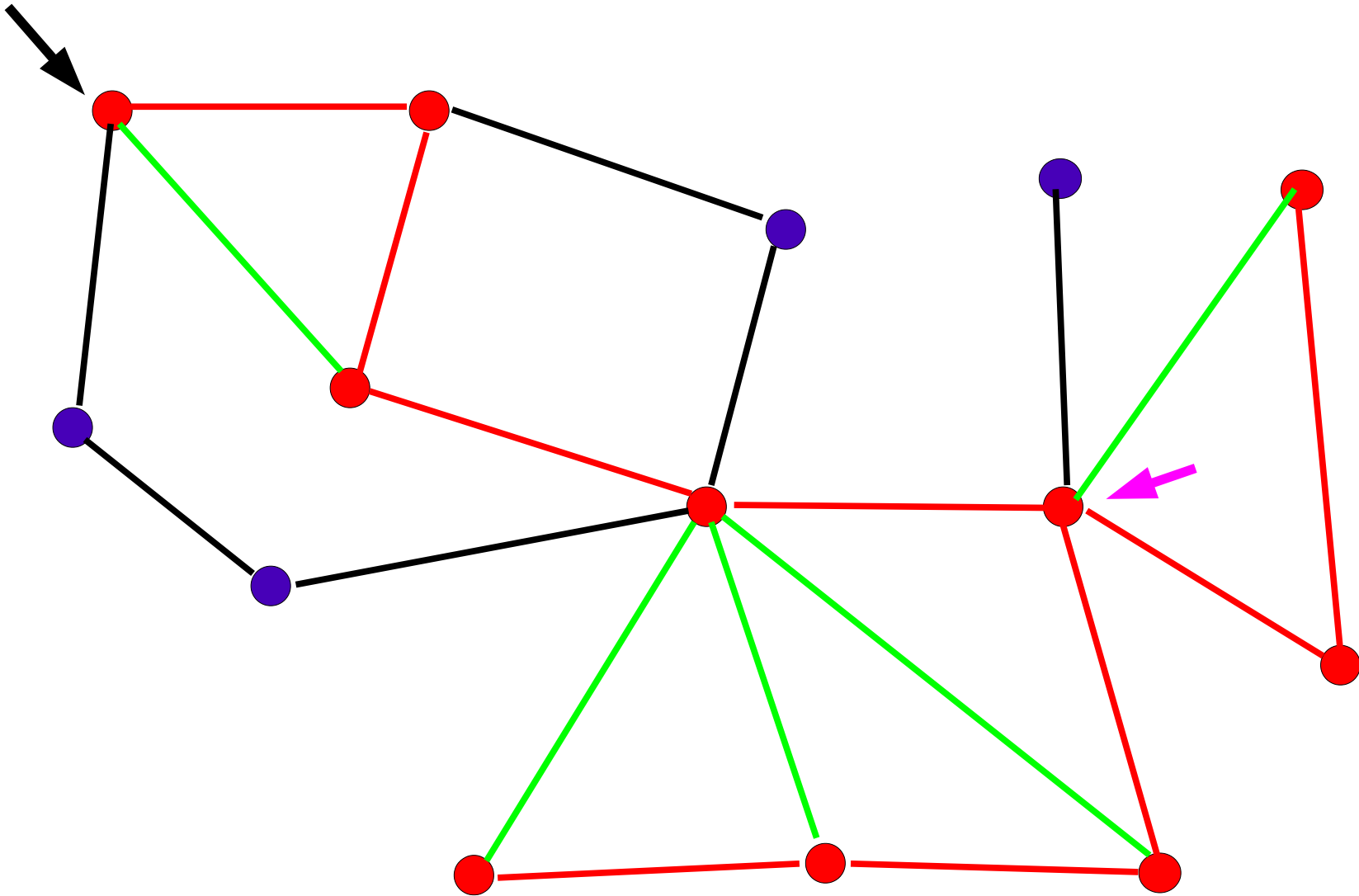
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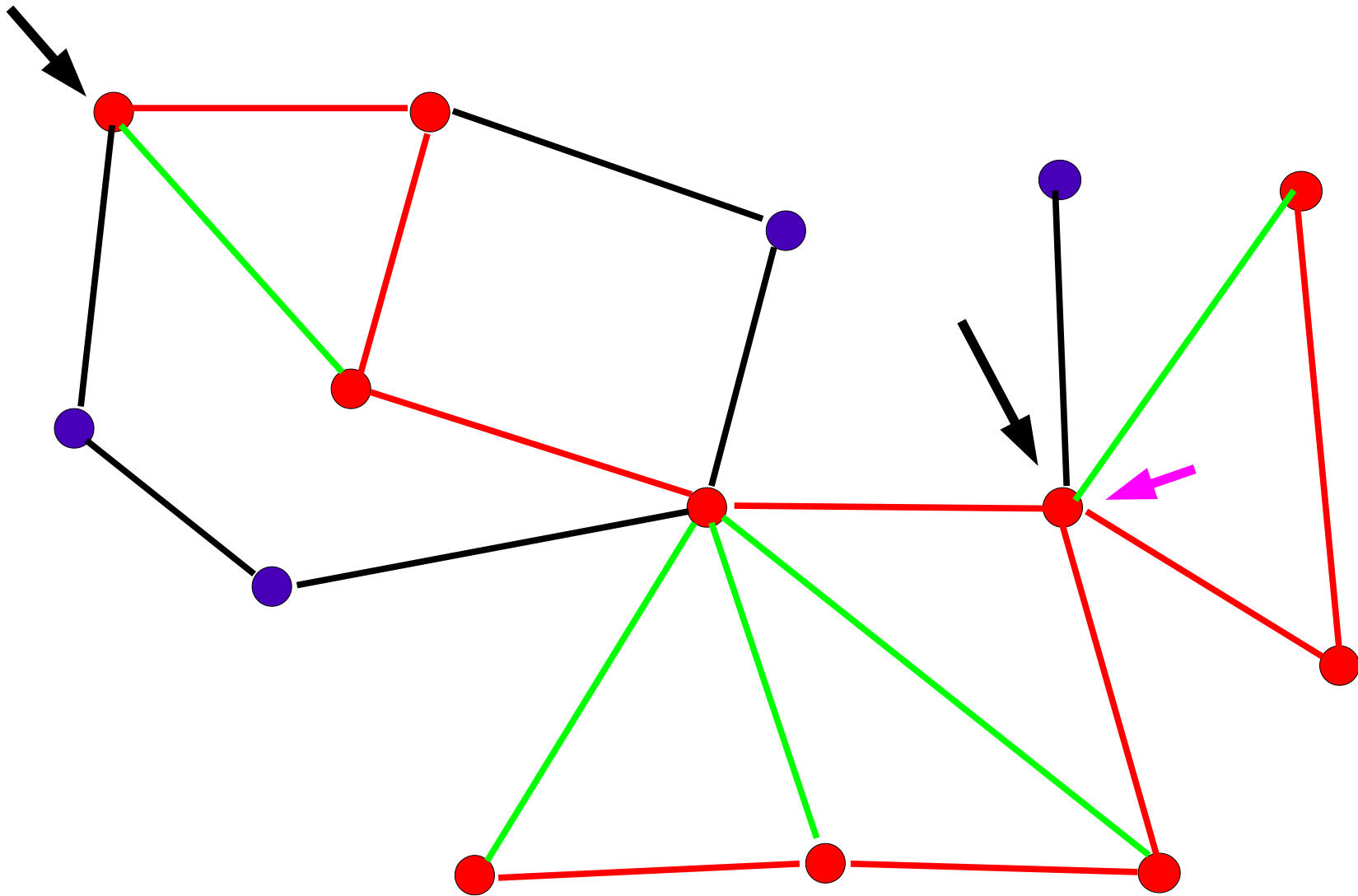
# Biconnected Components



# Biconnected Components

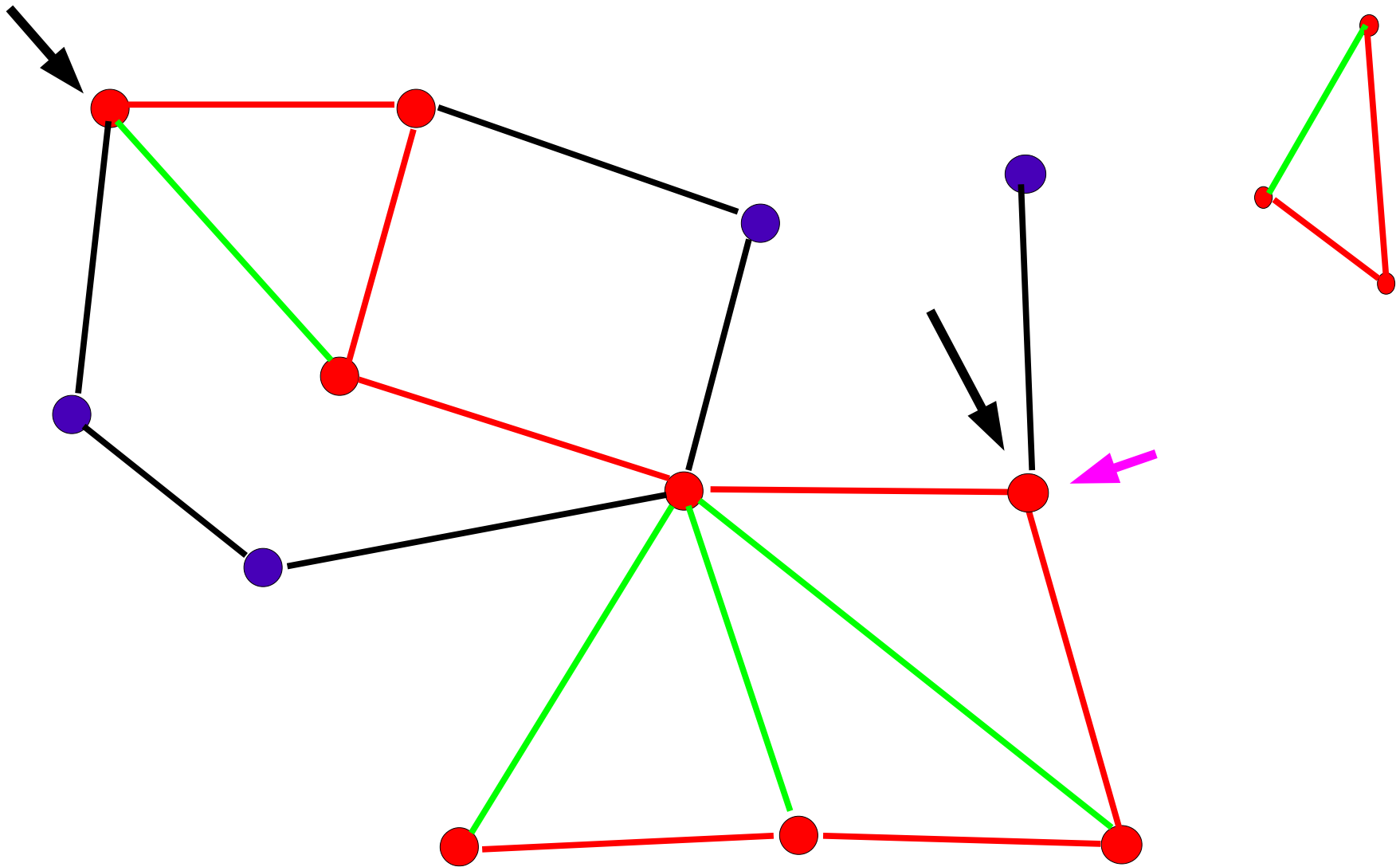


# Biconnected Components



Must be an articulation point since paths from all neighbors so far considered all lead back to this vertex

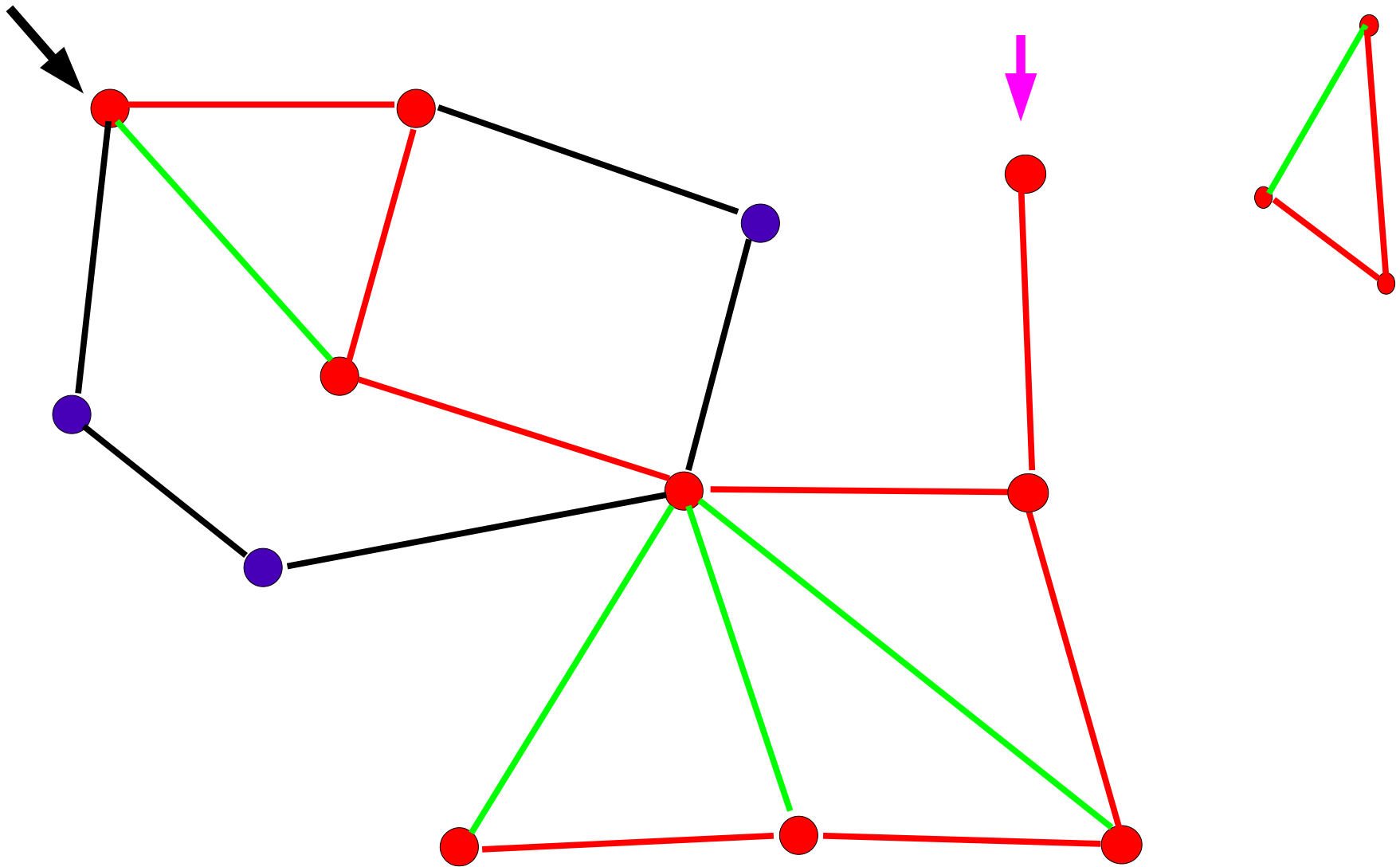
# Biconnected Components



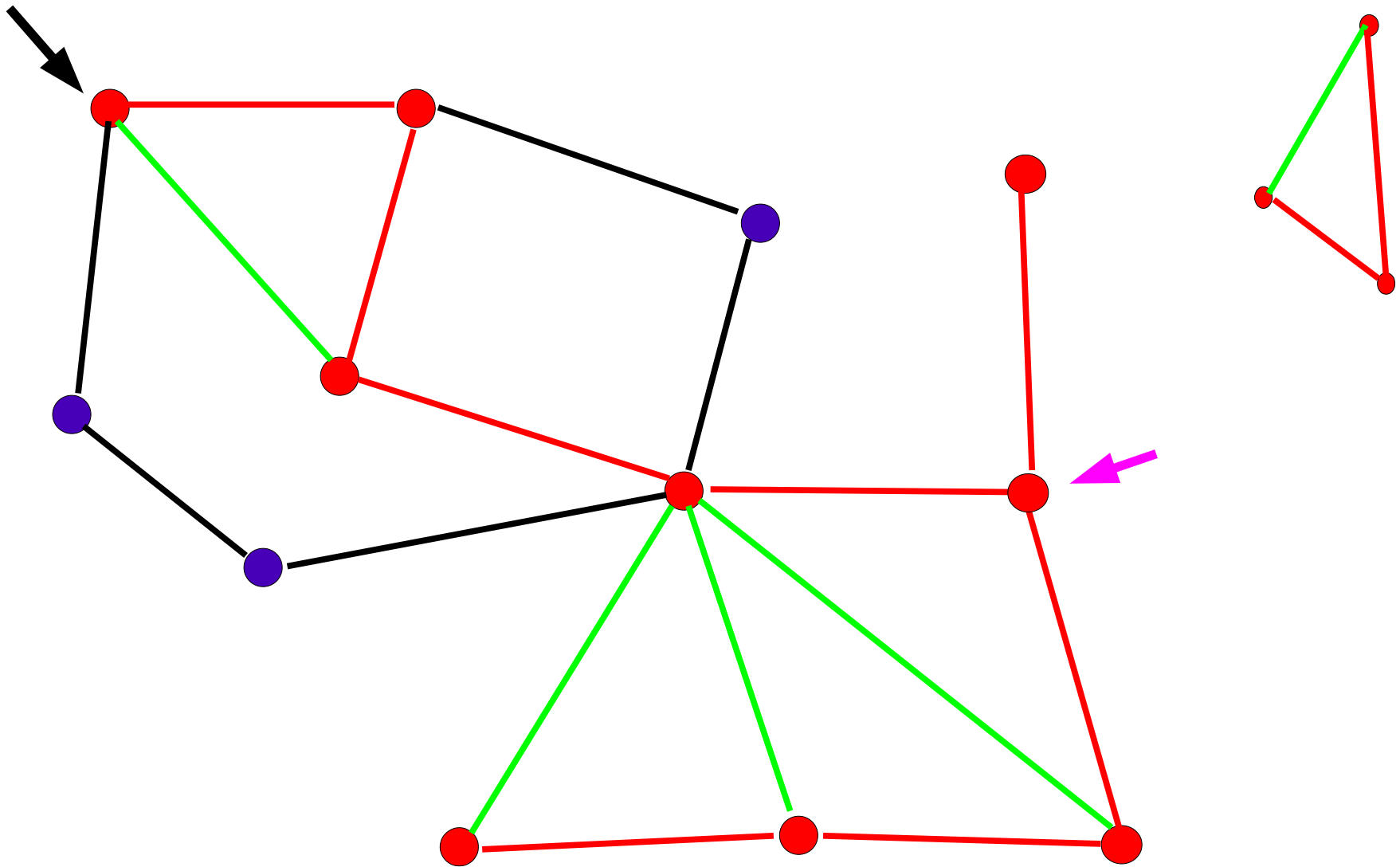
Save that biconnected component on the side and continue



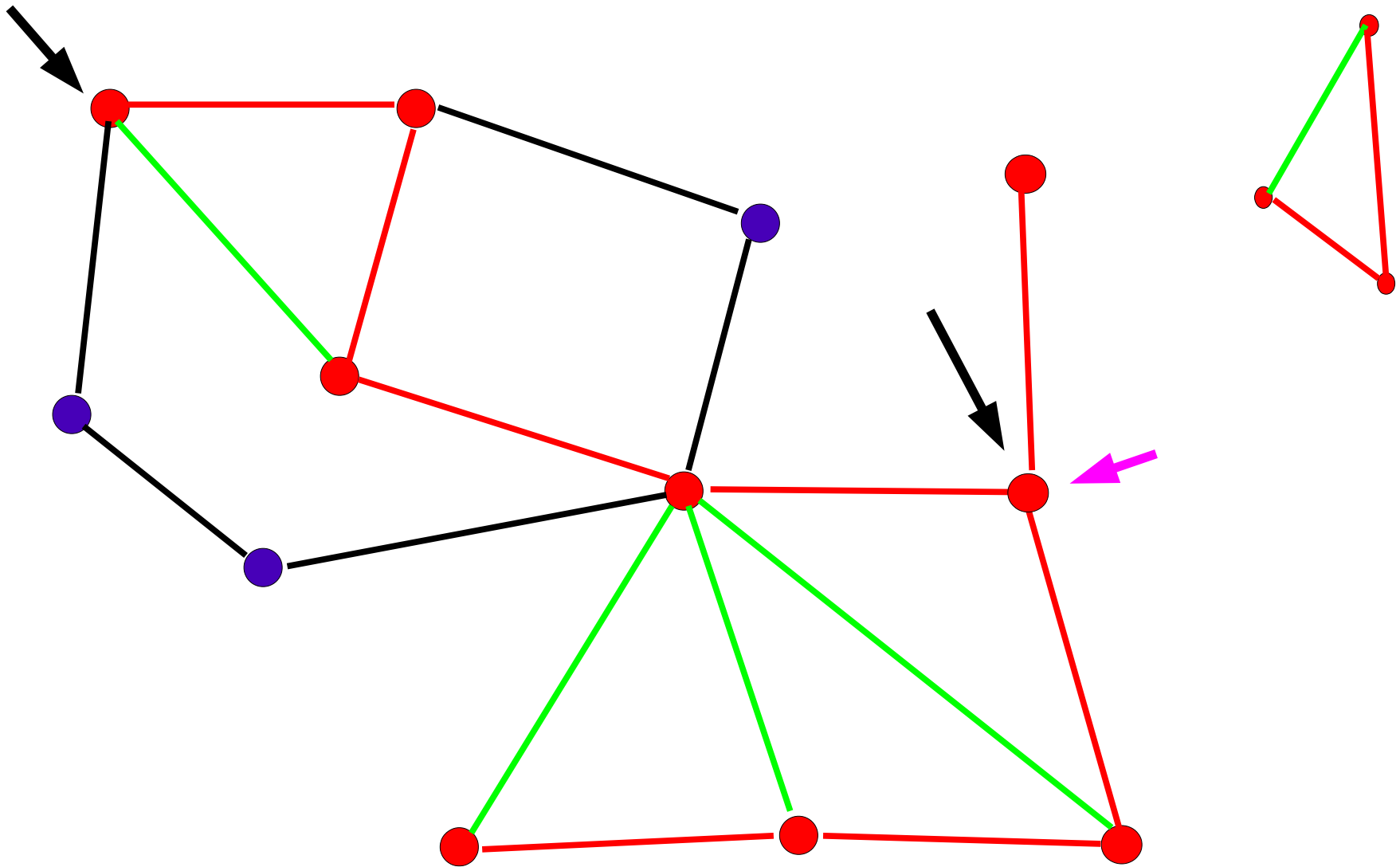
# Biconnected Components



# Biconnected Components

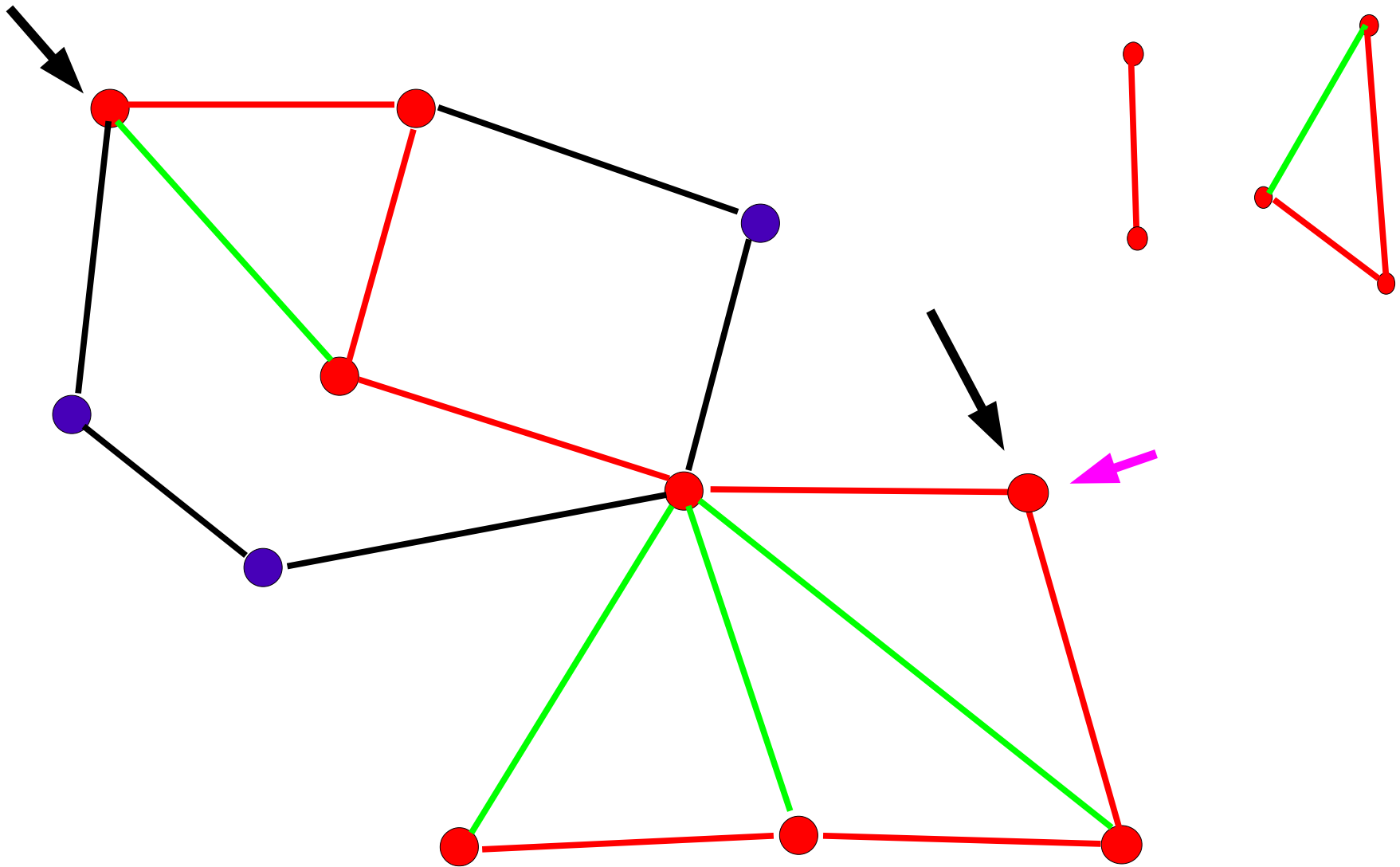


# Biconnected Components



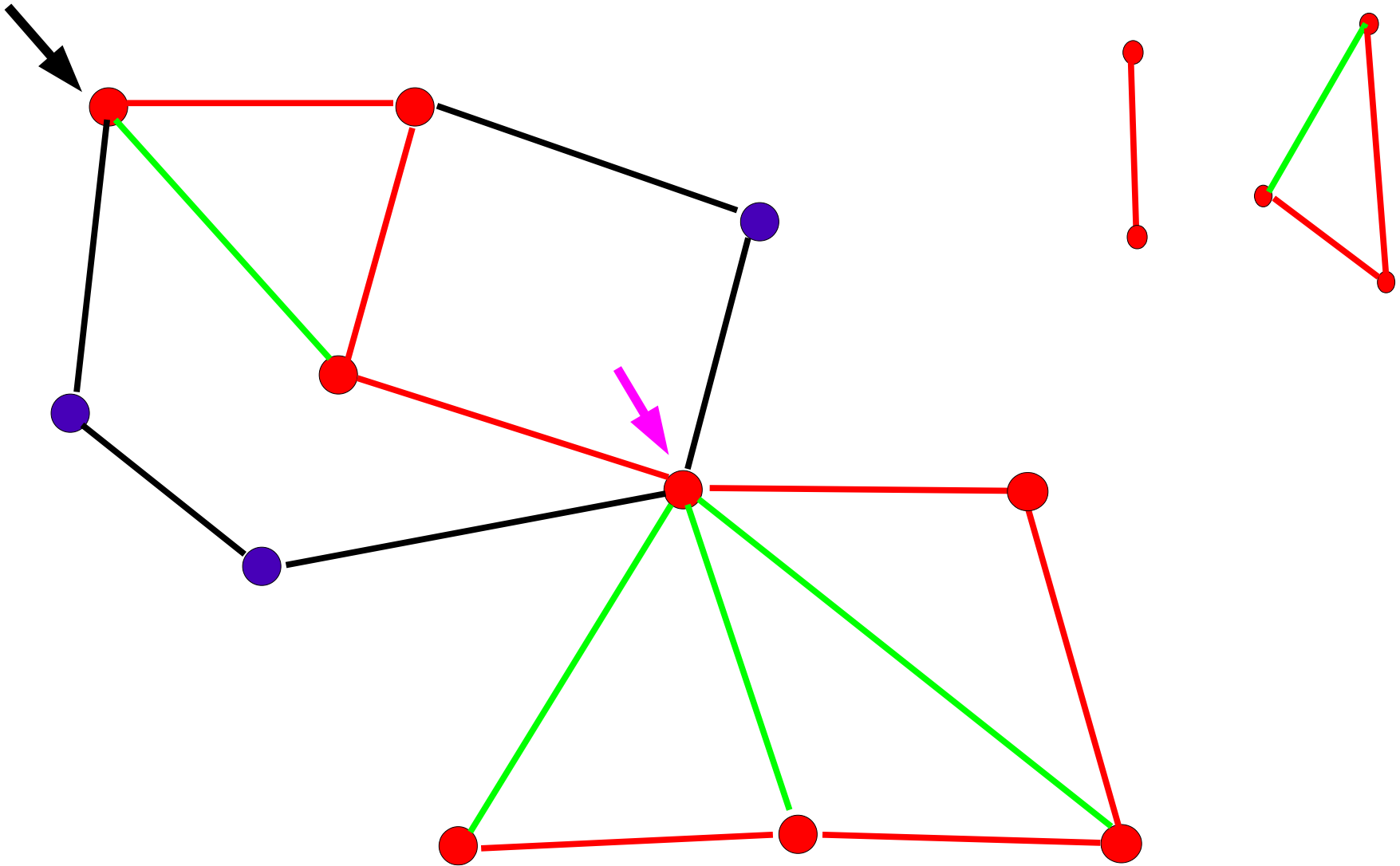
Must be an articulation point since paths from all neighbors so far considered all lead back to this vertex

# Biconnected Components

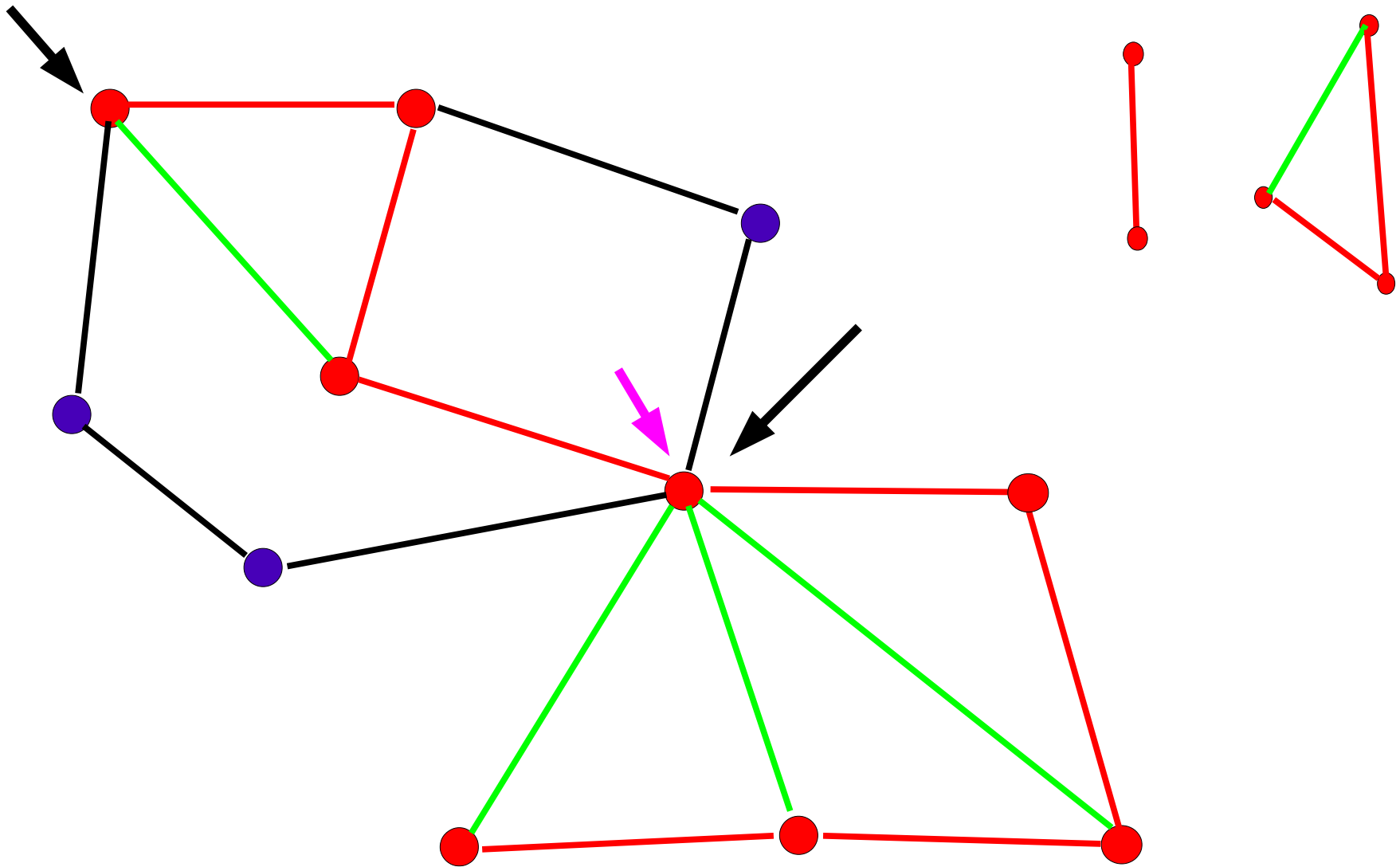


Save that biconnected component on the side and continue

# Biconnected Components

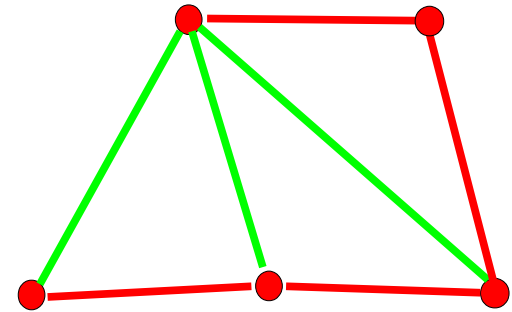
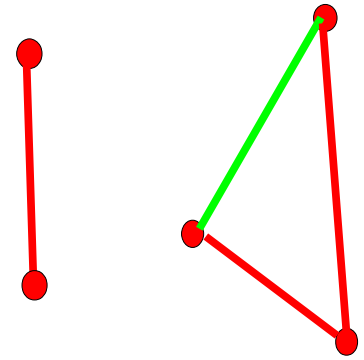
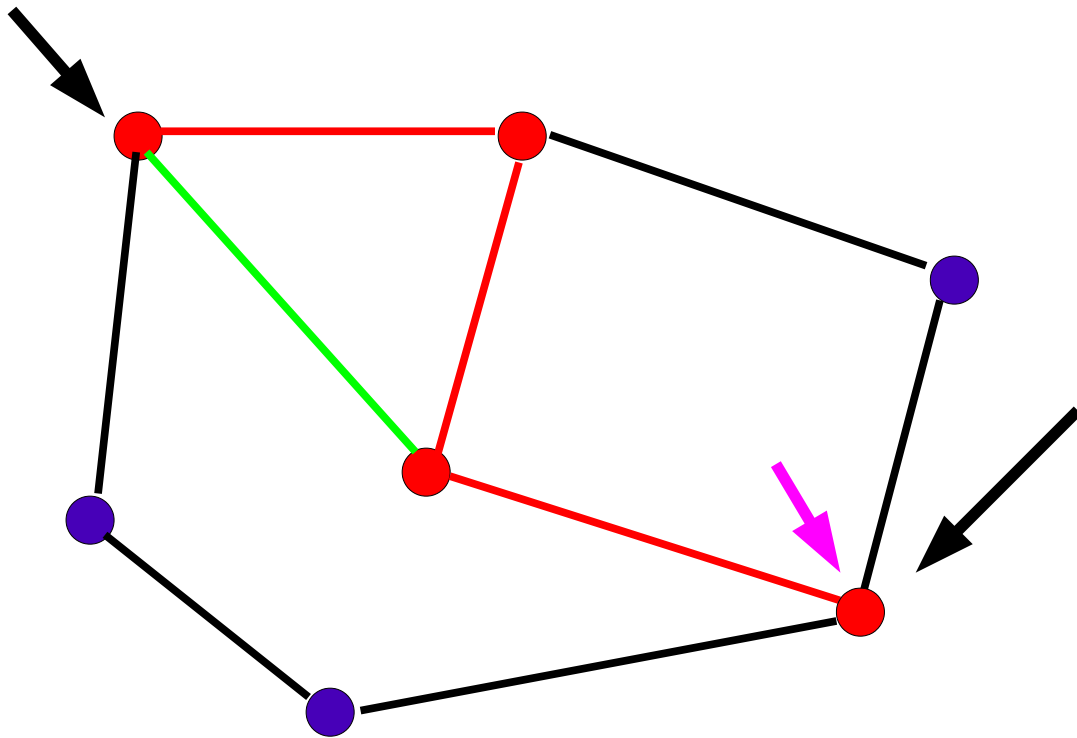


# Biconnected Components



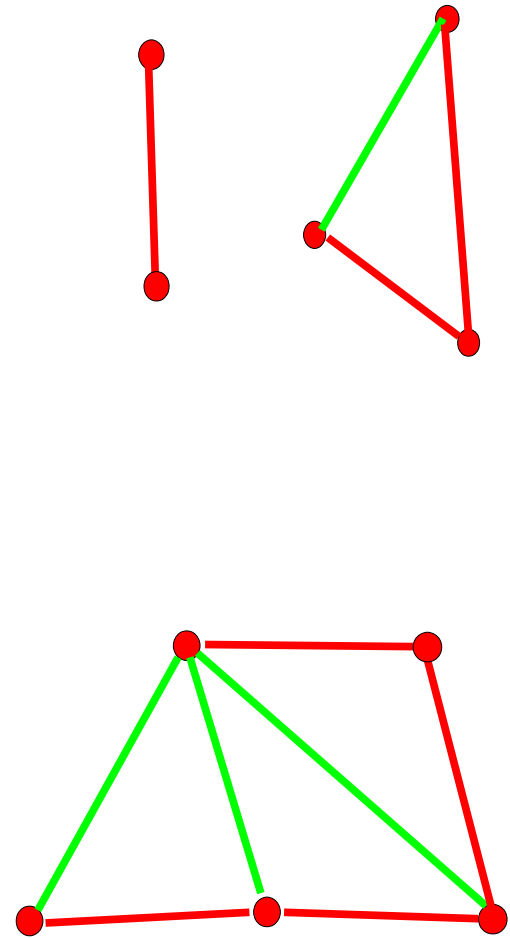
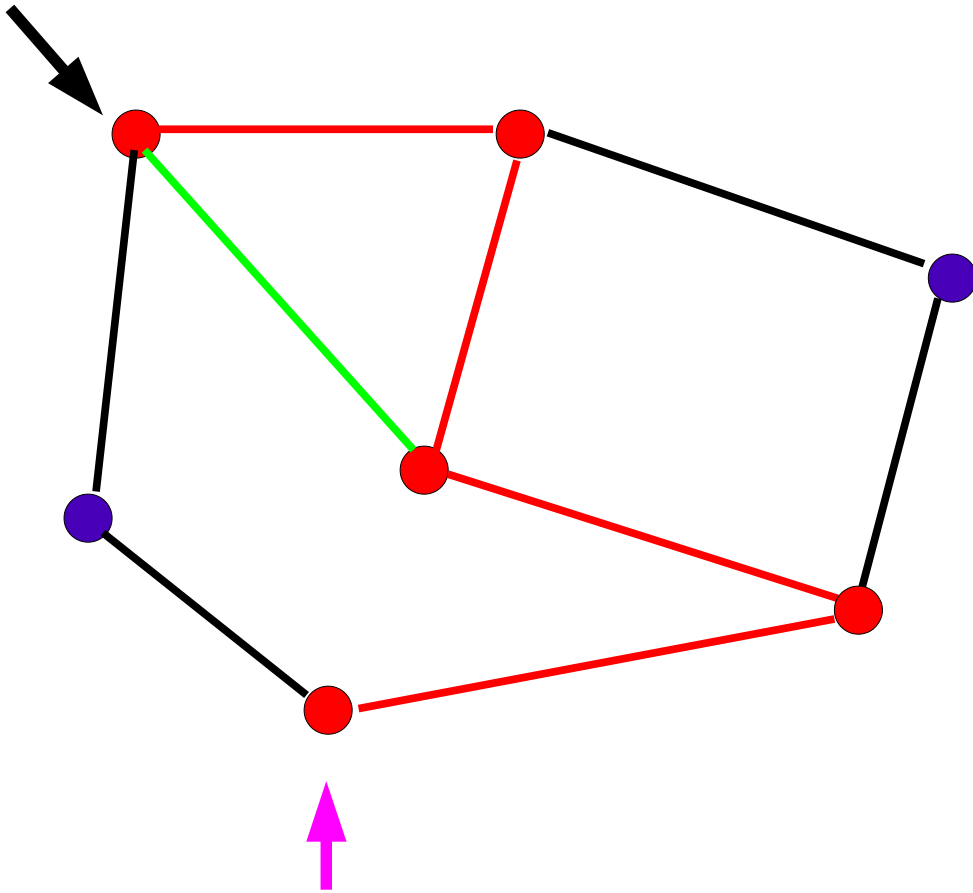
Must be an articulation point since paths from all neighbors so far considered all lead back to this vertex

# Biconnected Components



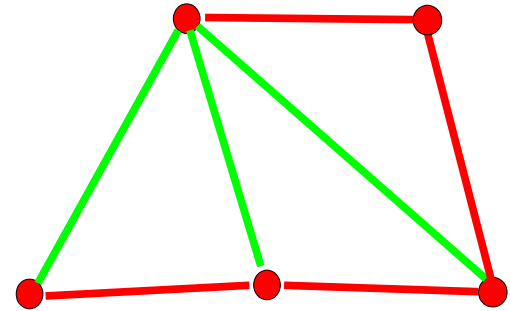
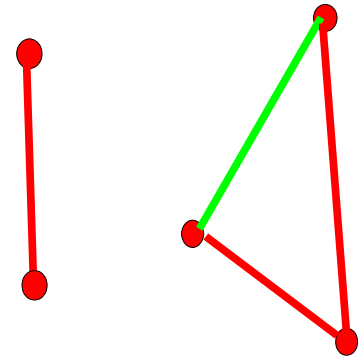
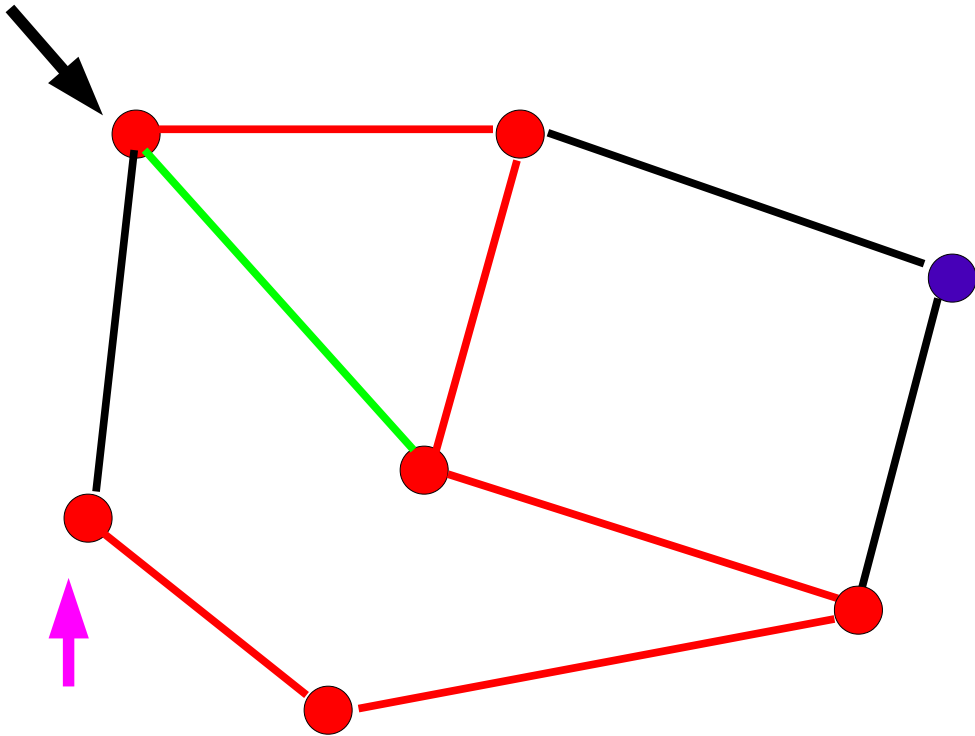
Save that biconnected component on the side and continue

# Biconnected Components

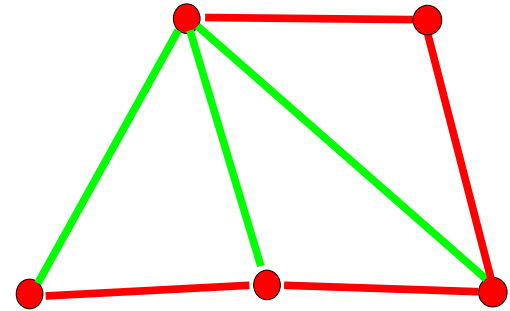
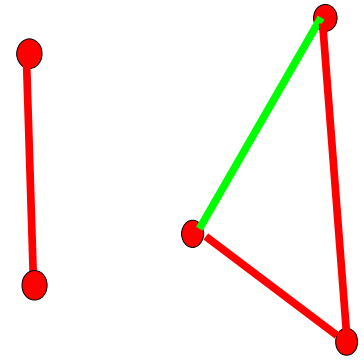
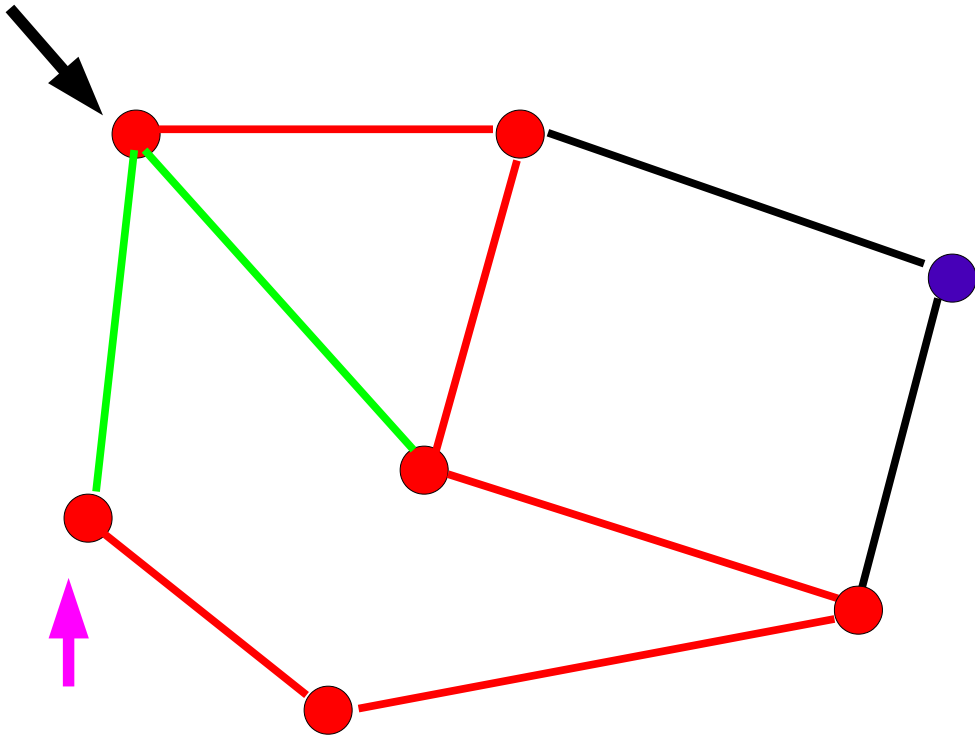




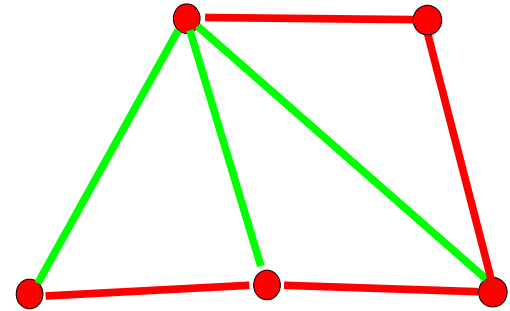
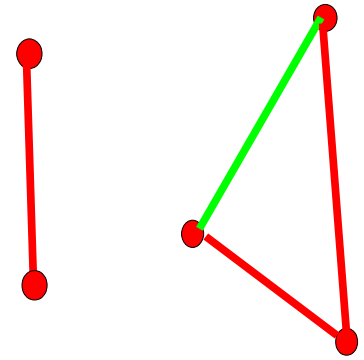
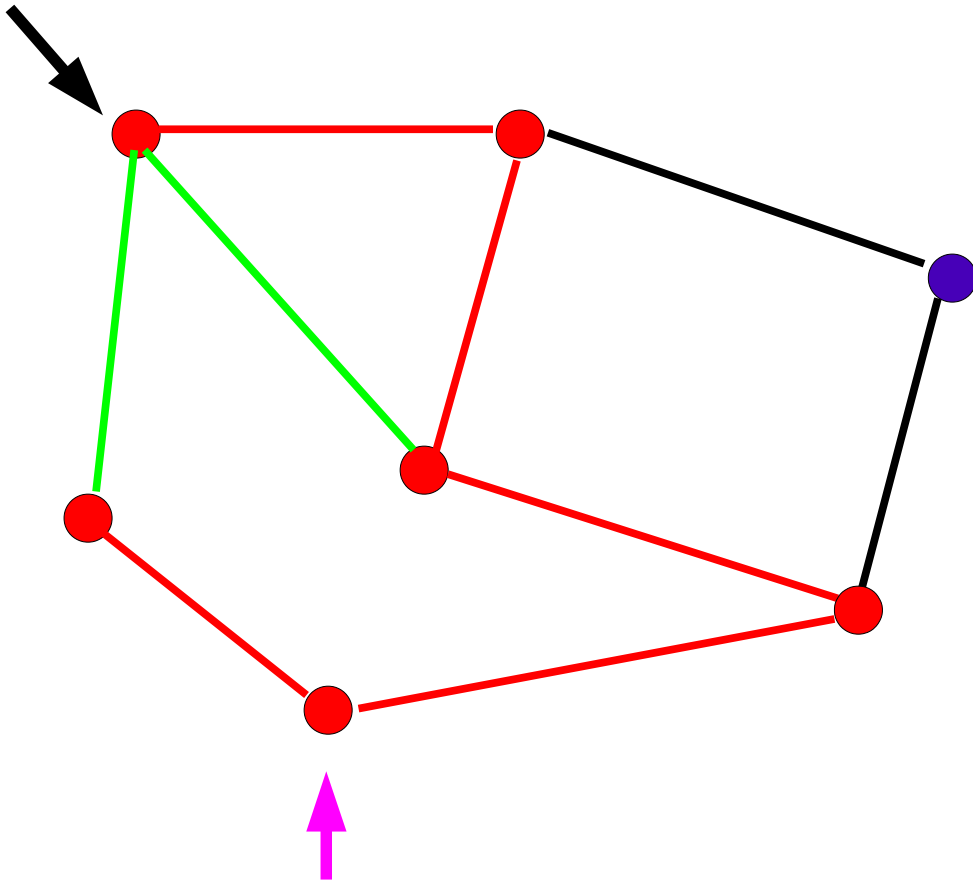
# Biconnected Components



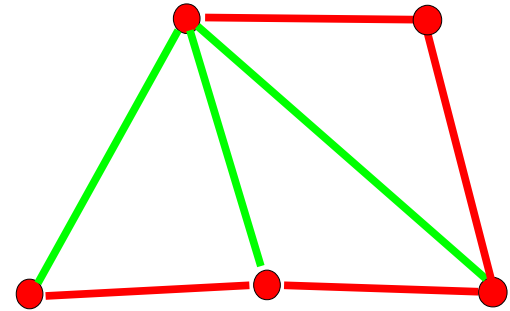
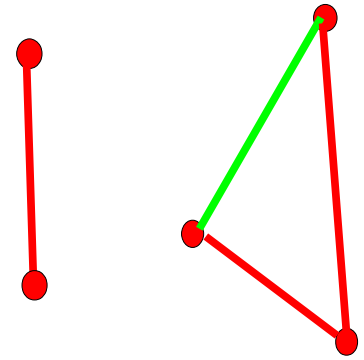
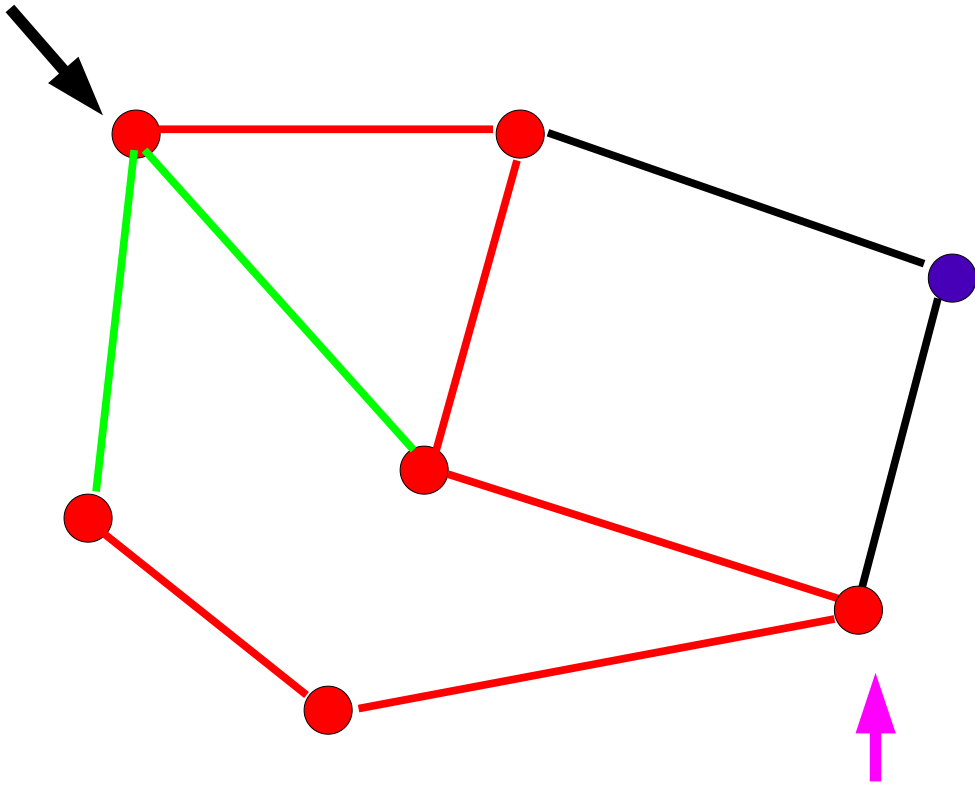
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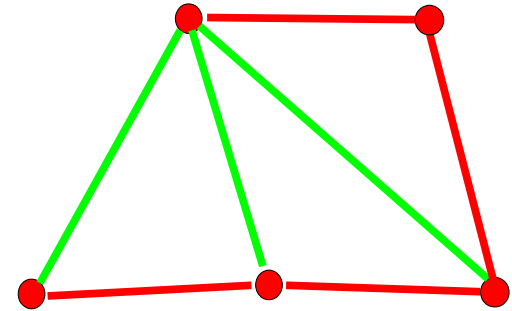
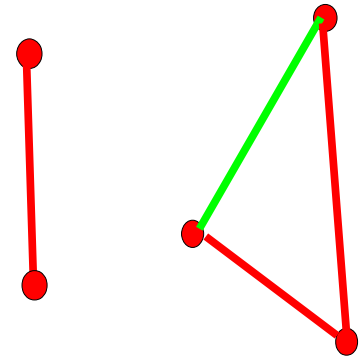
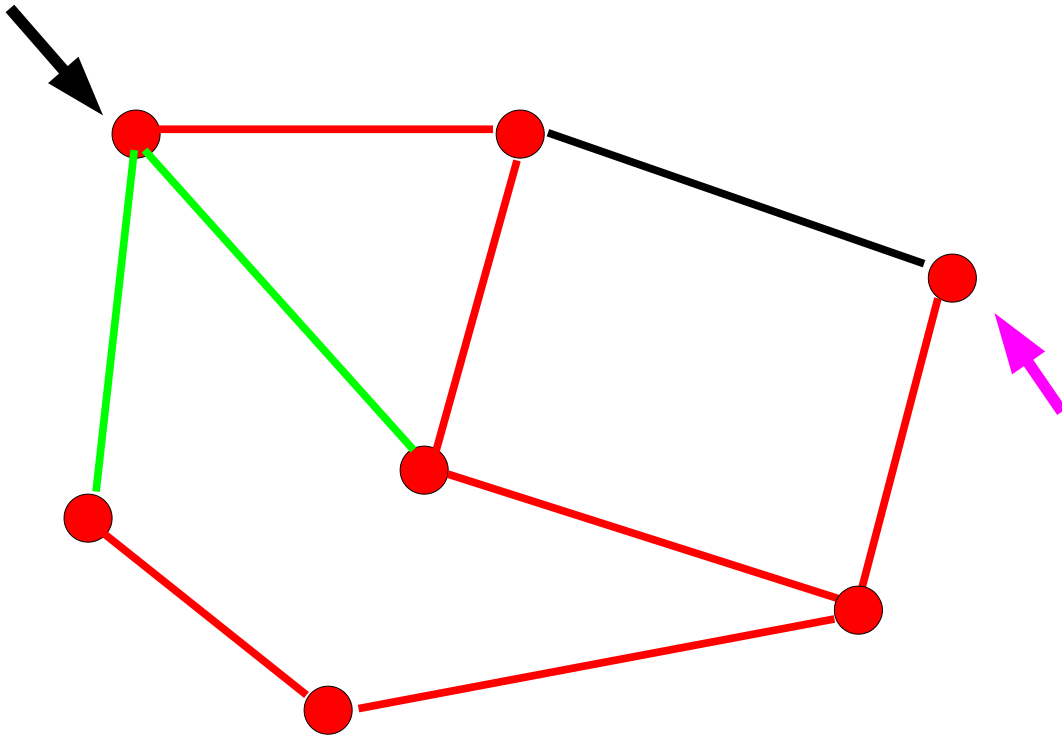
# Biconnected Components



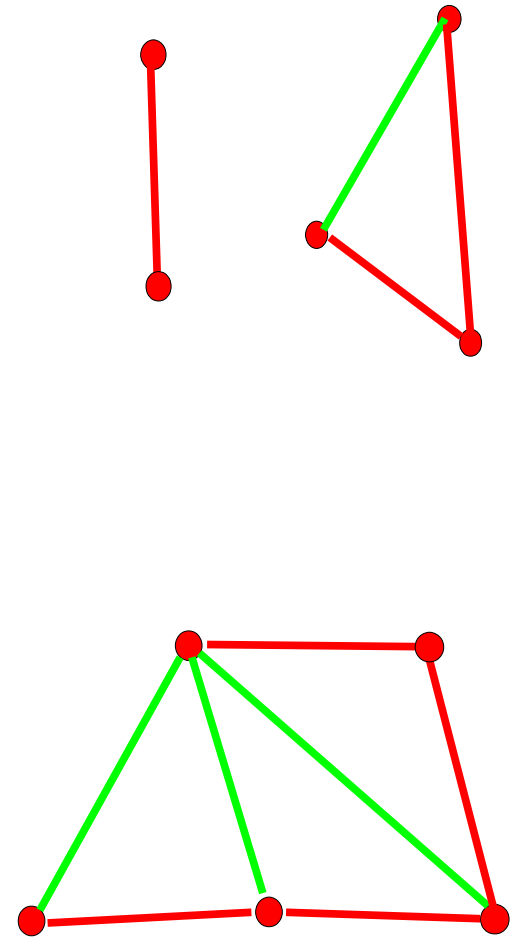
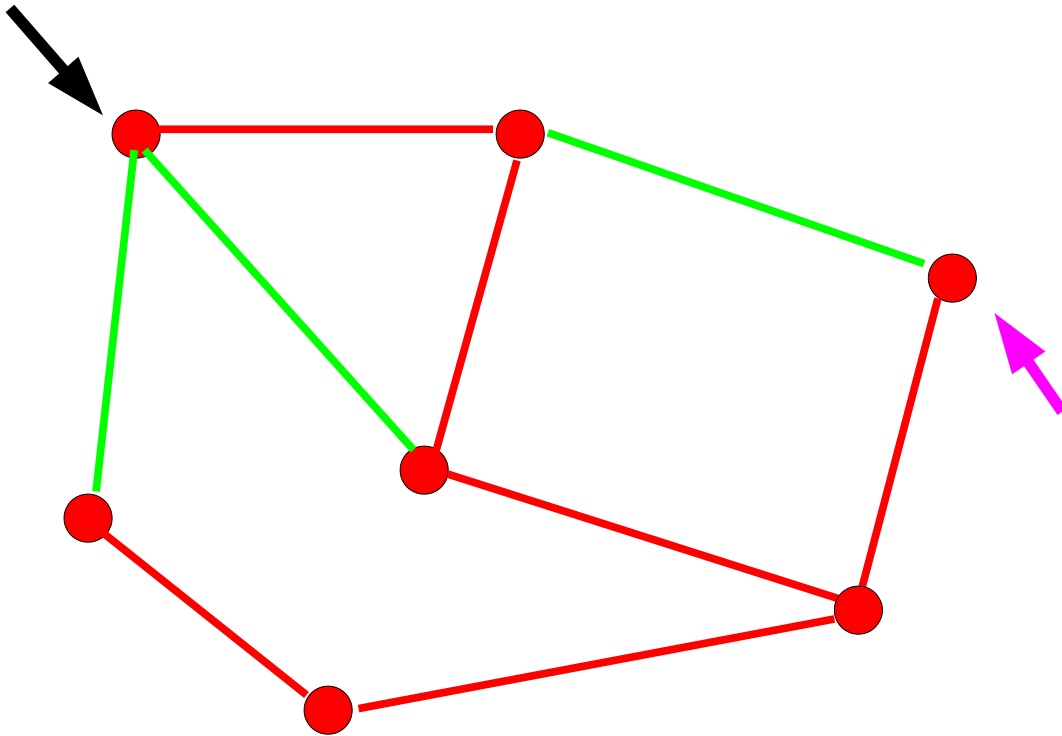
# Biconnected Components



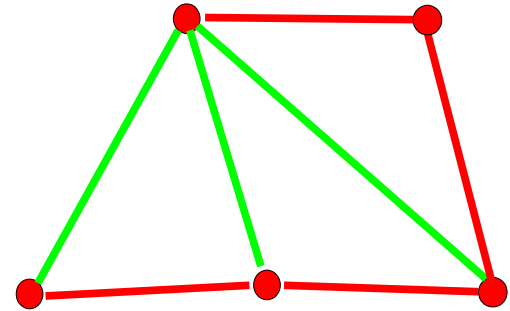
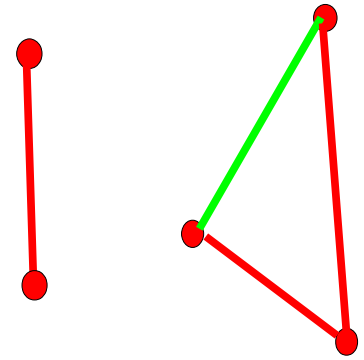
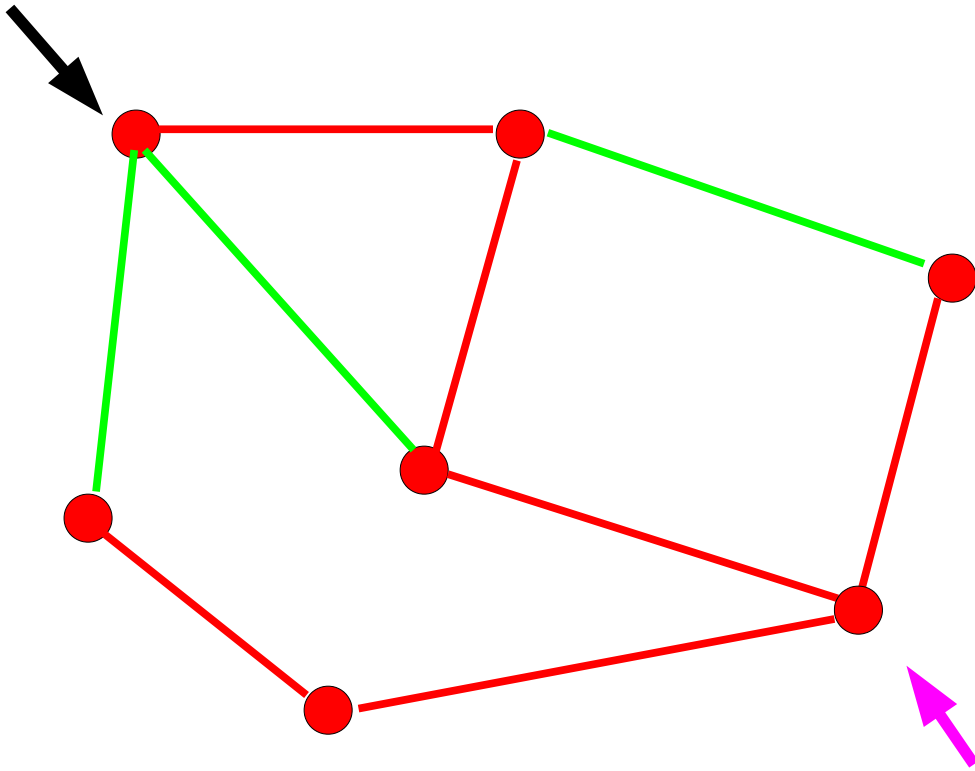
# Biconnected Components



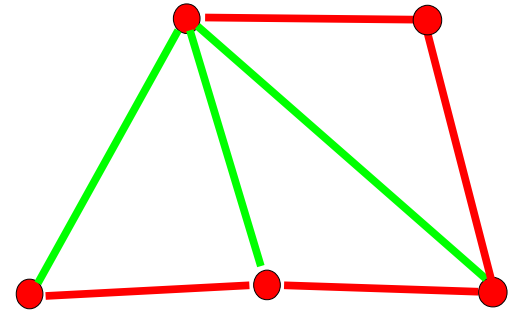
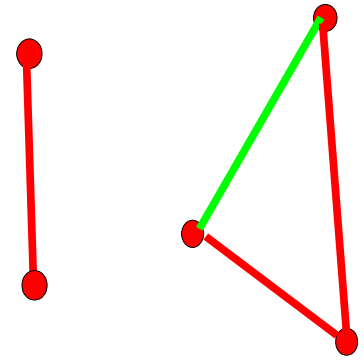
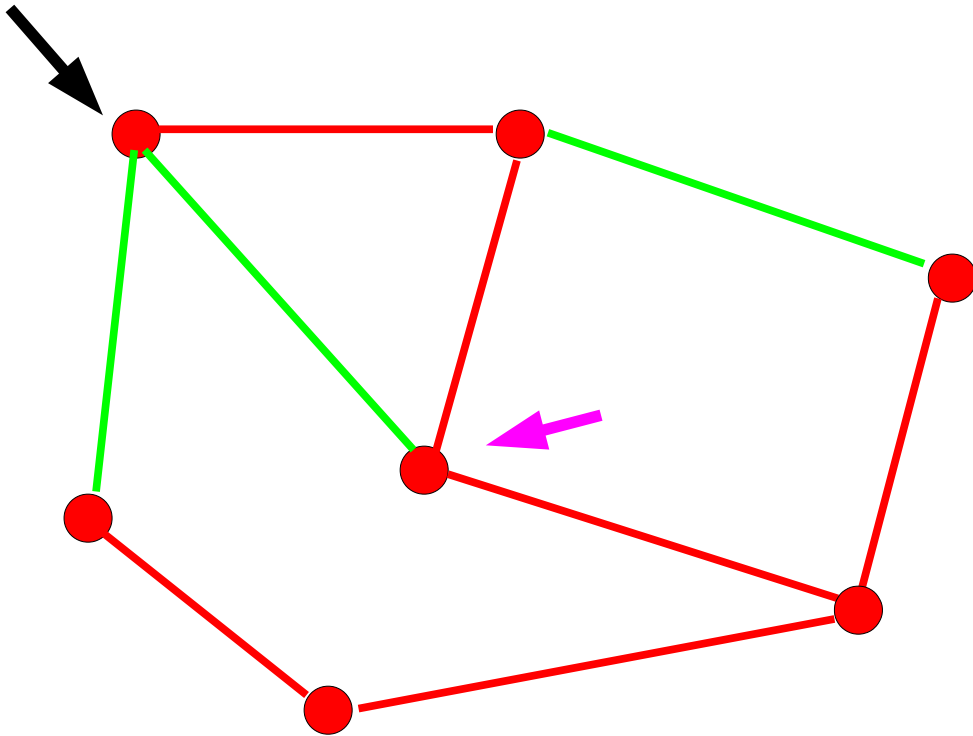
# Biconnected Components



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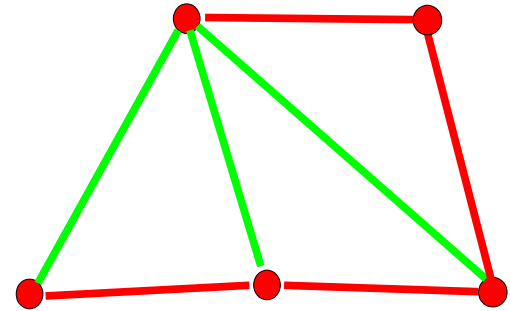
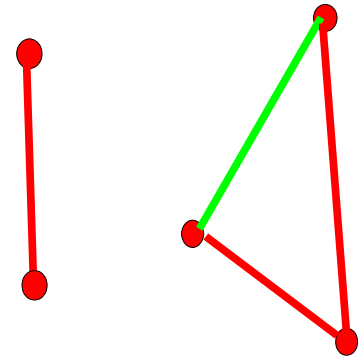
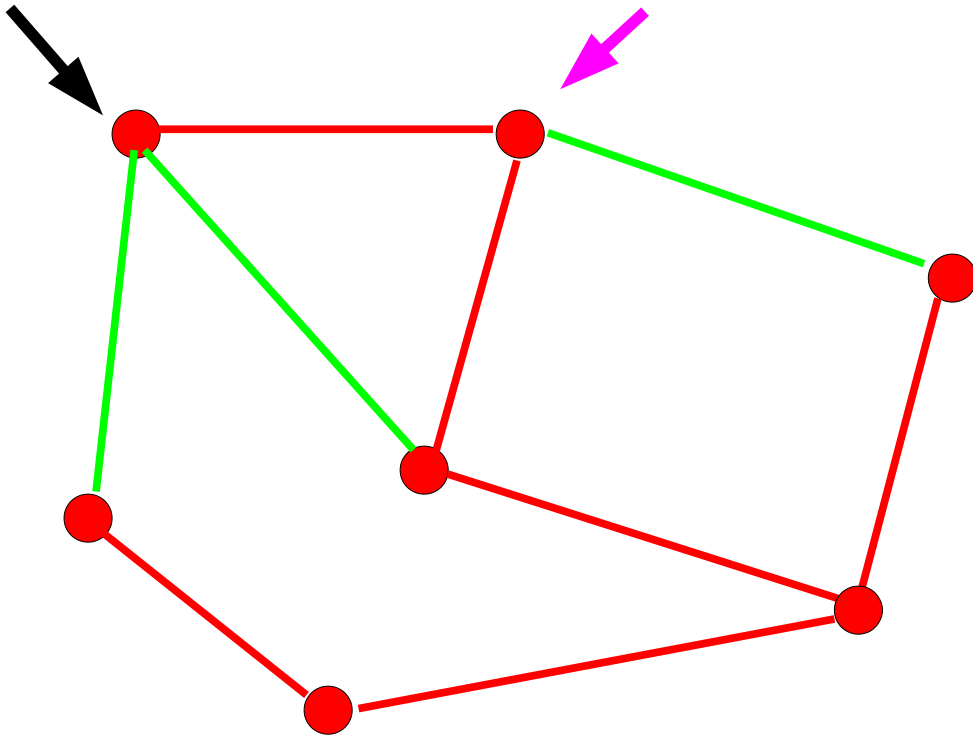


# Biconnected Components

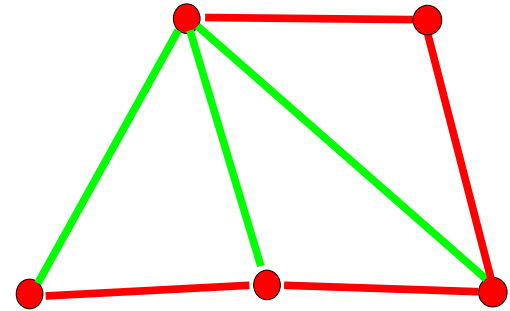
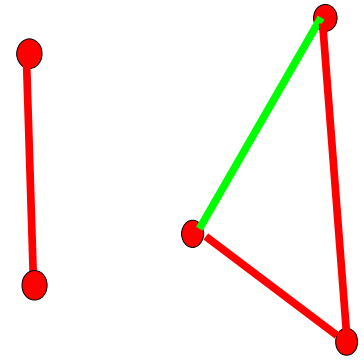
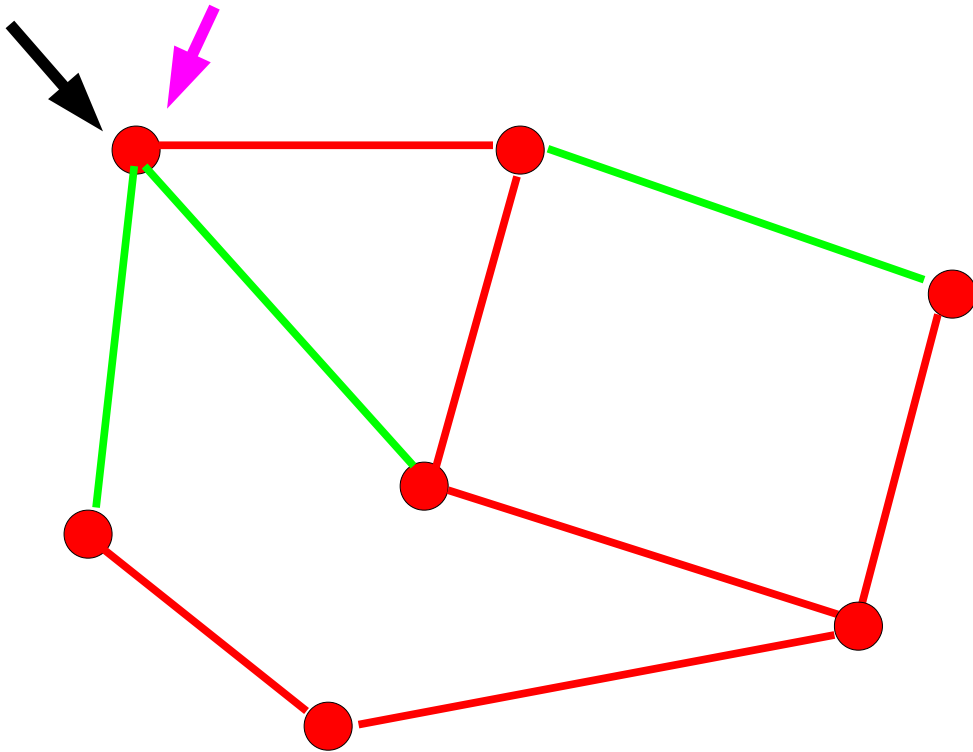




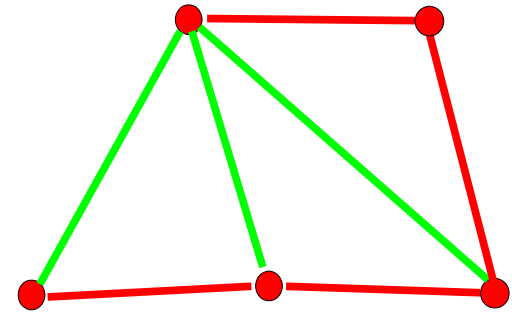
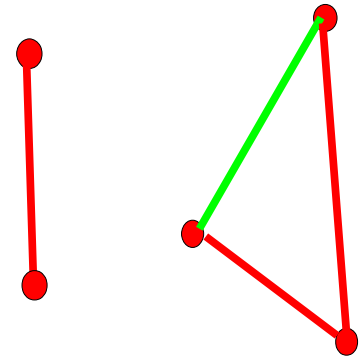
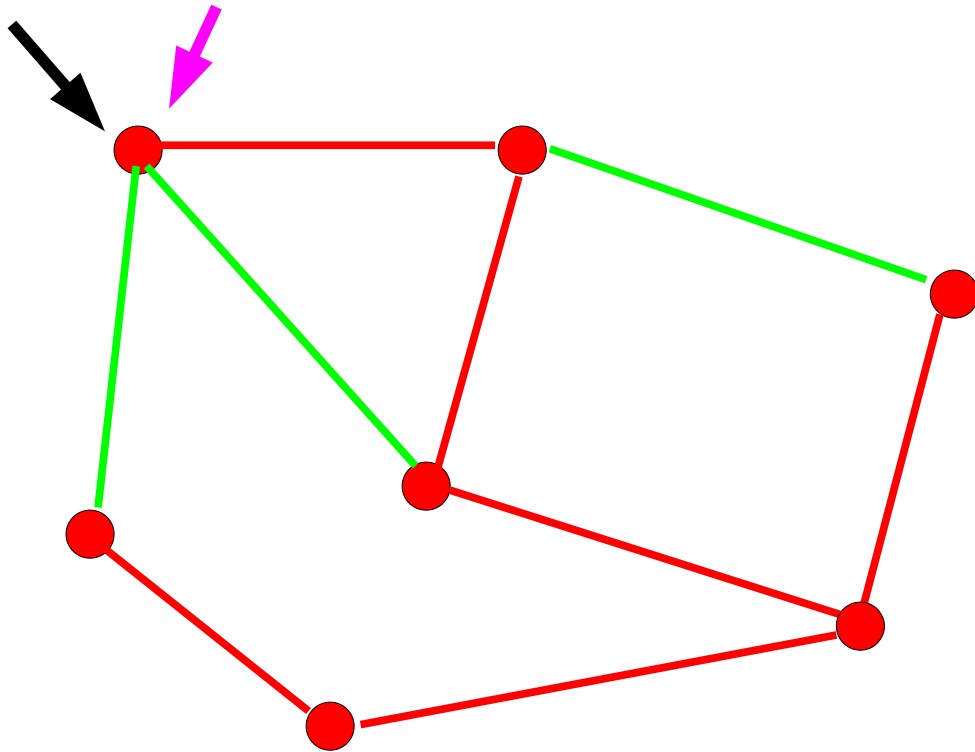
# Biconnected Components



# Biconnected Components

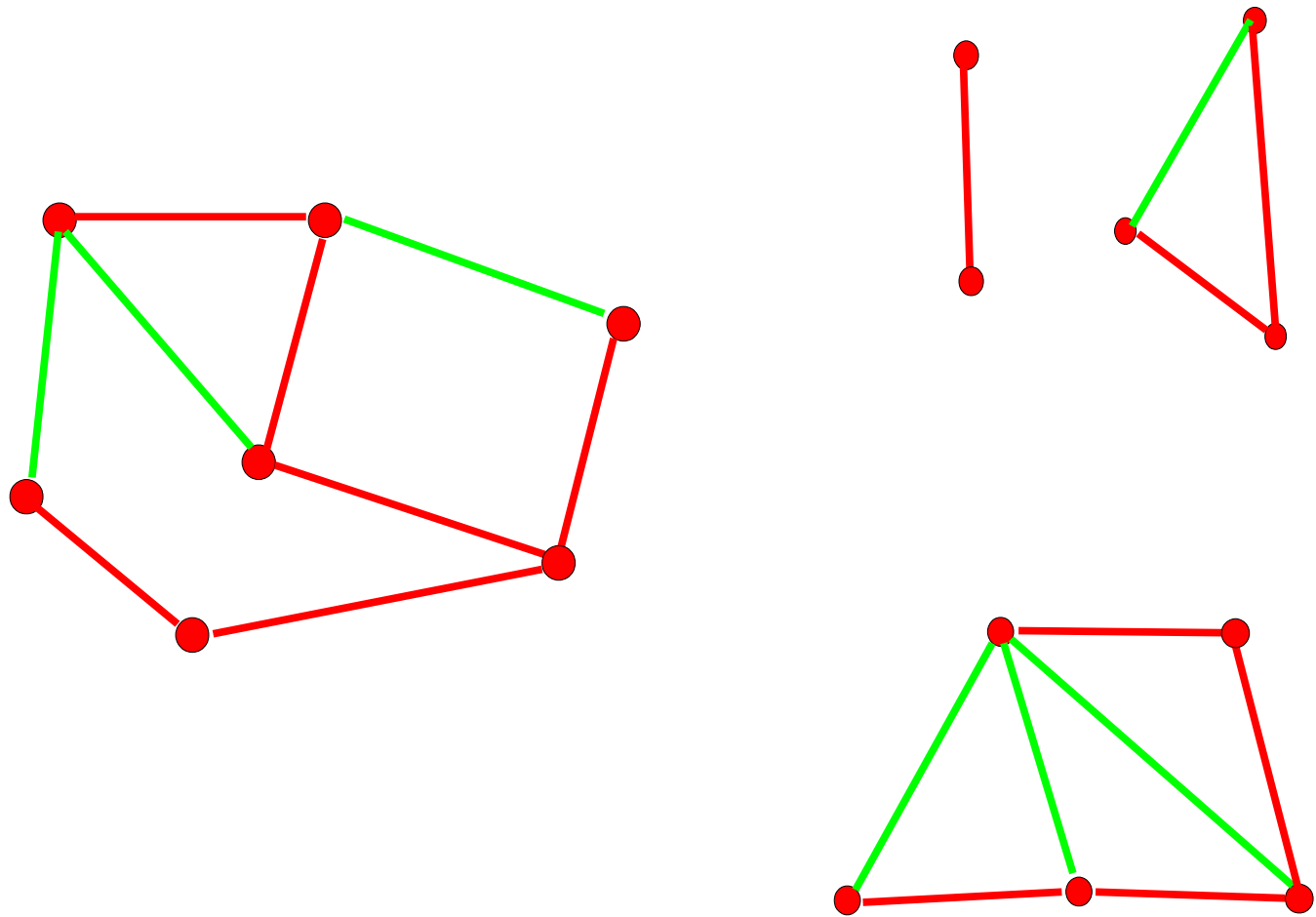


# Biconnected Components



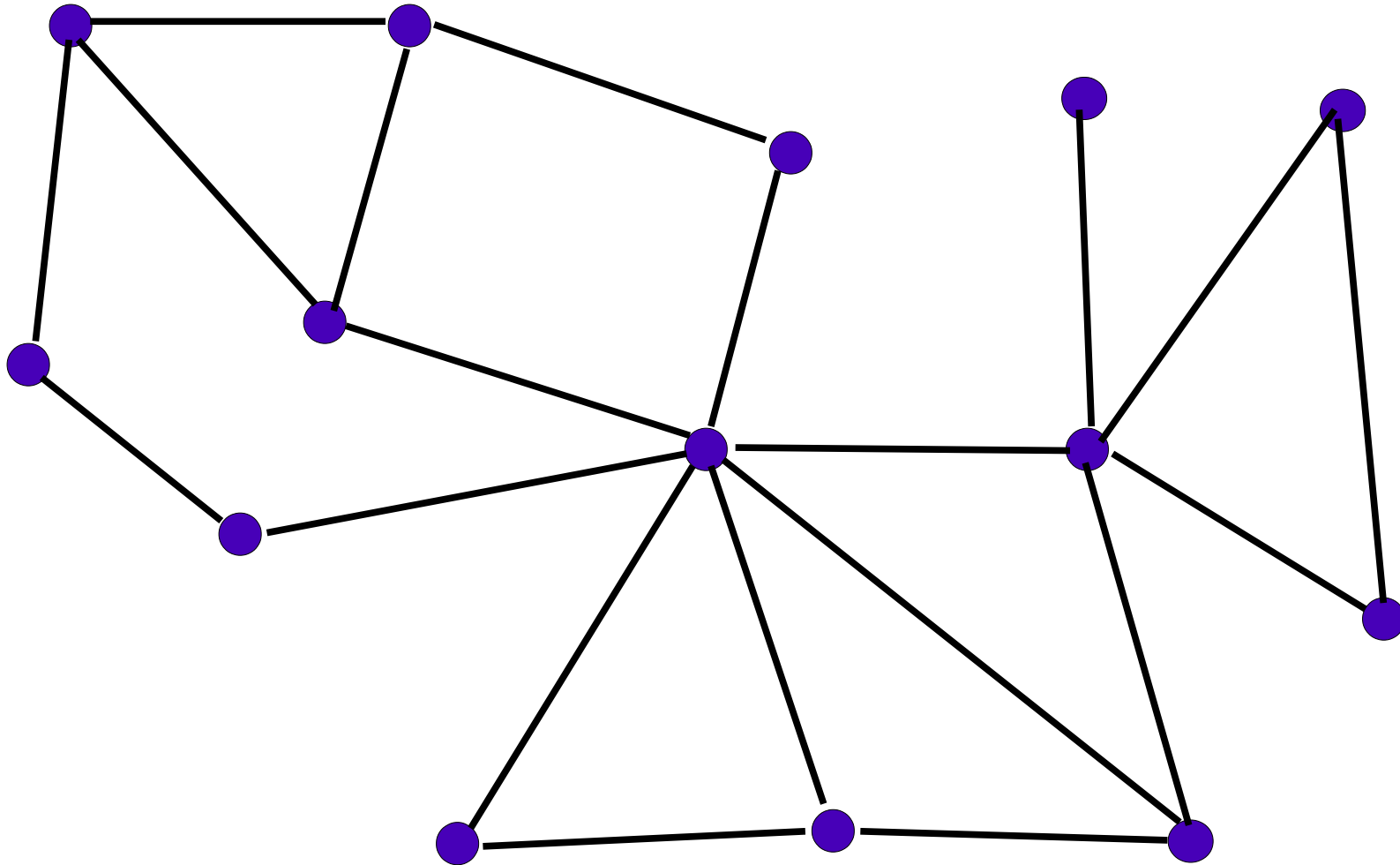
Must be a biconnected component since no more neighbors to explore at start point

# Biconnected Components



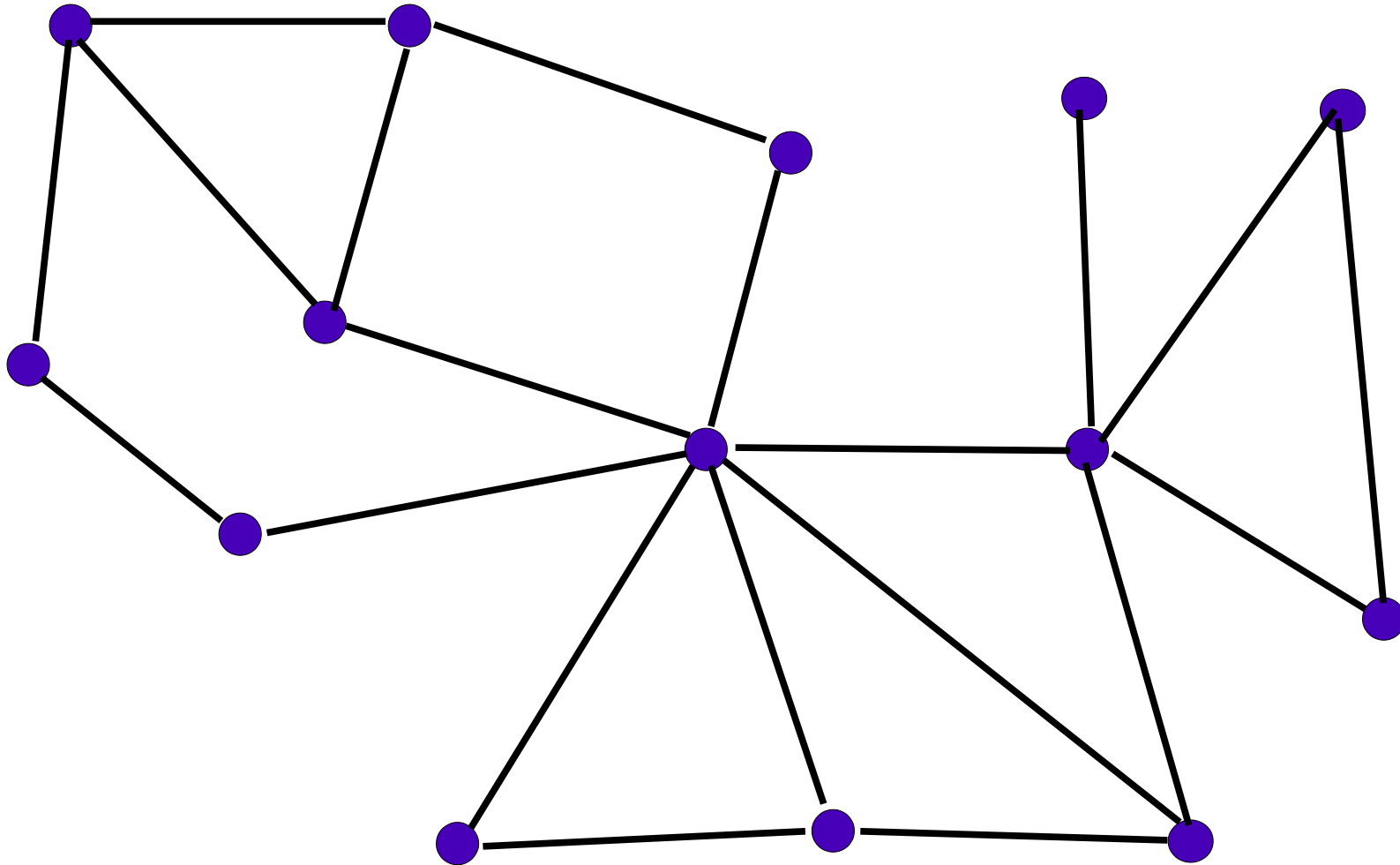
Save that biconnected component on the side, return all biconnected components, stop

# Biconnected Components



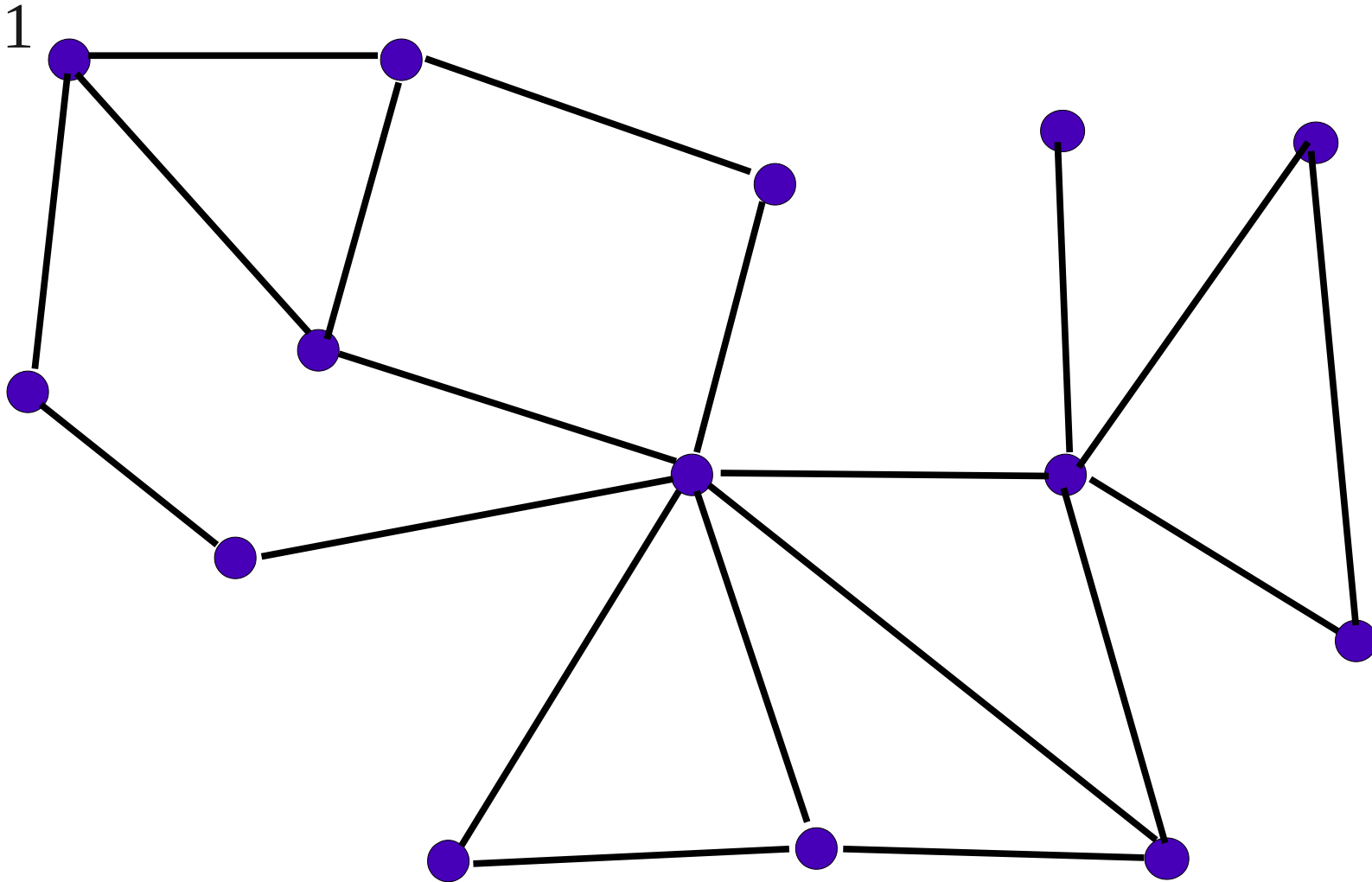
How to detect, during depth-first search, that all paths from neighbors explored so far lead back to the current vertex?

# Biconnected Components



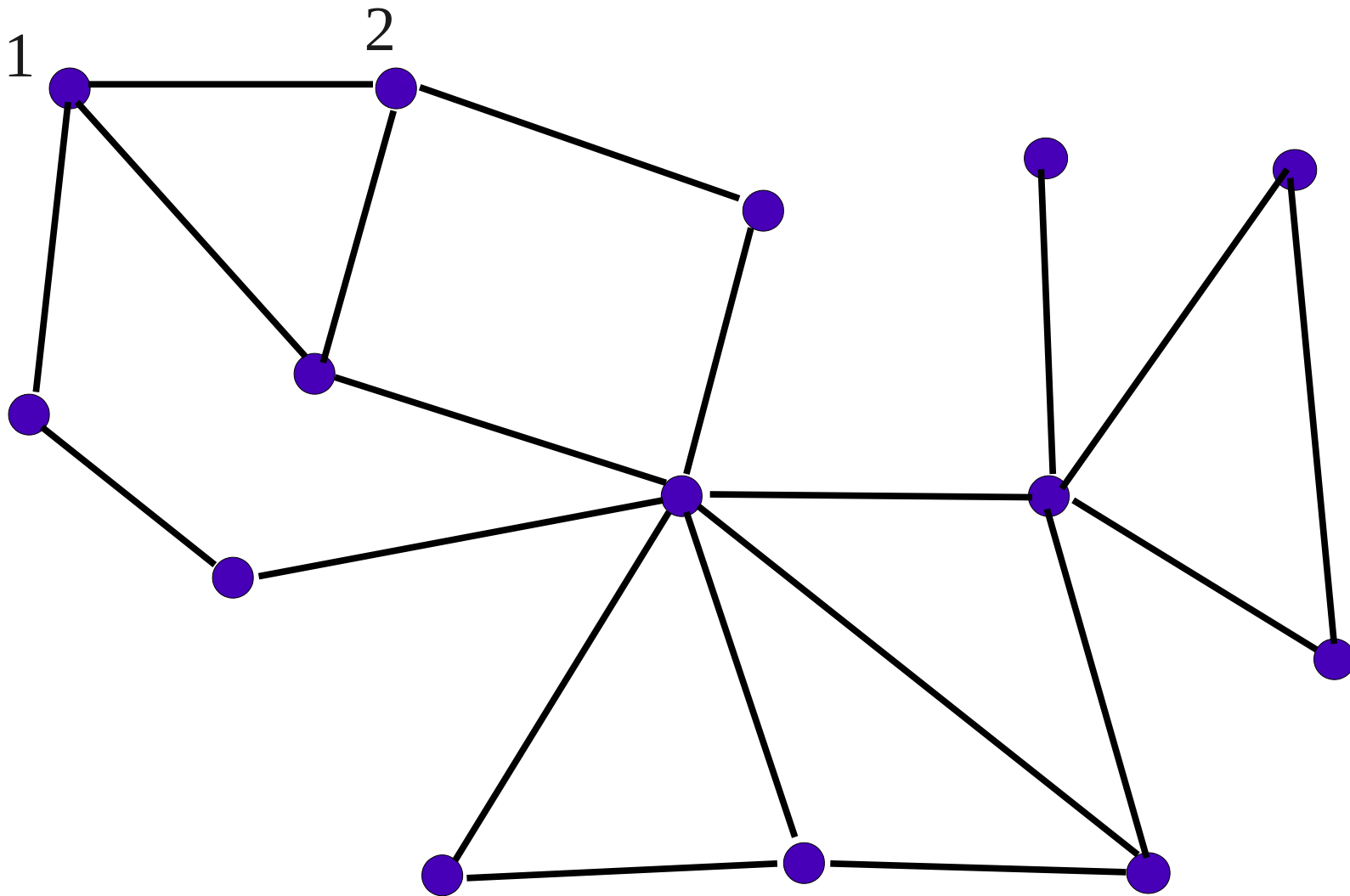
Maybe it has something to do with the order that vertices are considered – let's try putting numbers on the vertices

# Biconnected Components



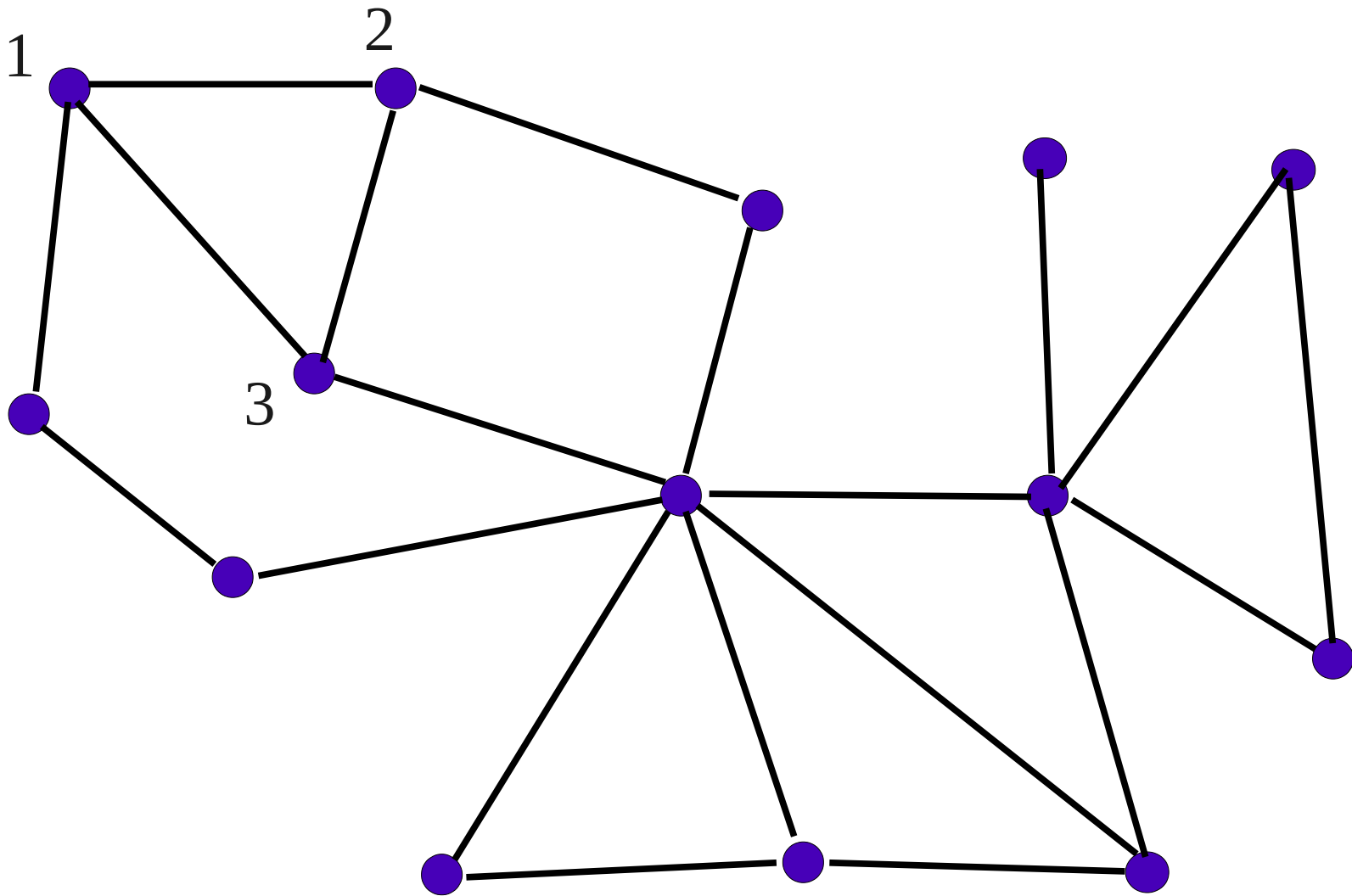
Maybe it has something to do with the order that vertices are considered – let's try putting numbers on the vertices

# Biconnected Components

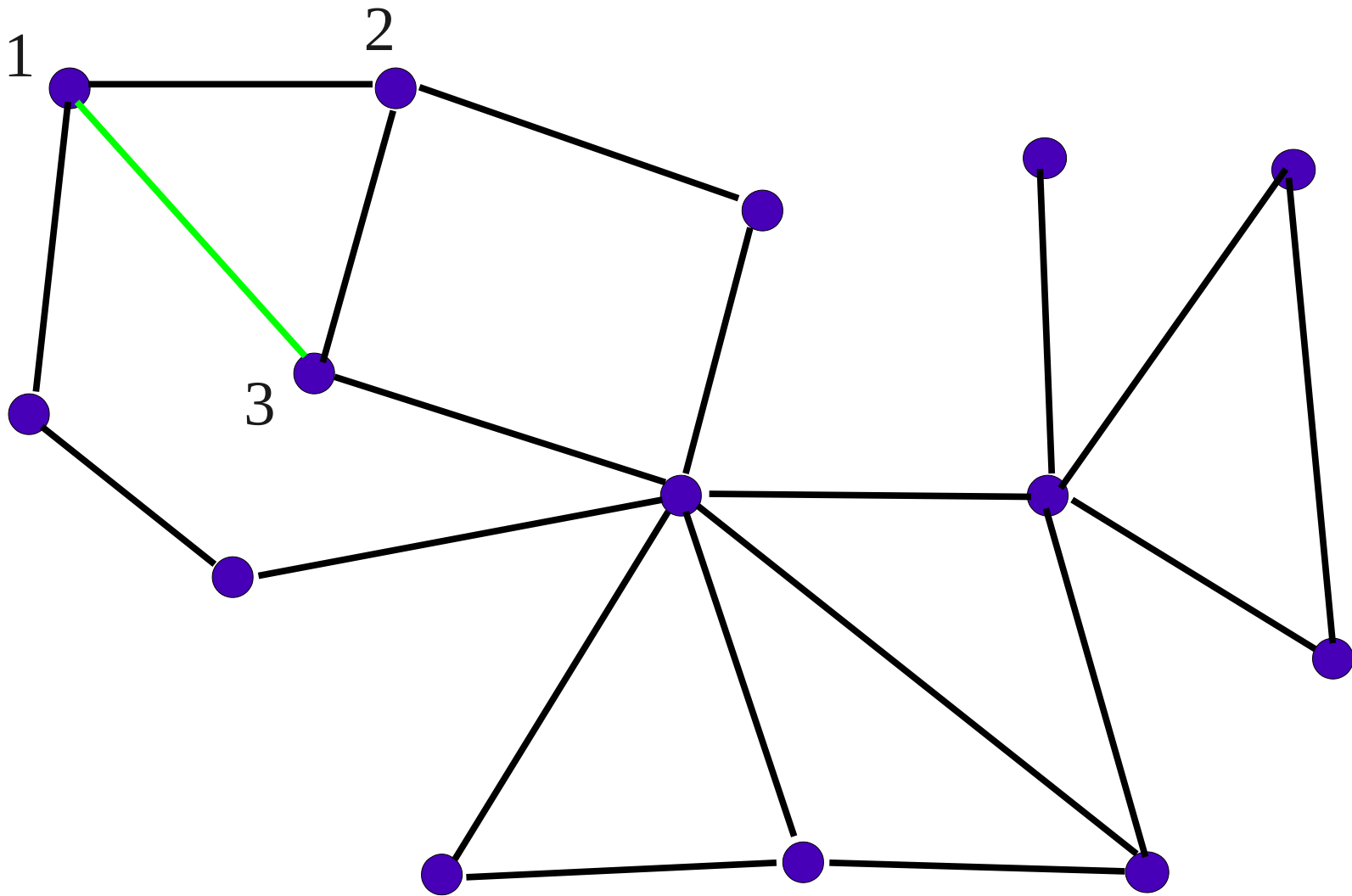




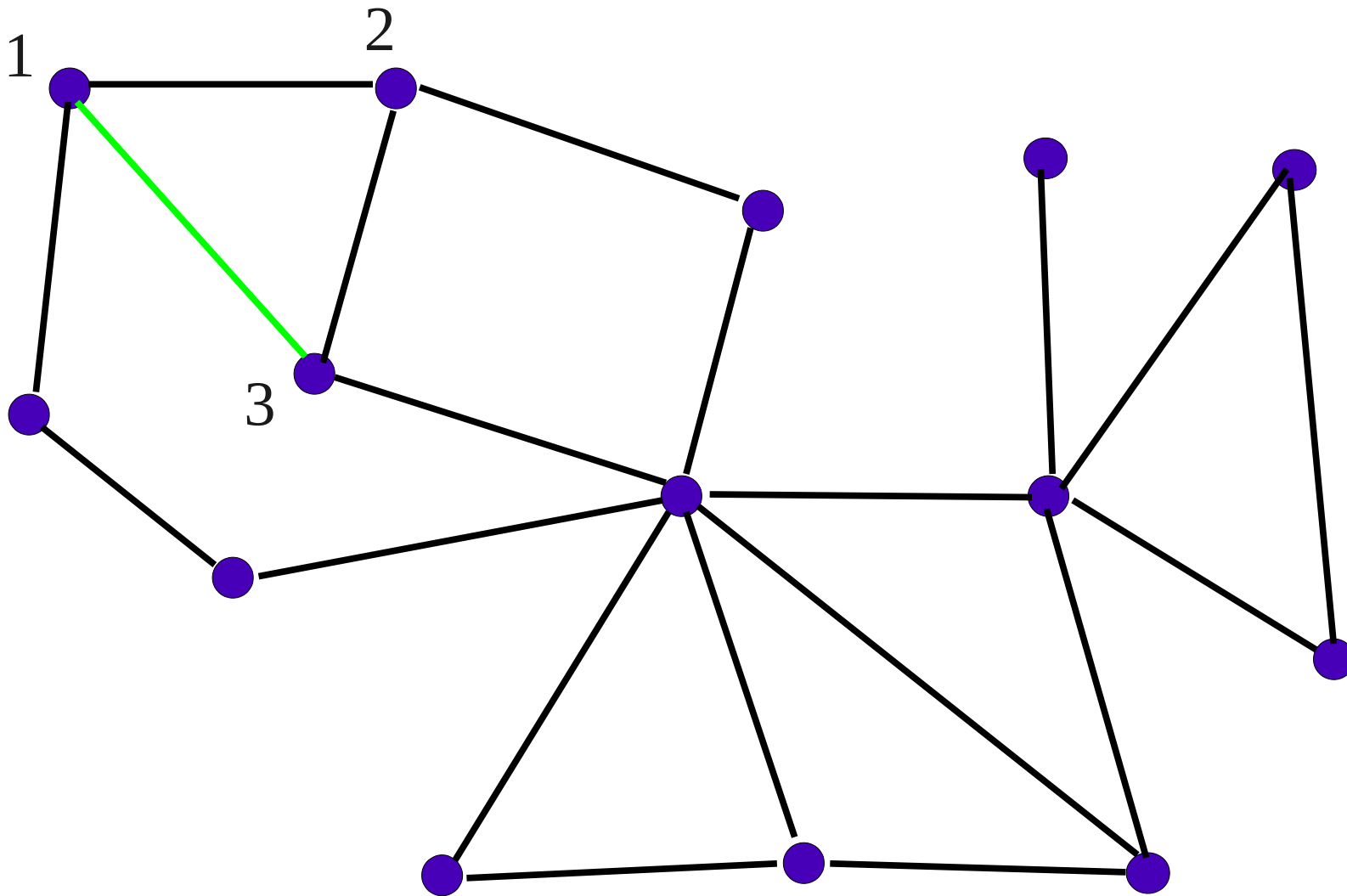
# Biconnected Components



# Biconnected Components

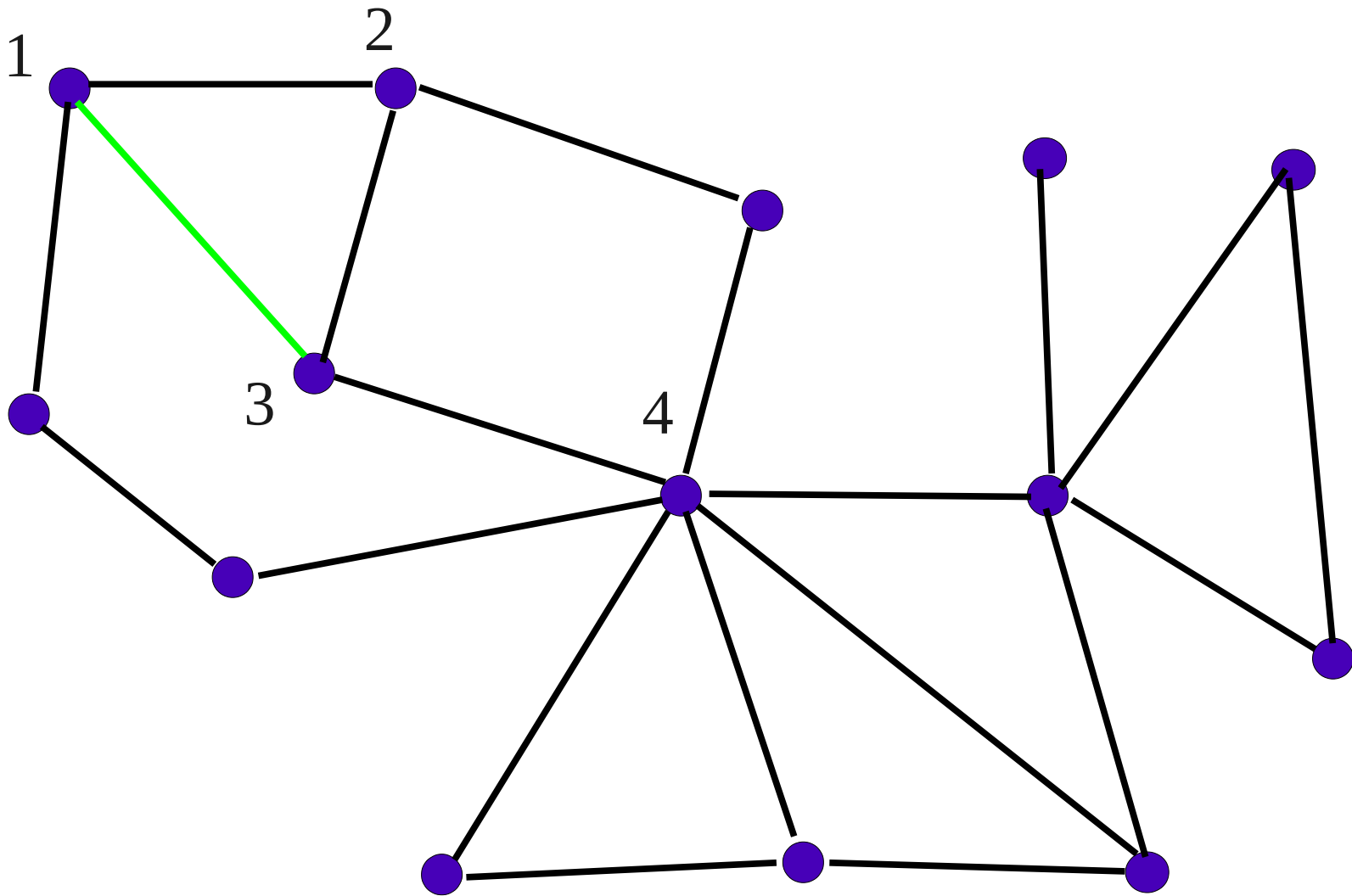


# Biconnected Components

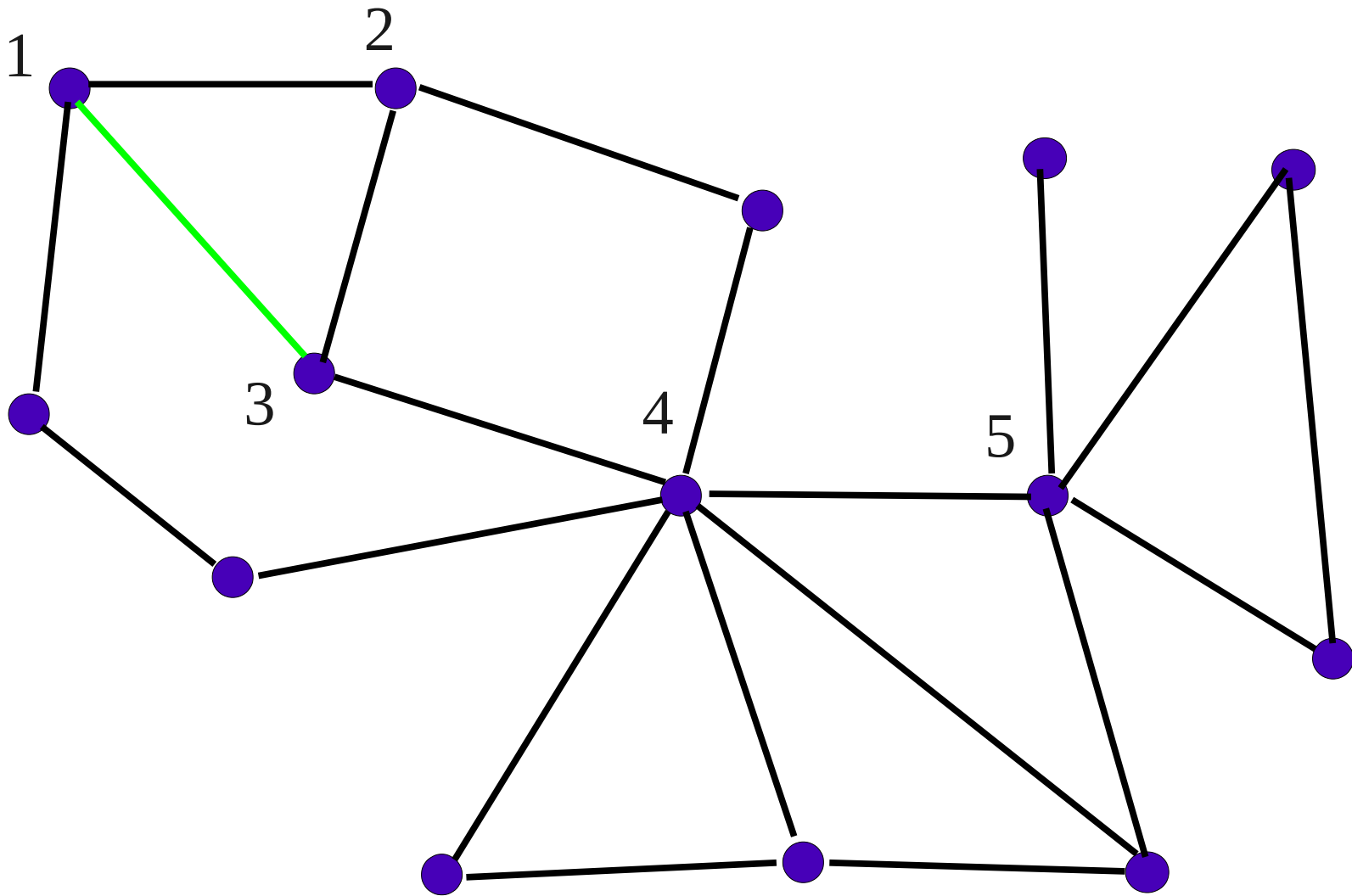


We arrive back at vertex 3 having seen vertex 1. So edges we have seen are not a biconnected component.

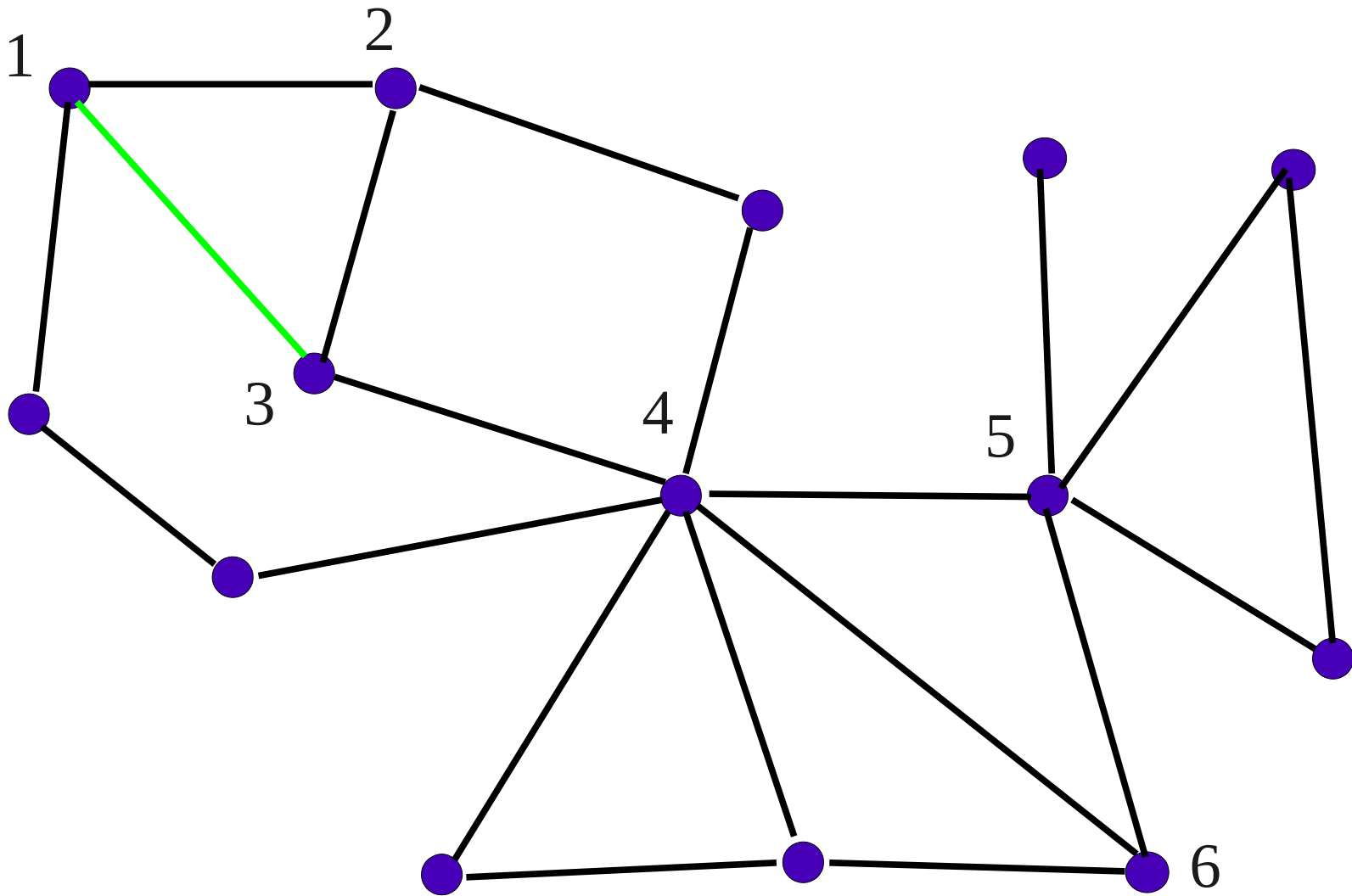
# Biconnected Components



# Biconnected Components

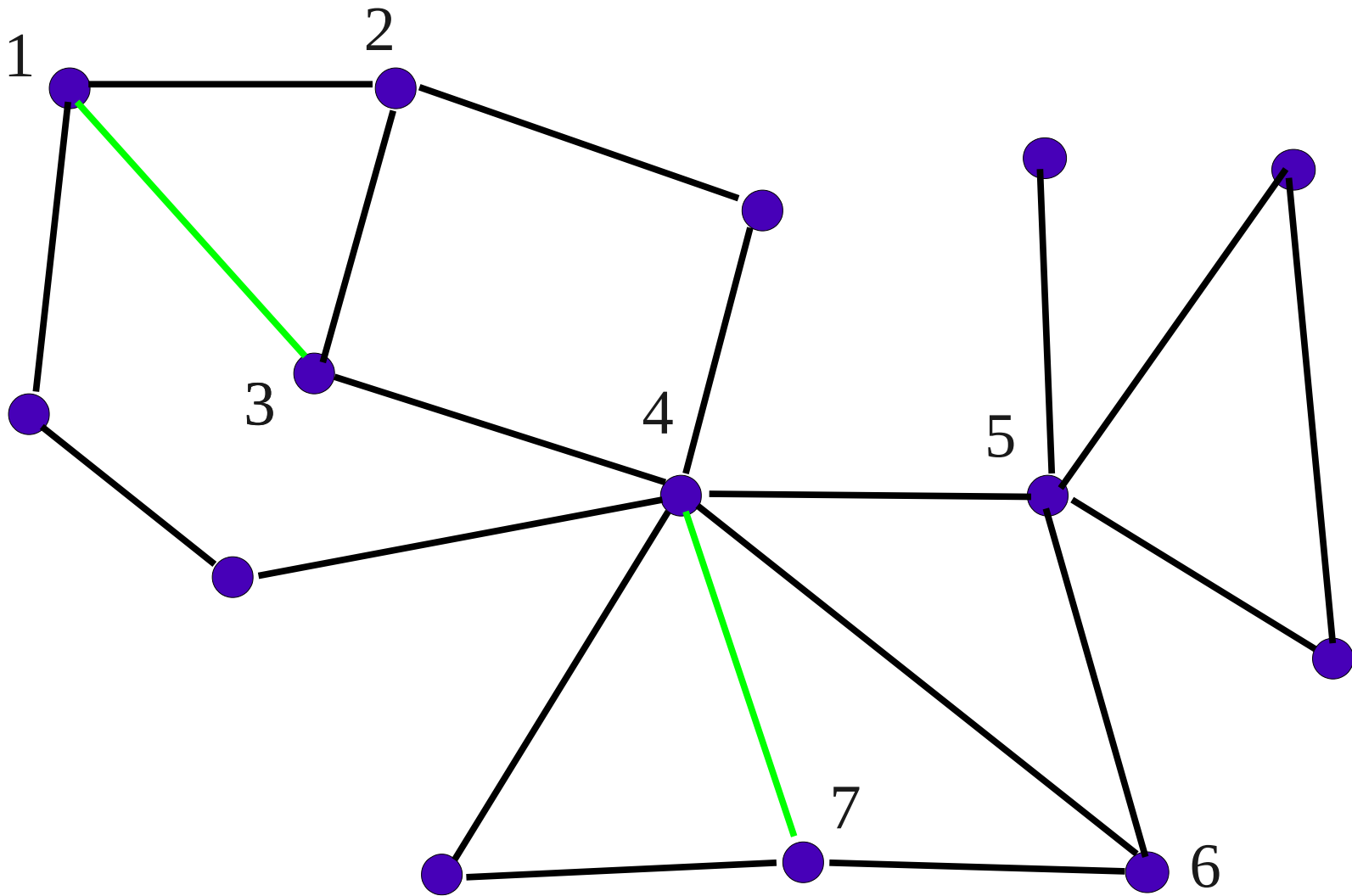


# Biconnected Components



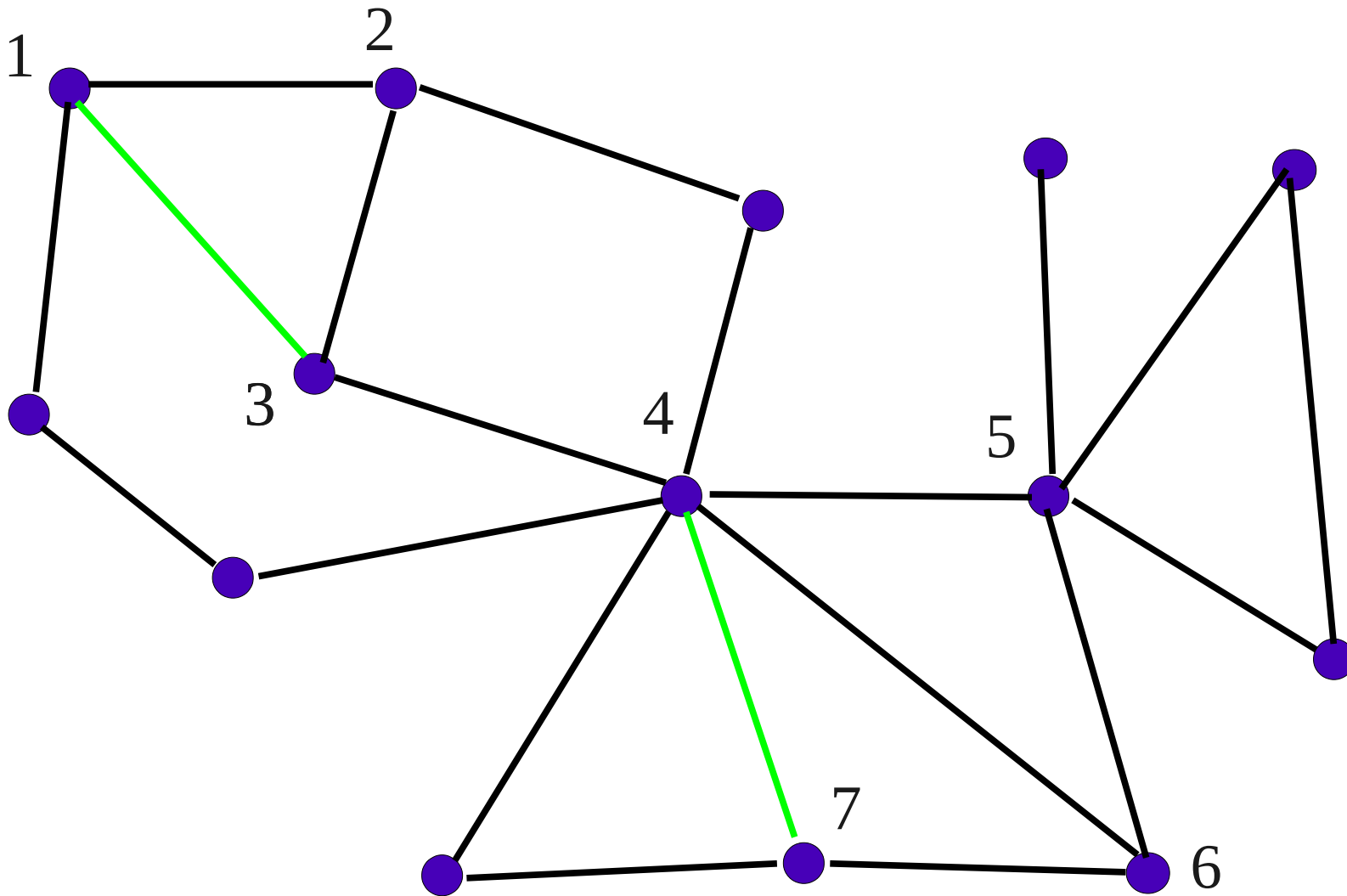


# Biconnected Components



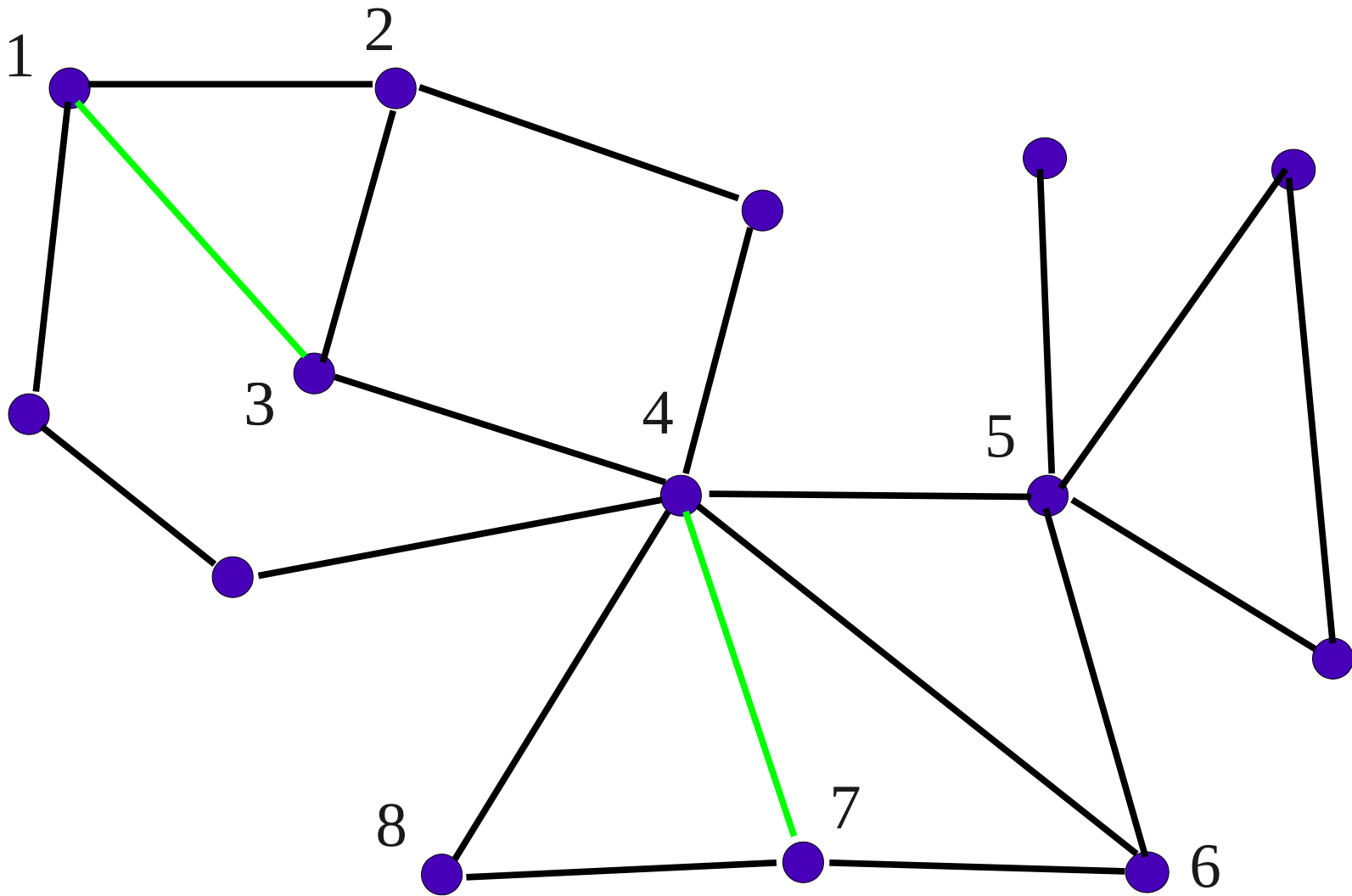


# Biconnected Components

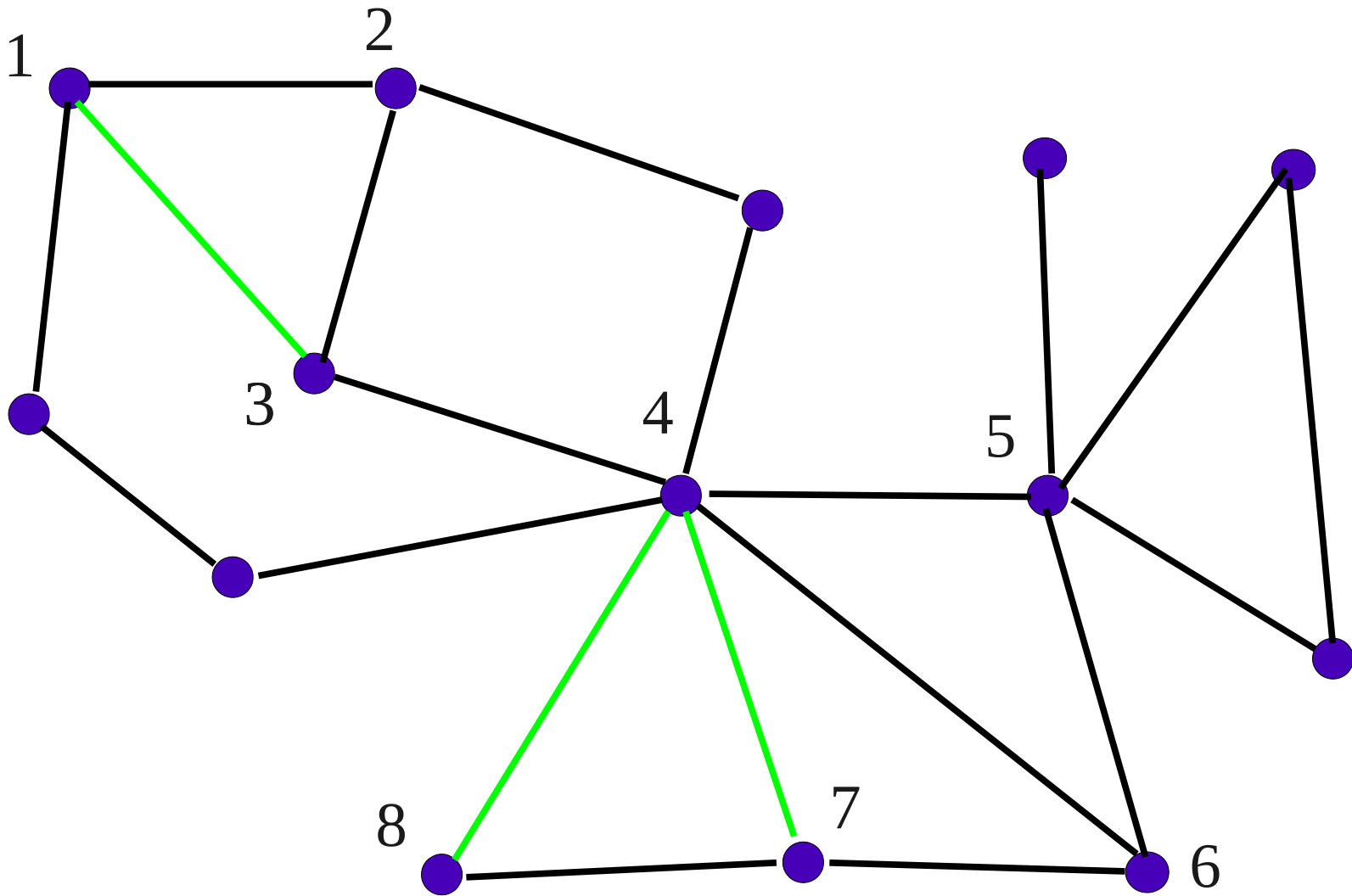


We arrive back at vertex 7 having seen vertex 4. So edges we have seen are not a biconnected component.

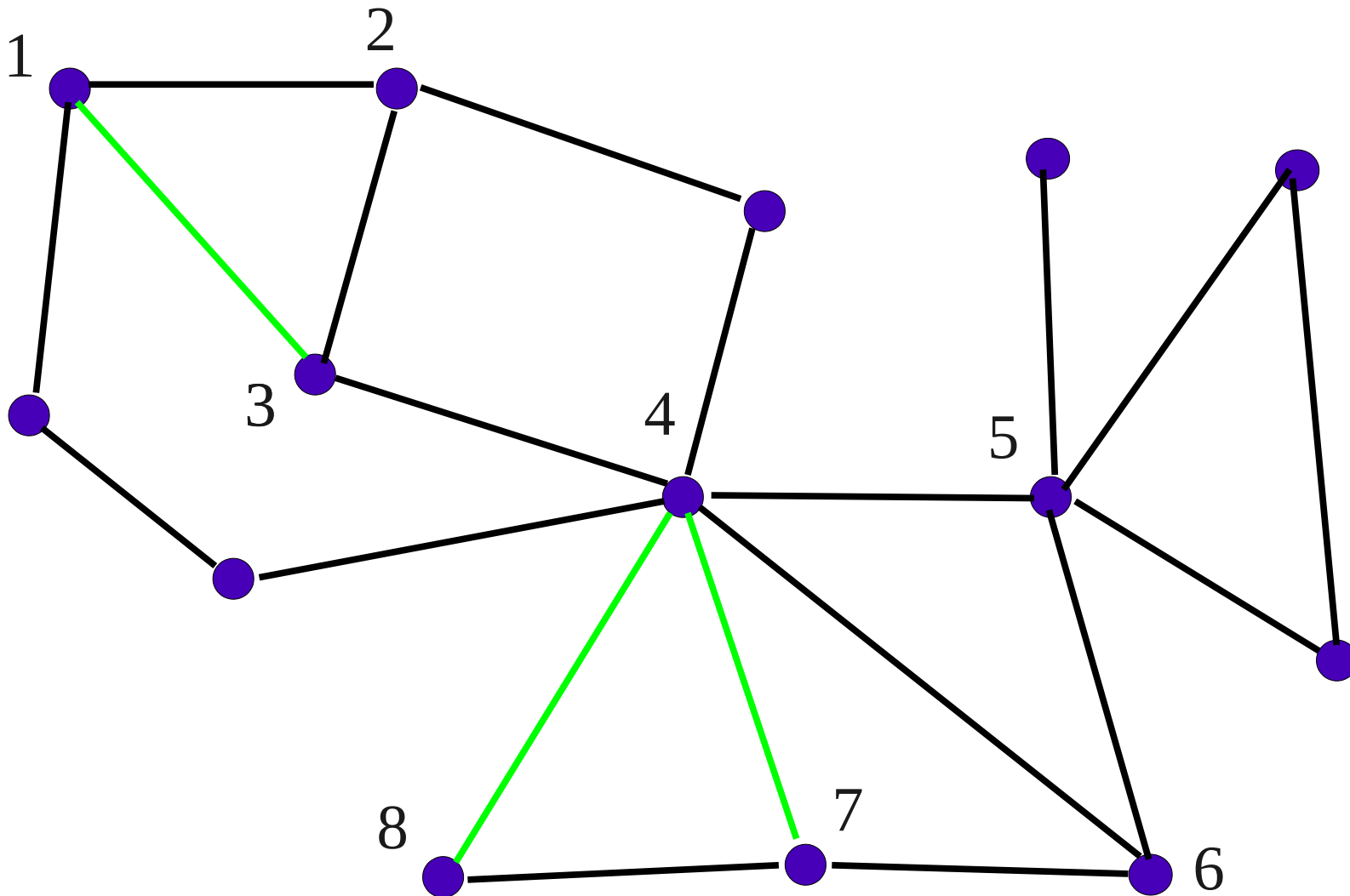
# Biconnected Components



# Biconnected Components

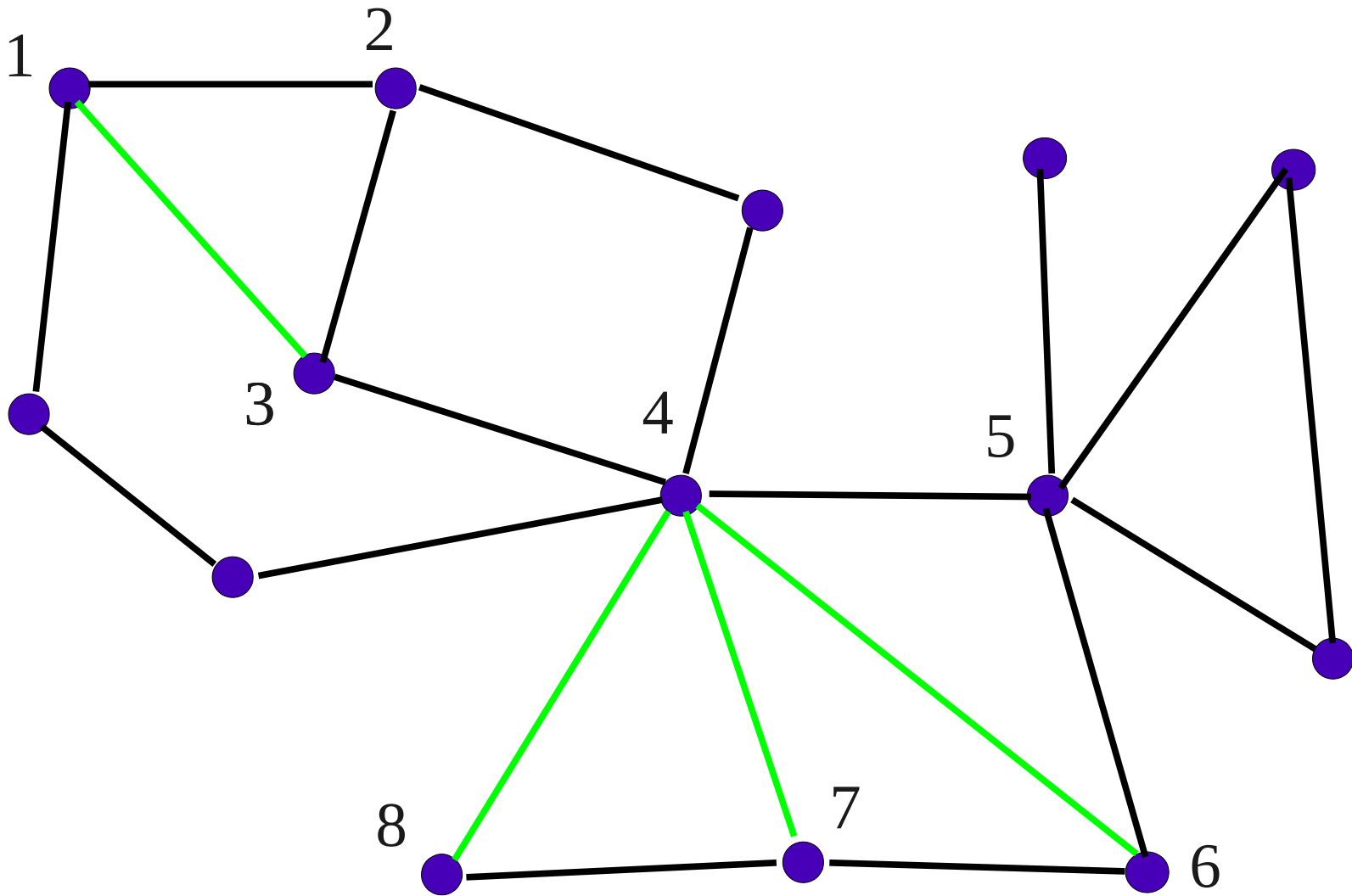


# Biconnected Components

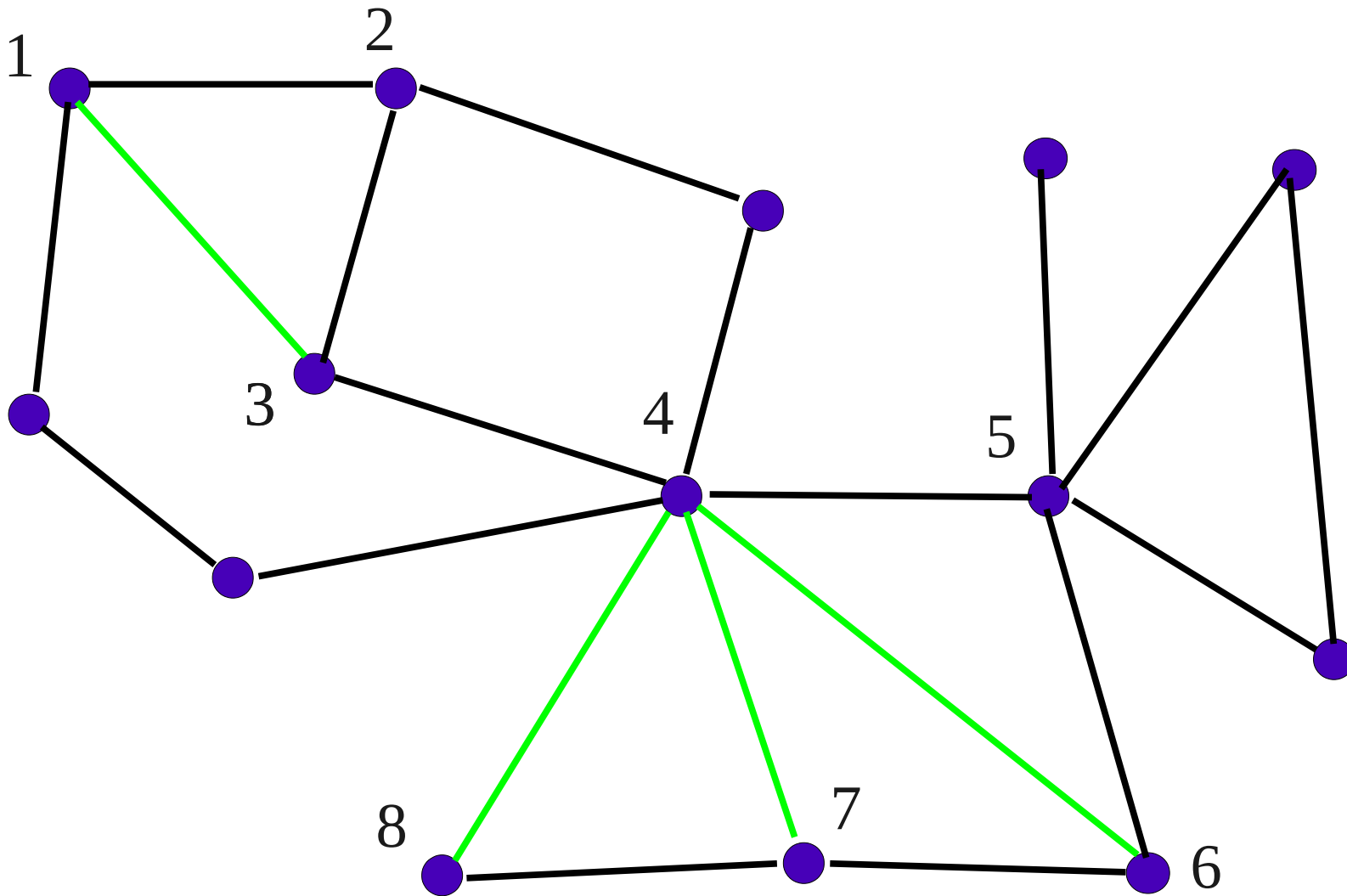


We return to vertex 8 having seen vertex 4. So this cannot be a biconnected component

# Biconnected Components

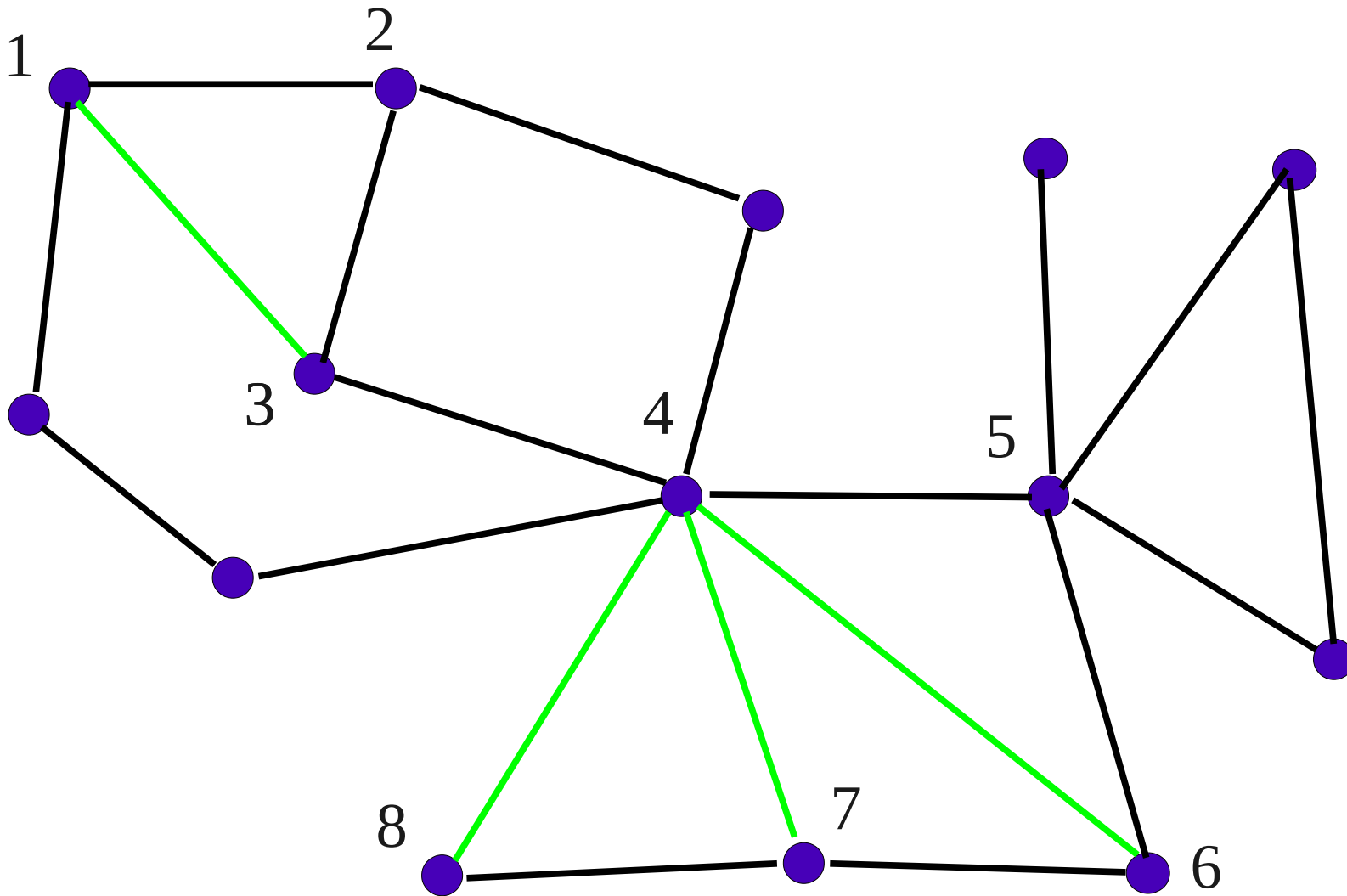


# Biconnected Components



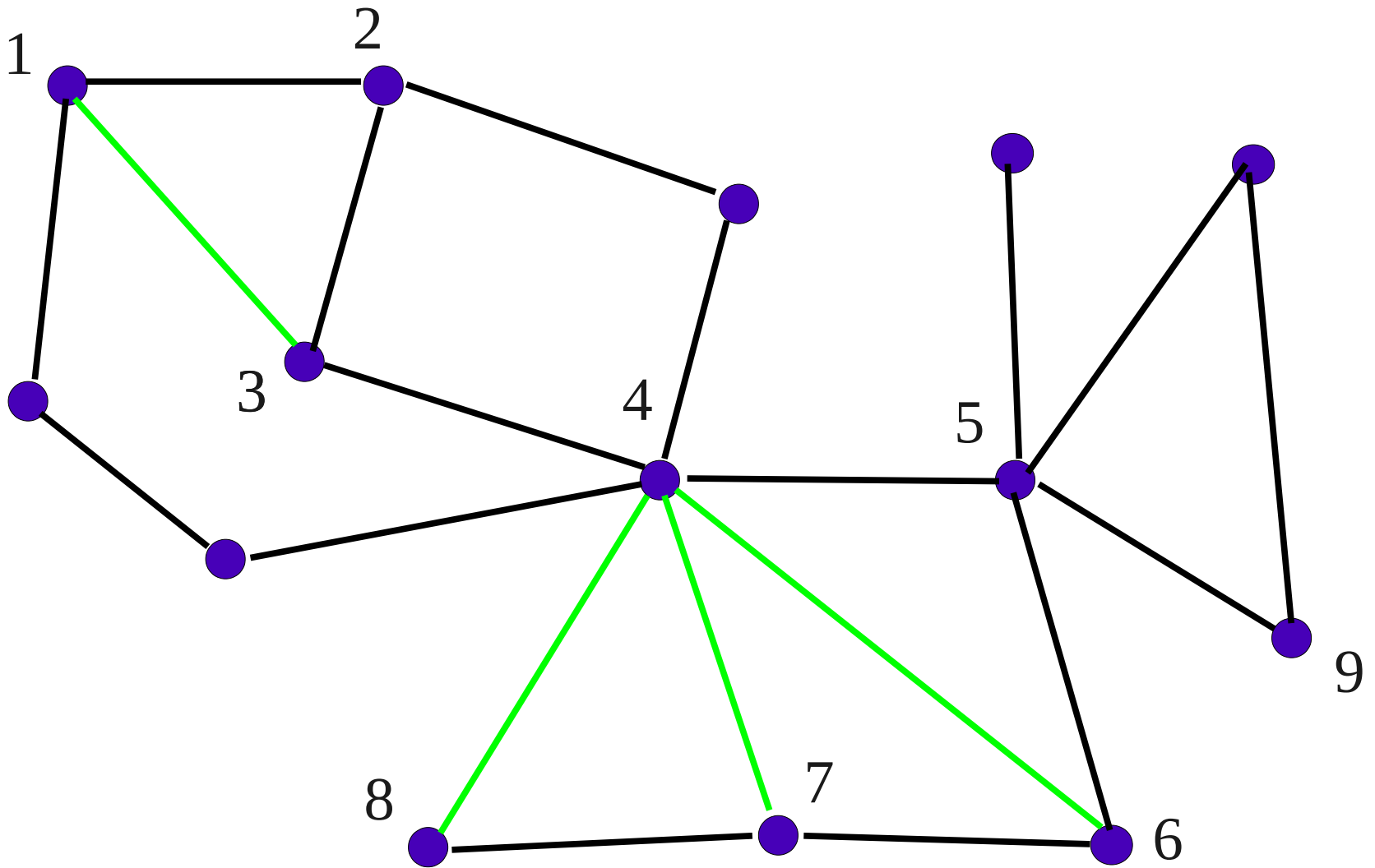
We arrive back at vertex 6 having seen vertex 4. So edges we have seen are not a biconnected component.

# Biconnected Components



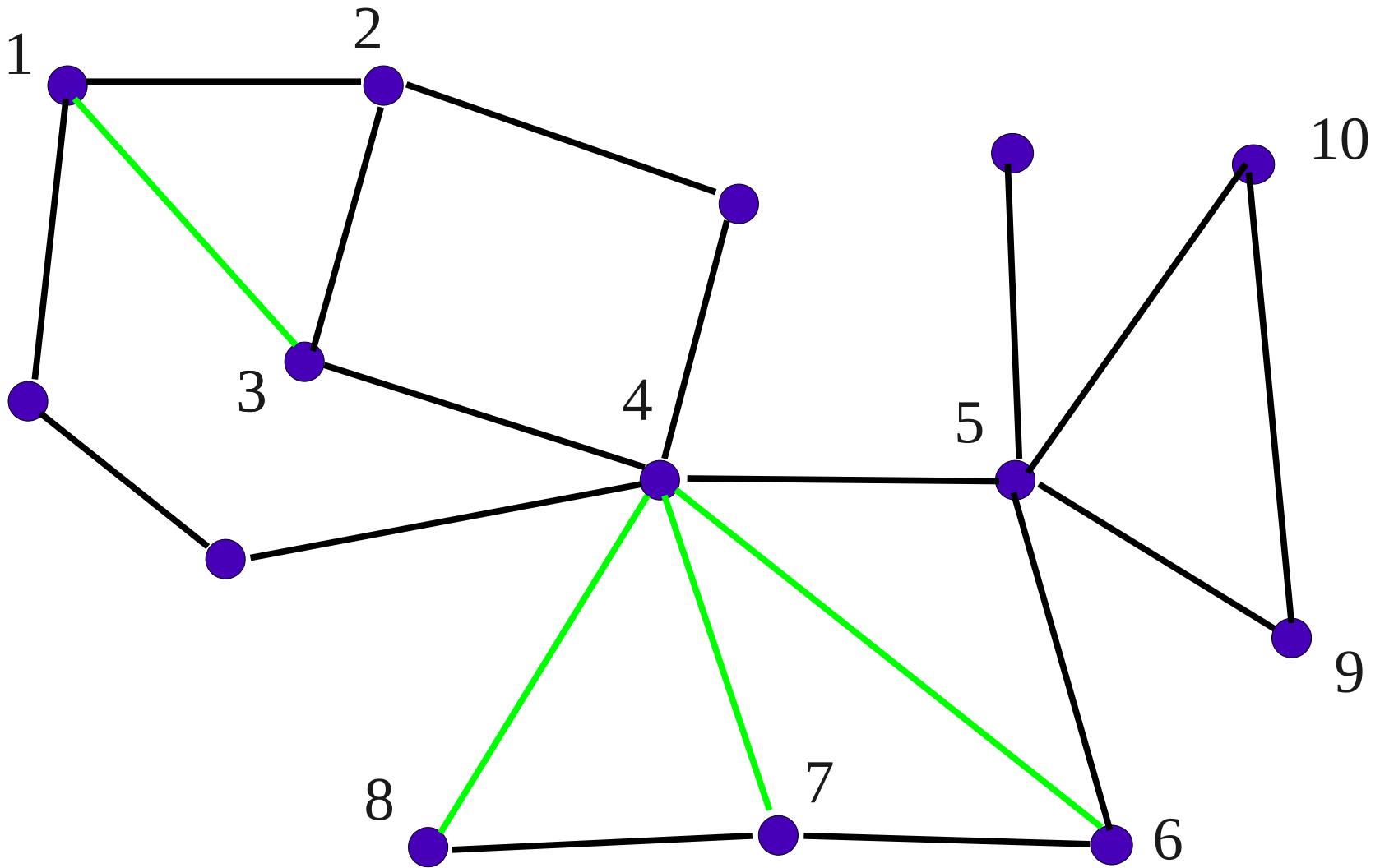
We arrive back at vertex 5 having seen vertex 4. So edges we have seen are not a biconnected component.

# Biconnected Components

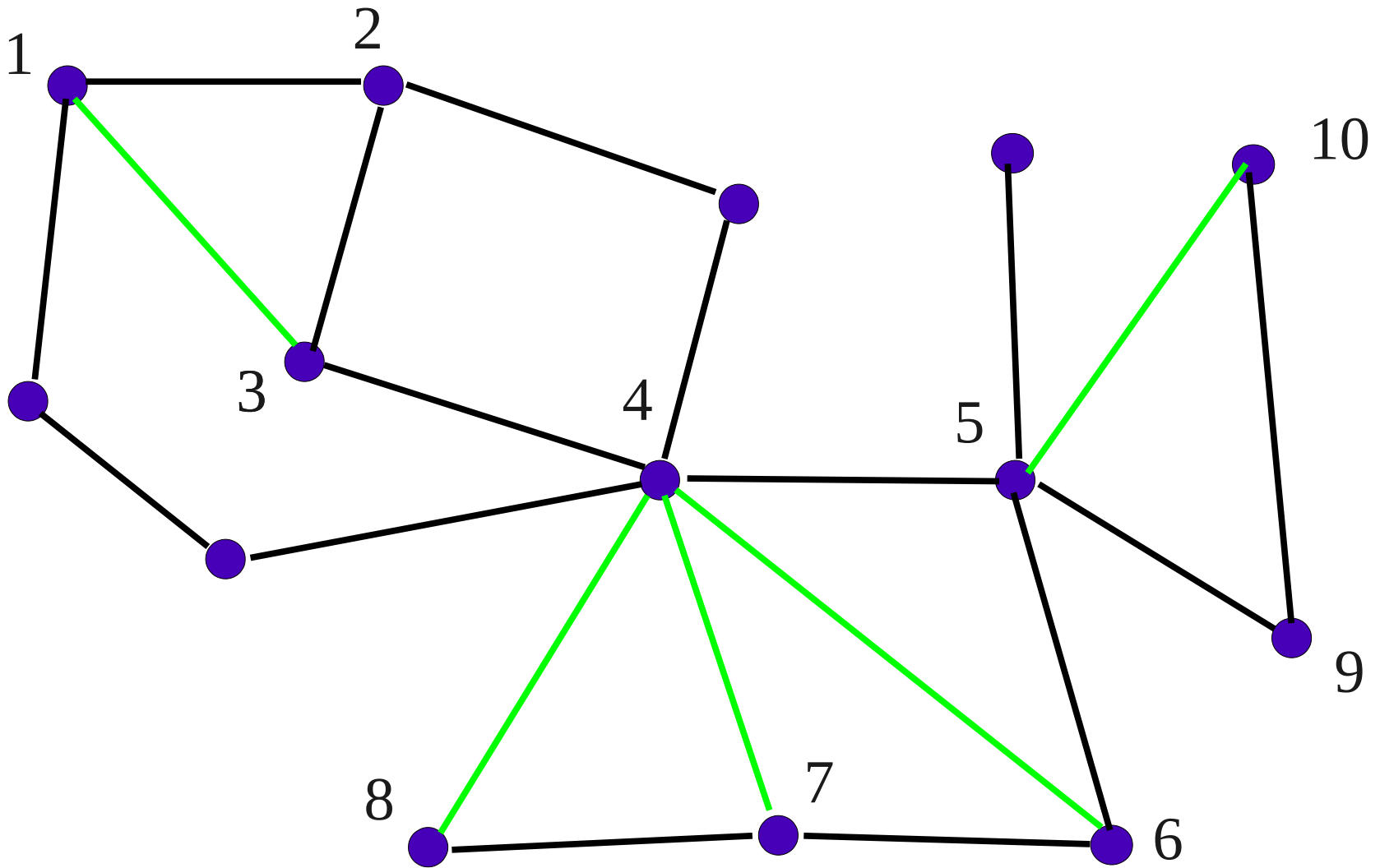




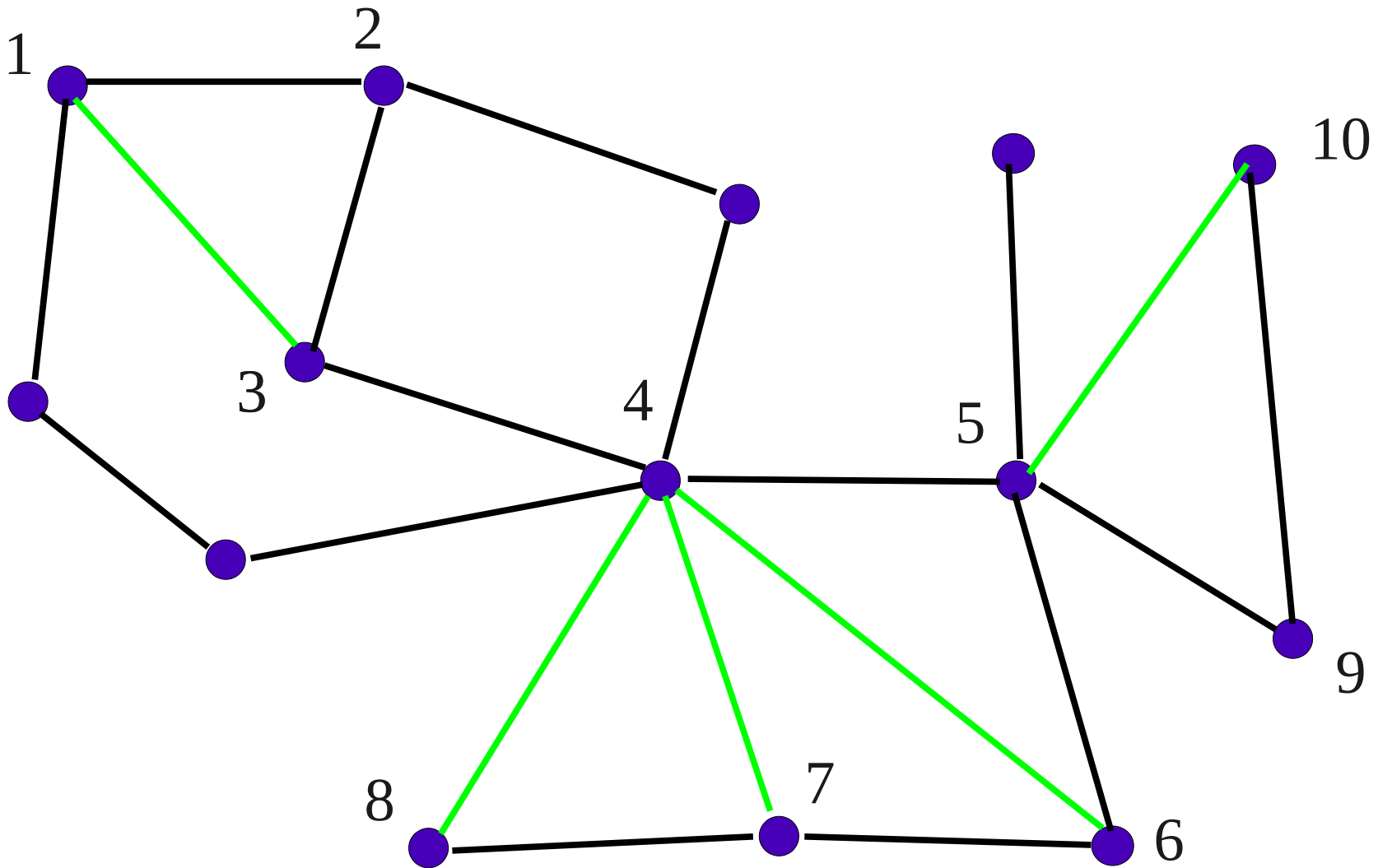
# Biconnected Components



# Biconnected Components



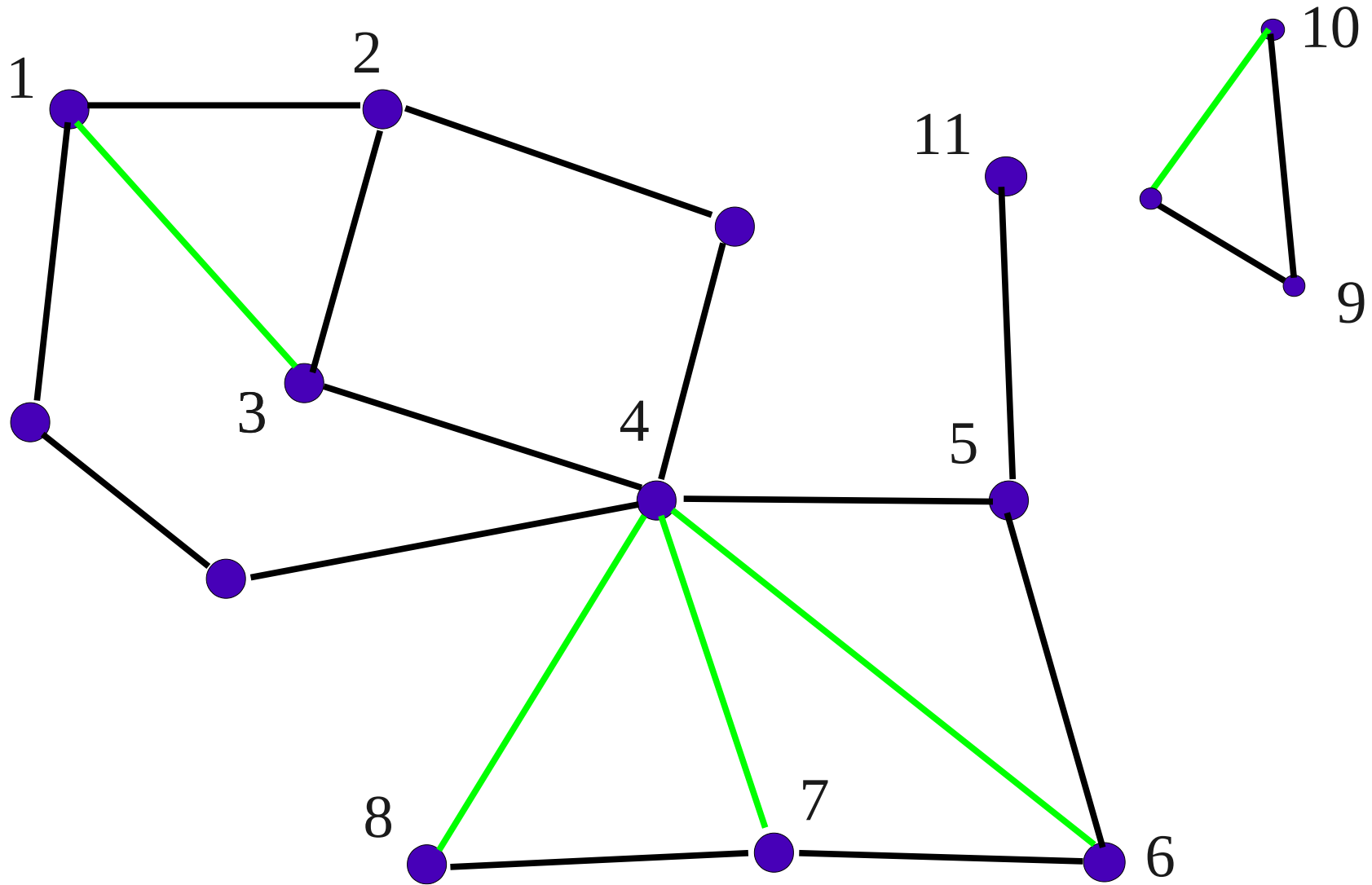
# Biconnected Components



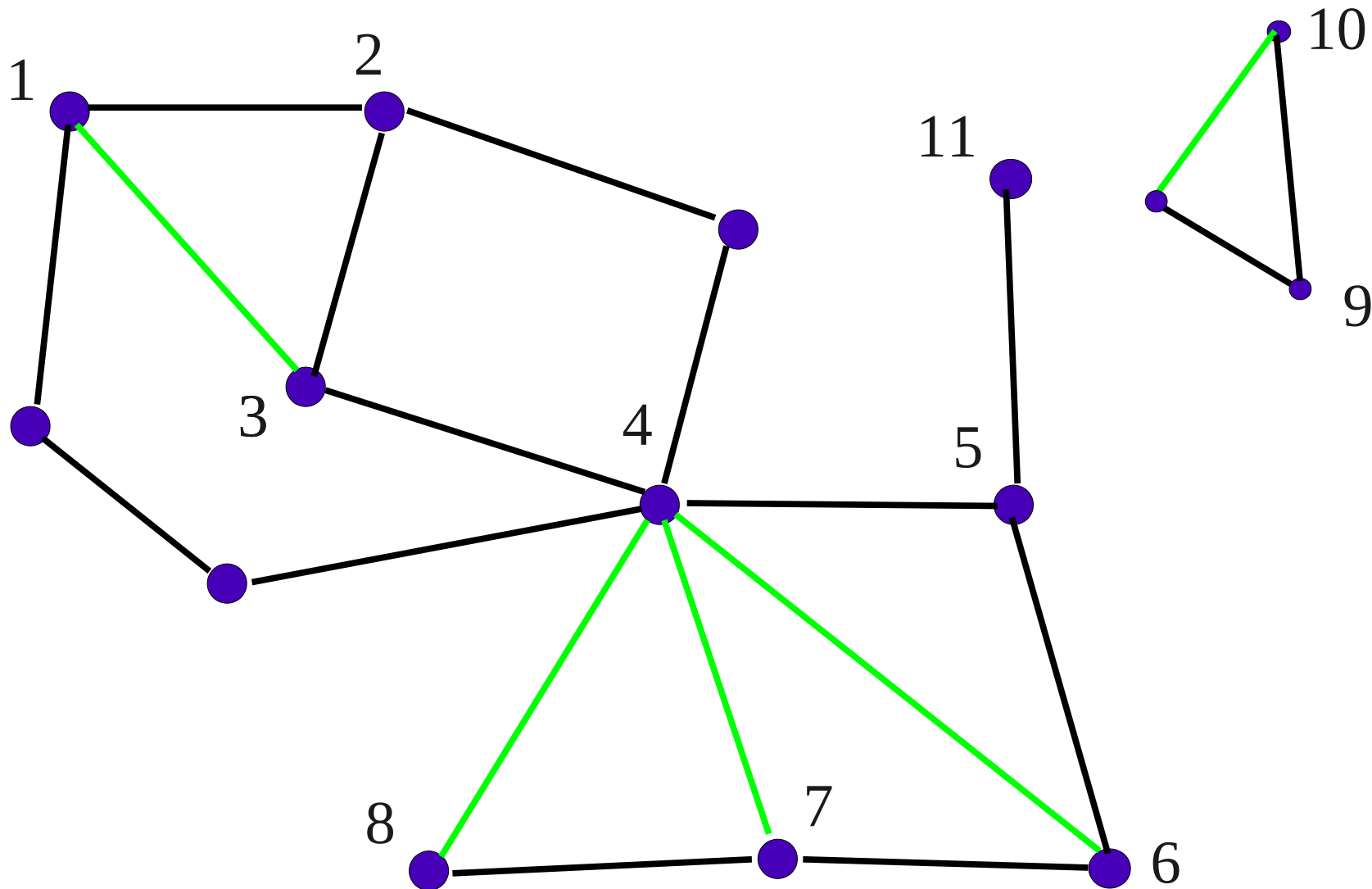
We arrive back at vertex 5 with no vertex having seen a neighboring vertex numbered less than 5. So this must be a biconnected comp.



# Biconnected Components

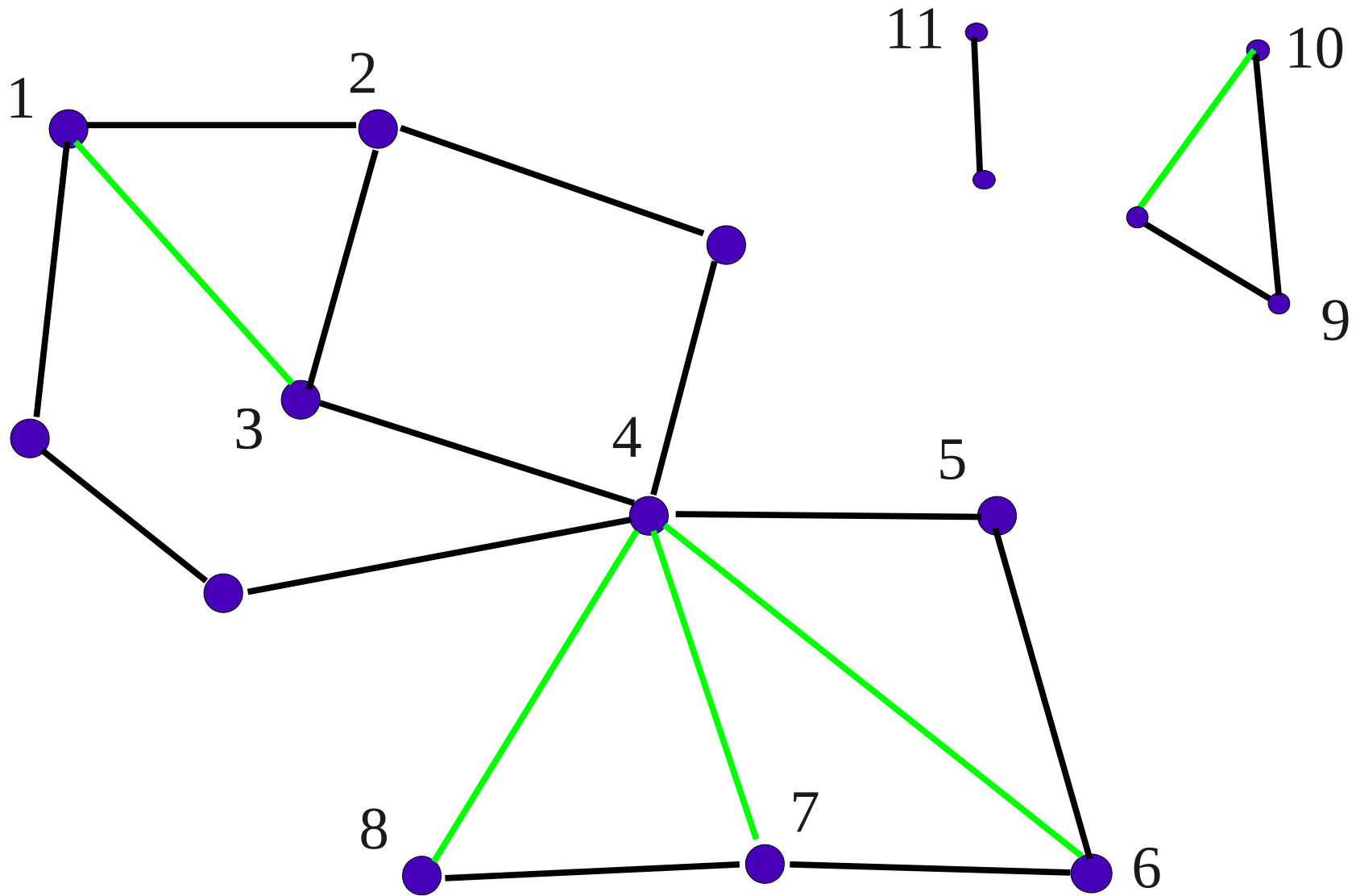


# Biconnected Components

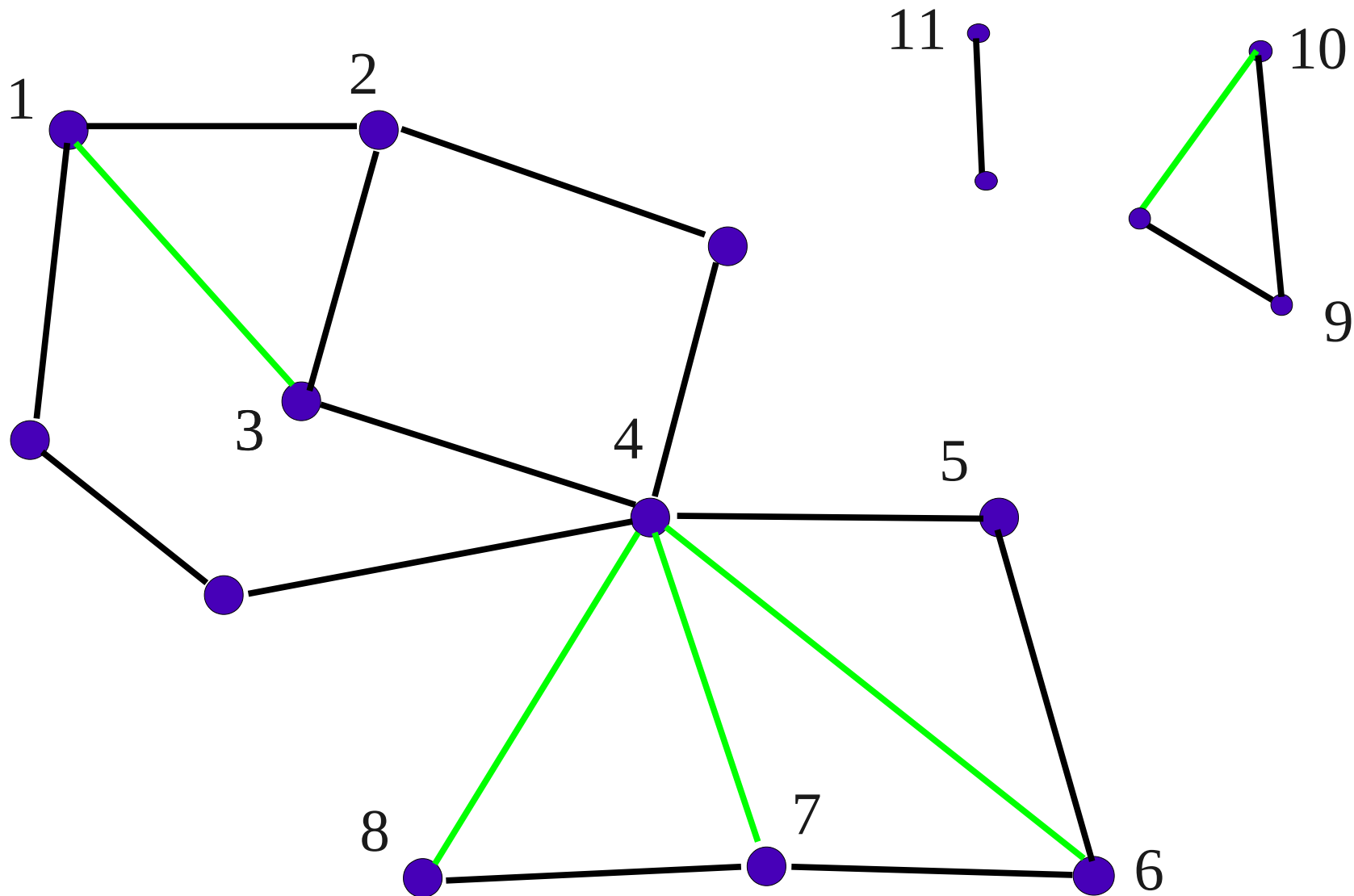


We return to vertex 5 with no vertex having seen a neighboring vertex numbered less than 5. So this must be a biconnected comp.

# Biconnected Components



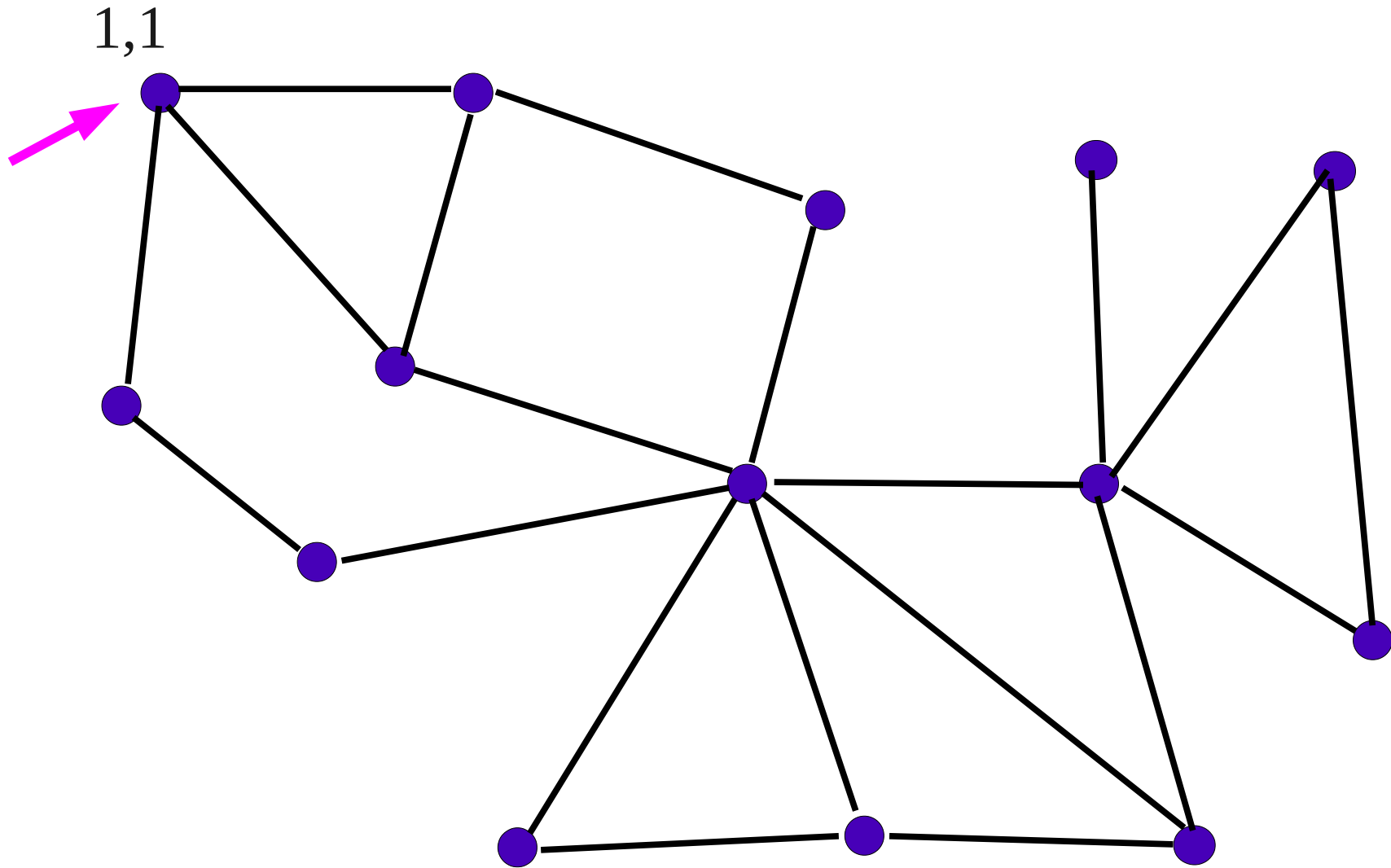
# Biconnected Components



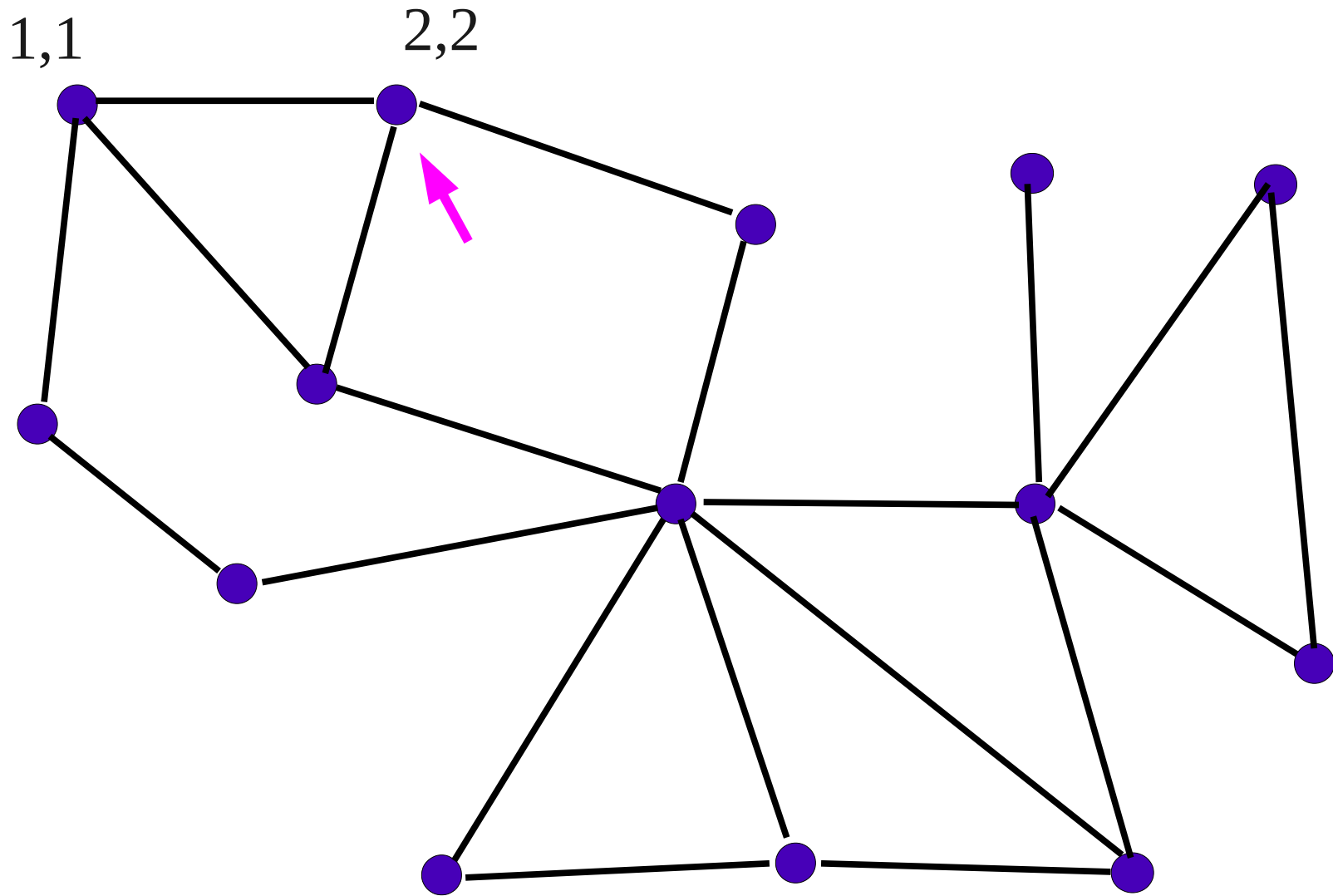
This suggests that each vertex carry a second number which is the lowest numbered vertex seen so far from a path out of it.



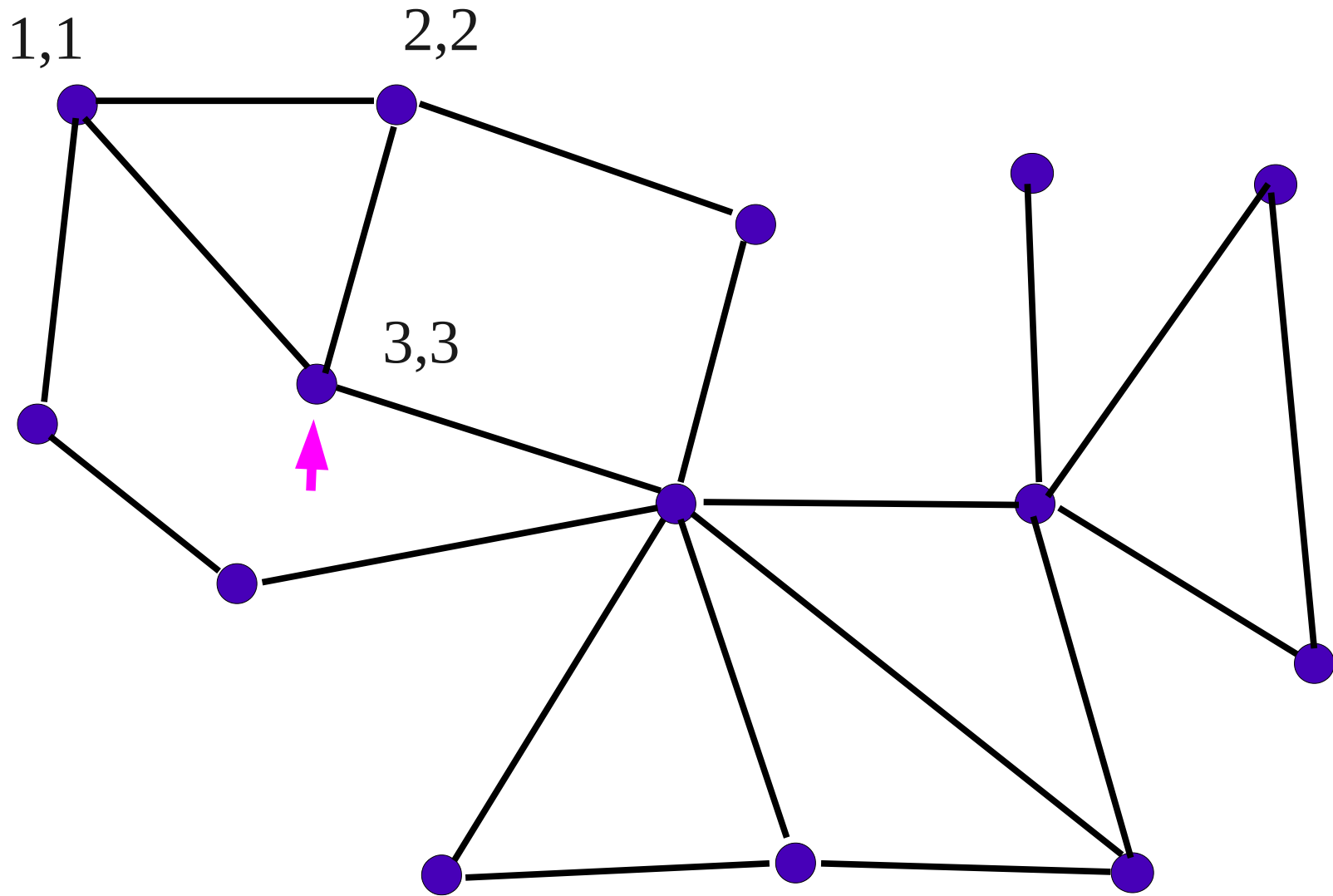
# Biconnected Components



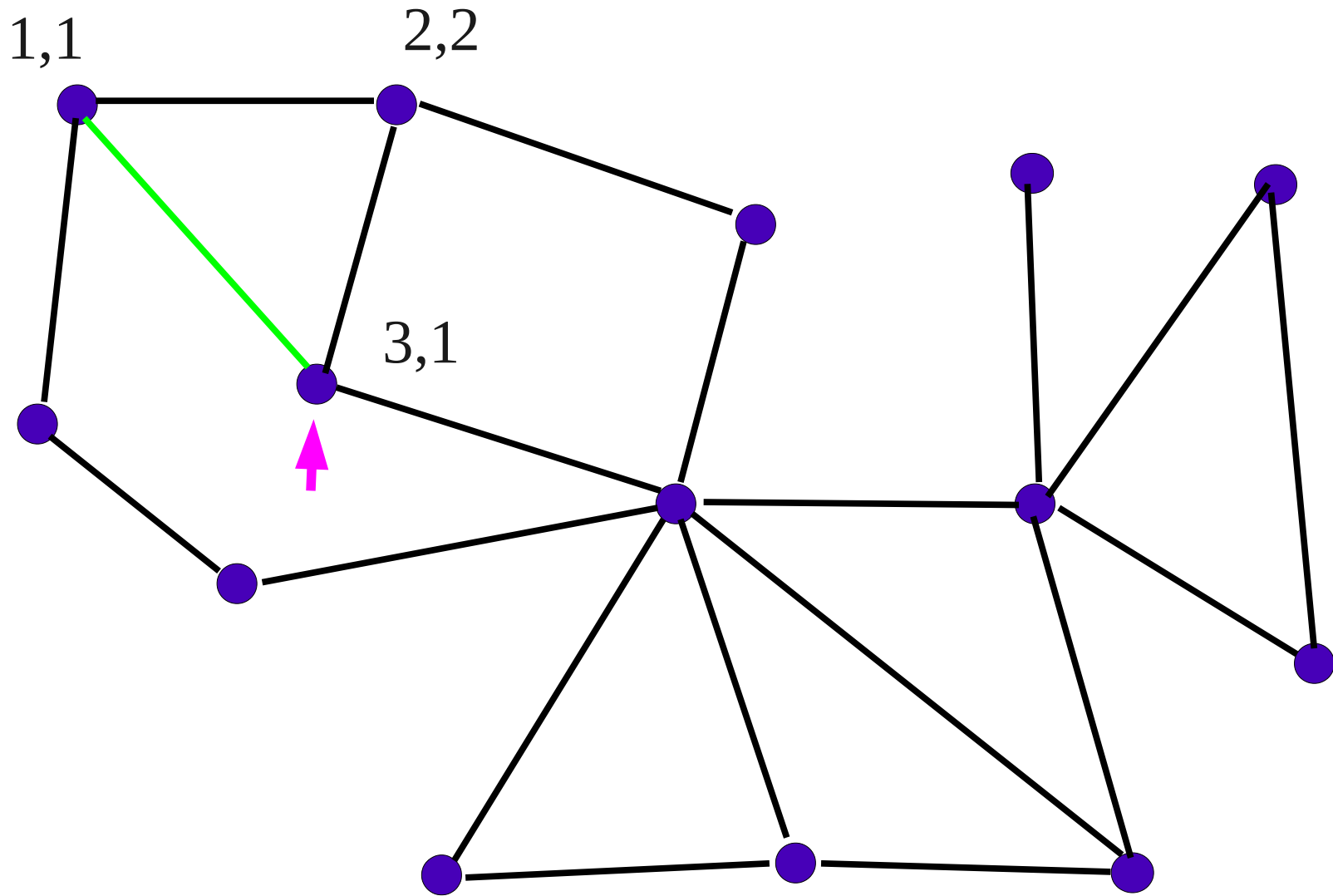
# Biconnected Components



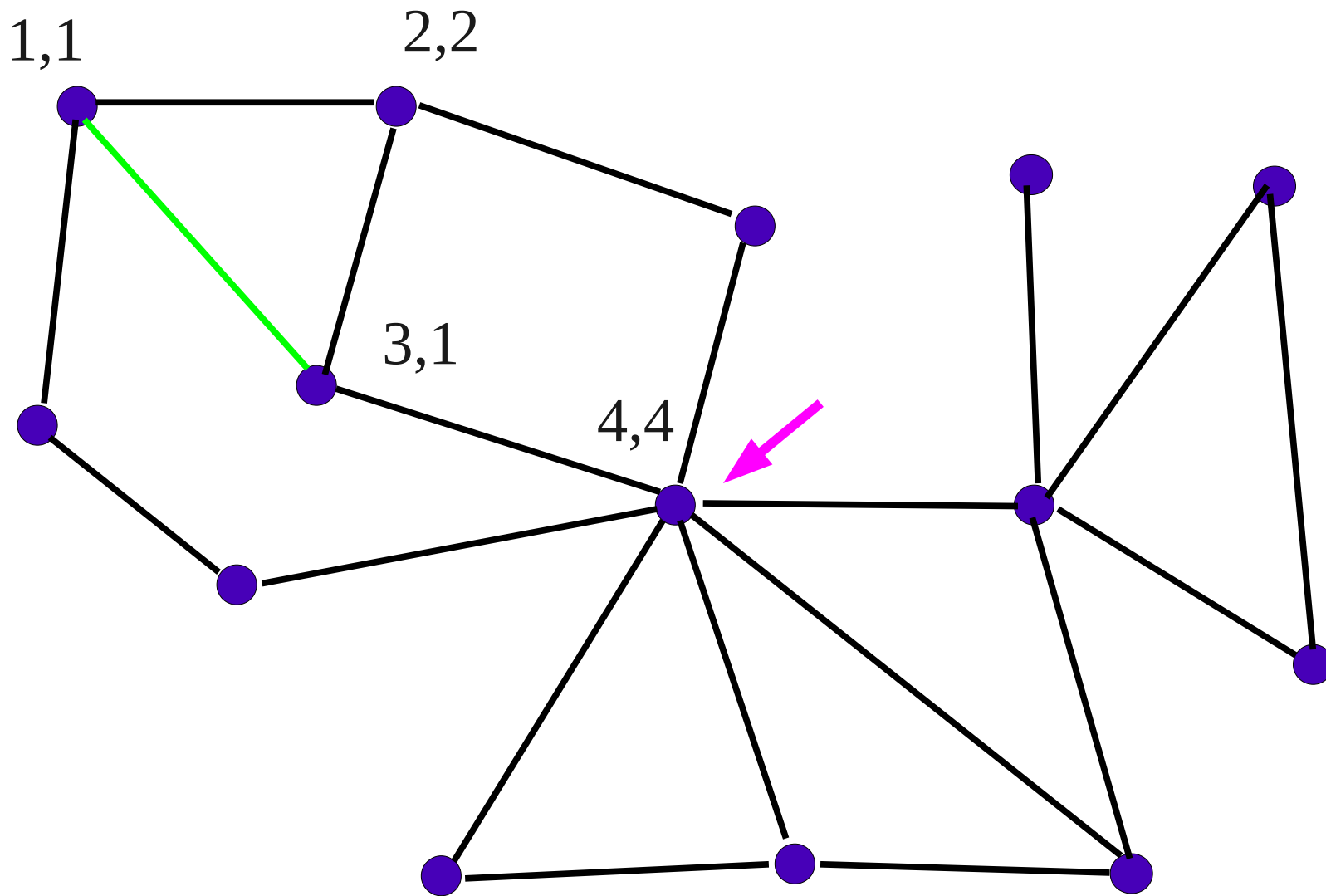
# Biconnected Components



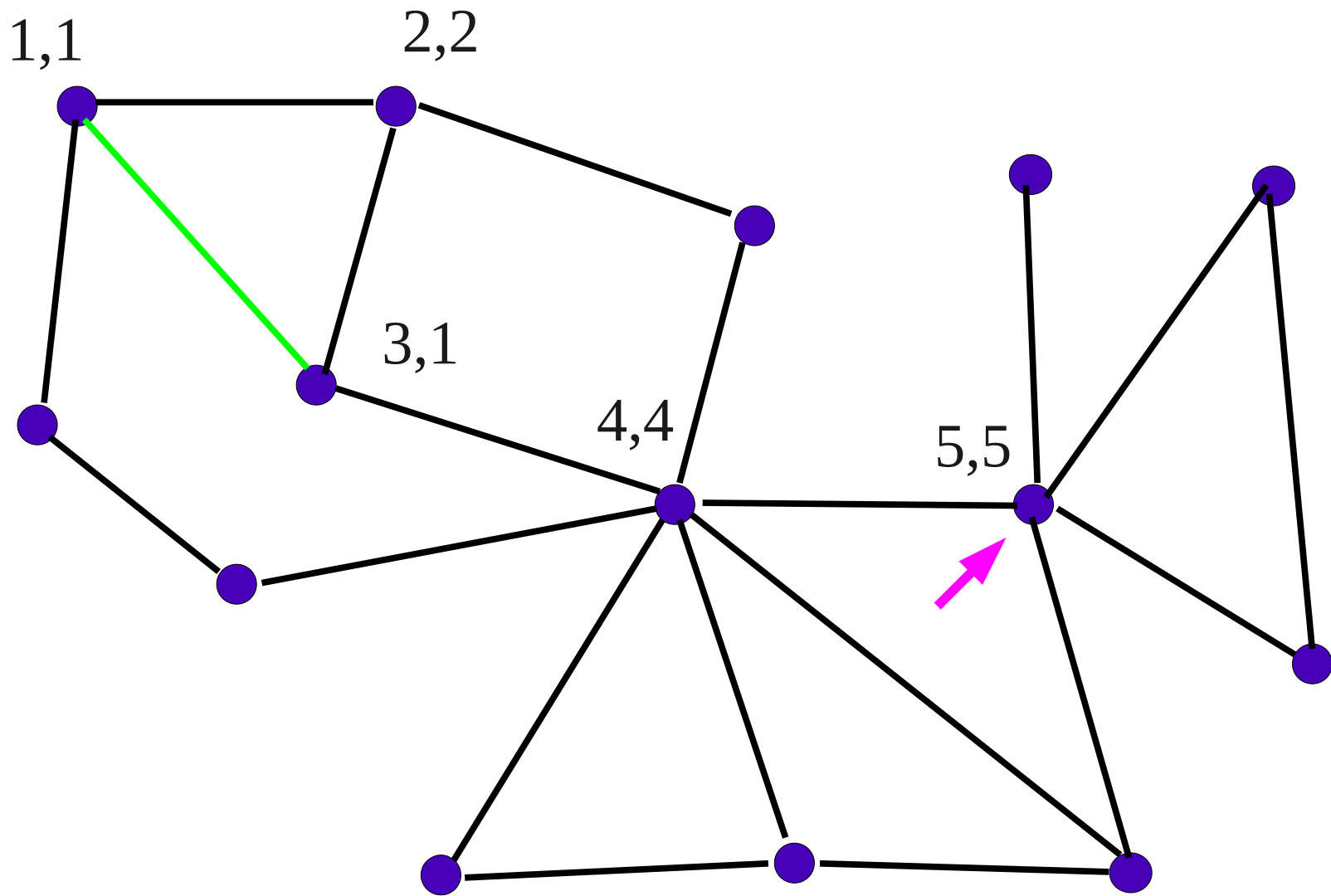
# Biconnected Components



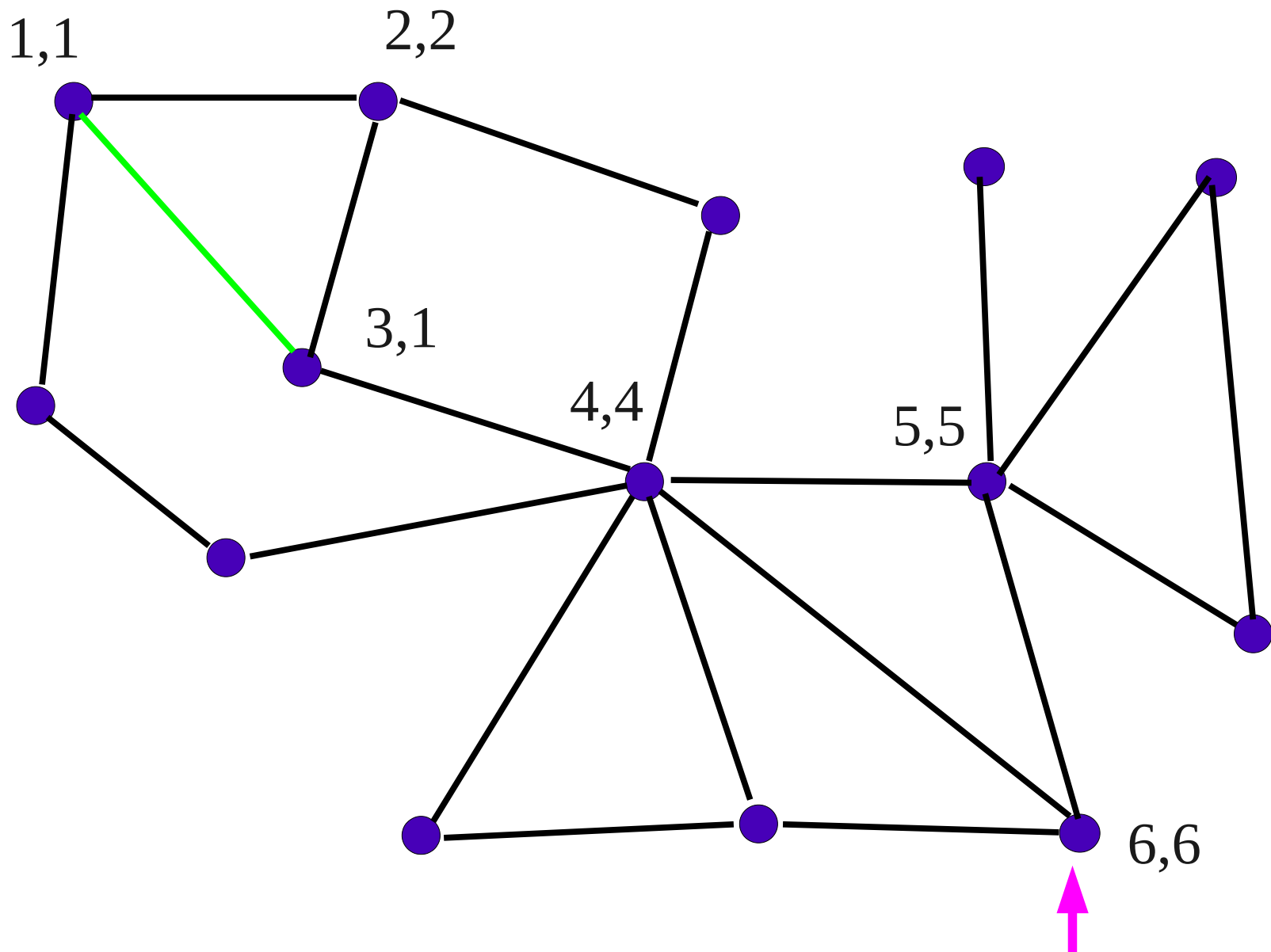
# Biconnected Components



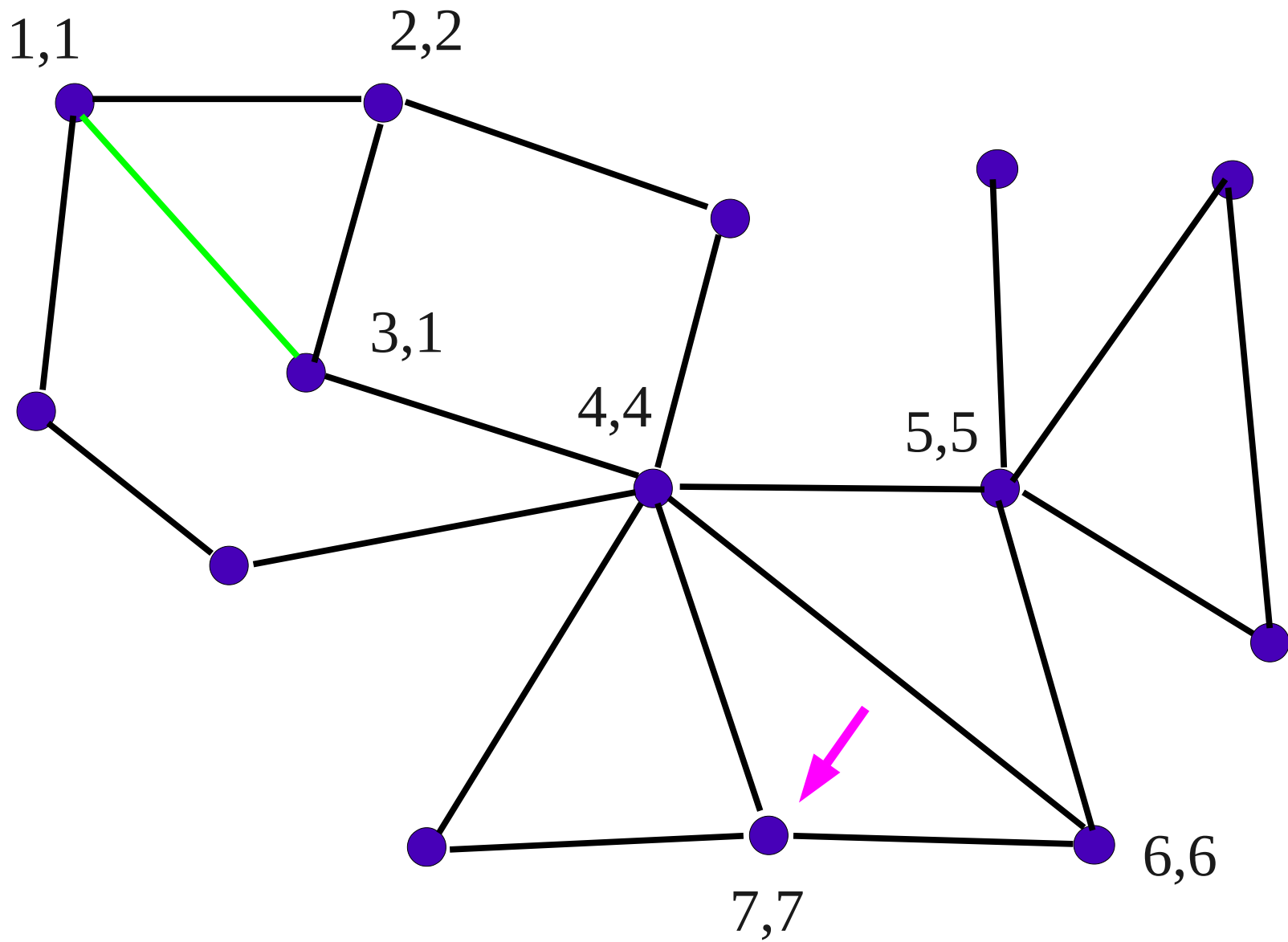
# Biconnected Components



# Biconnected Components

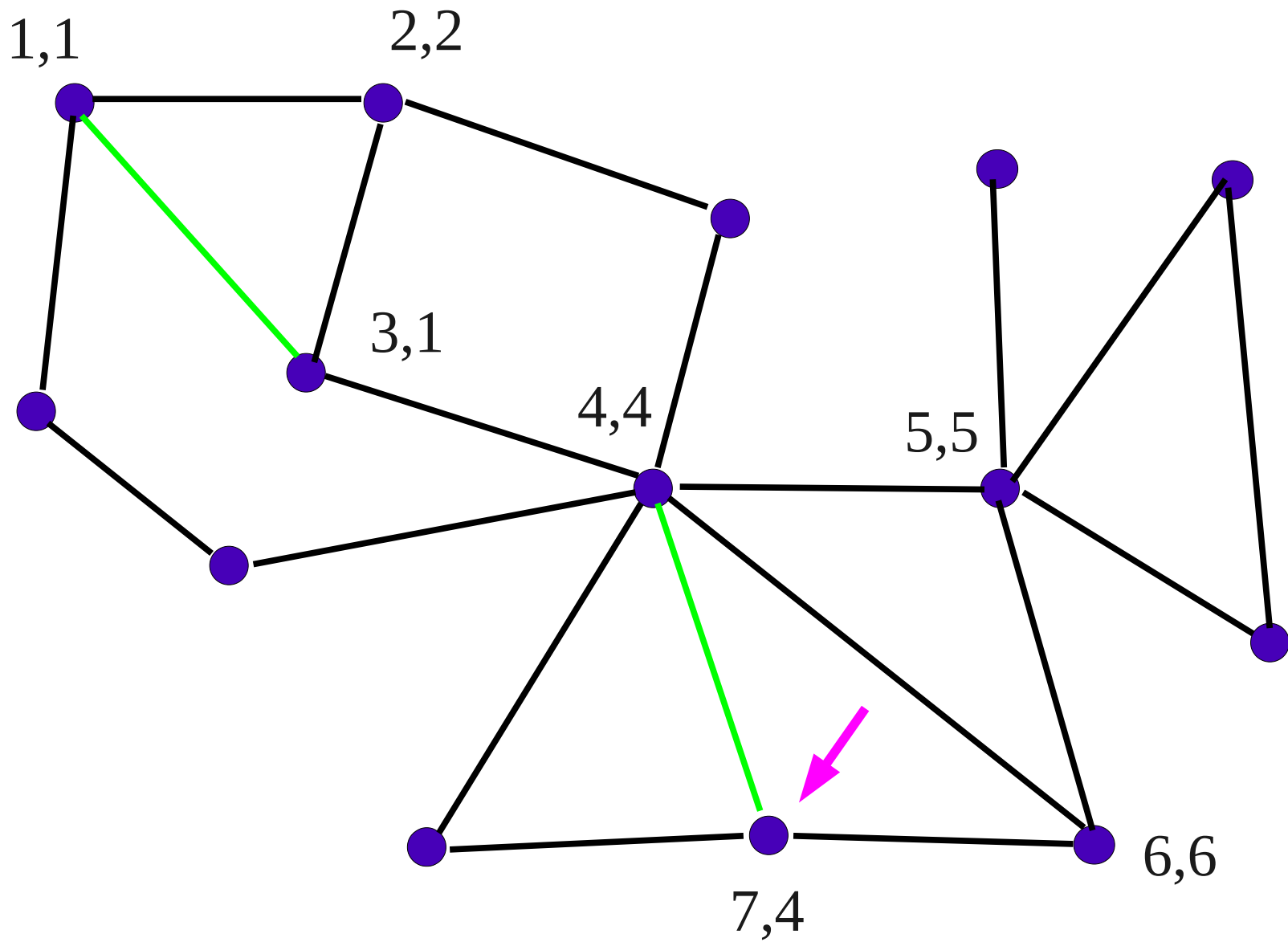


# Biconnected Components

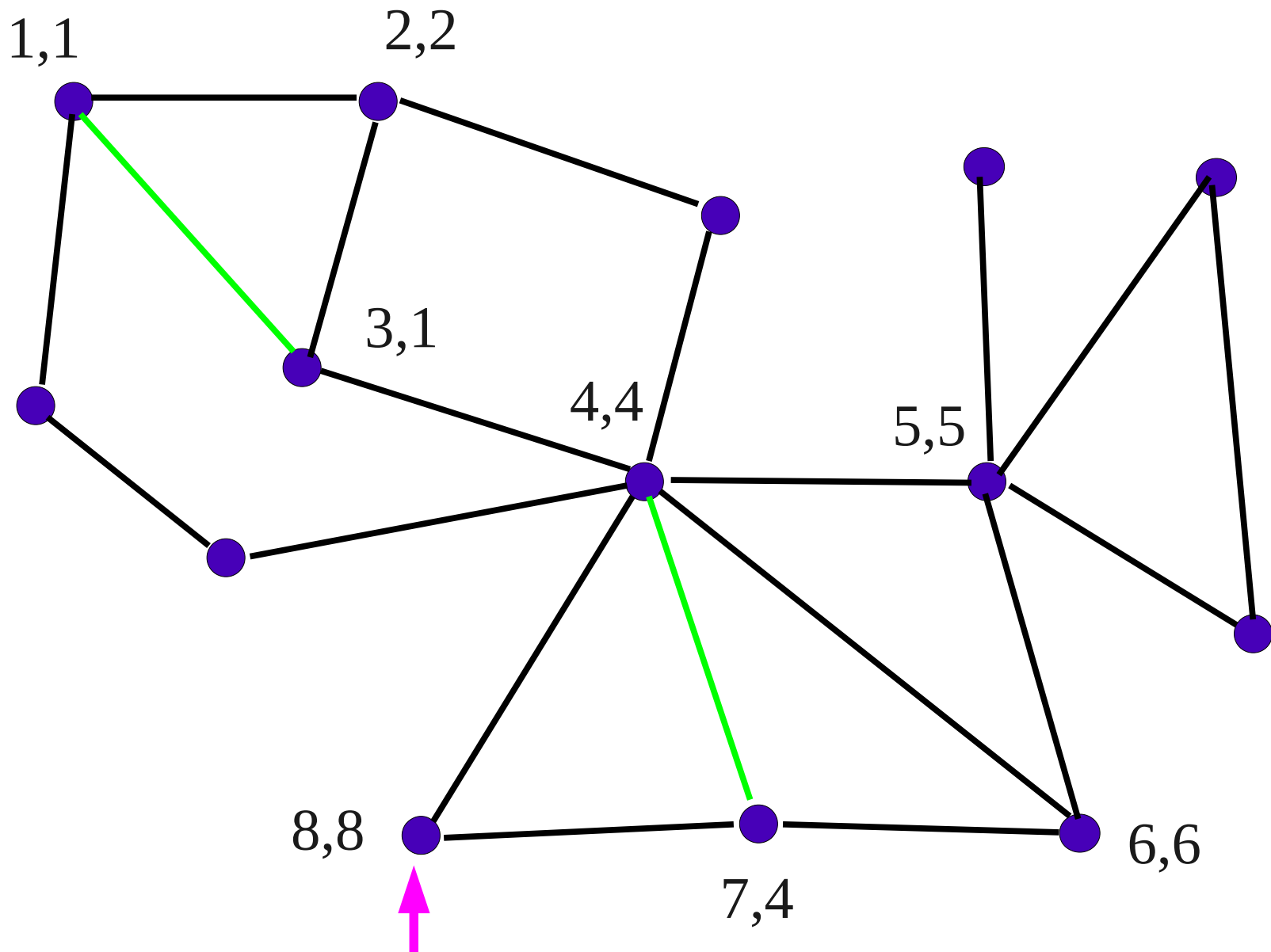




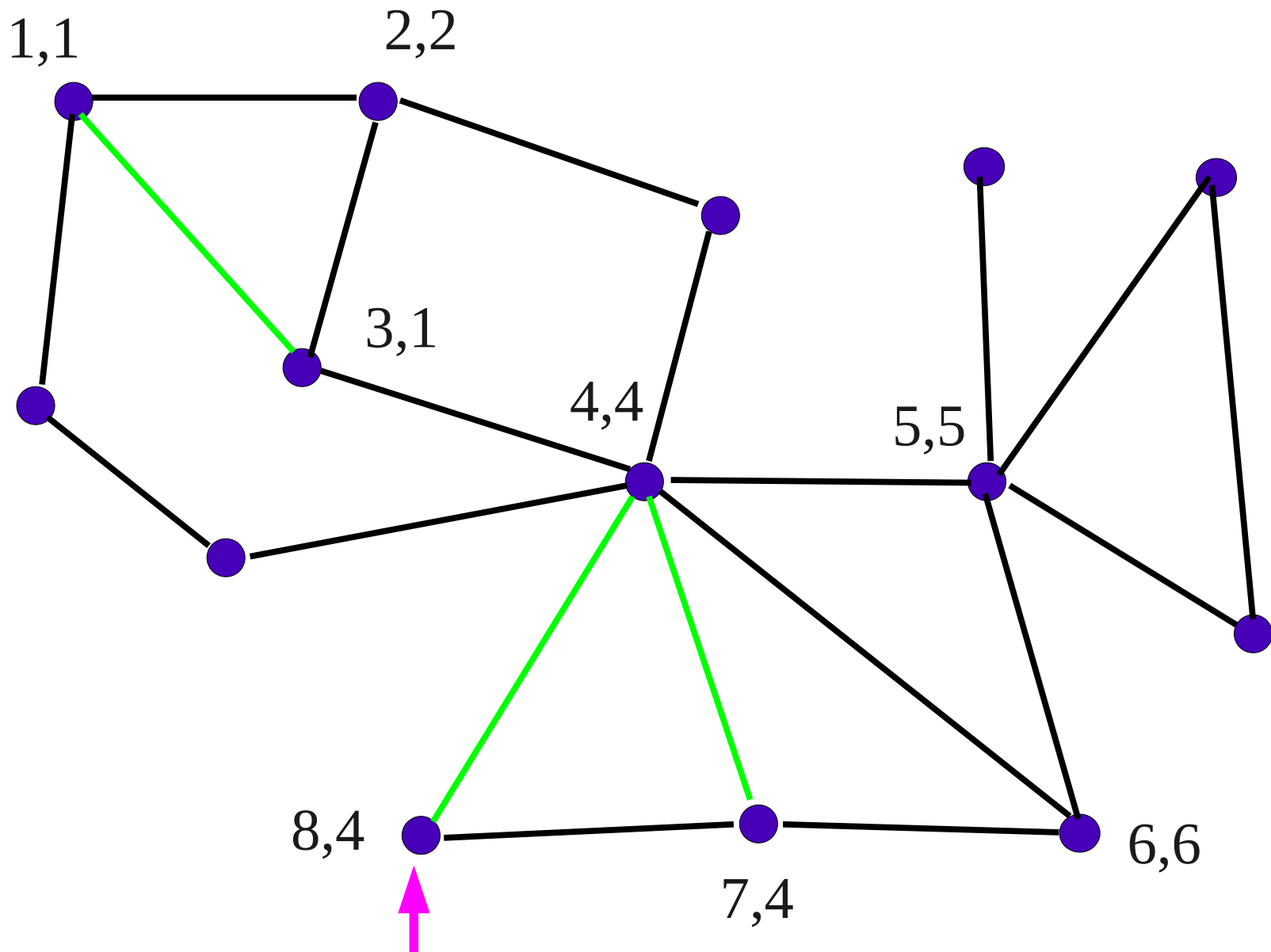
# Biconnected Components



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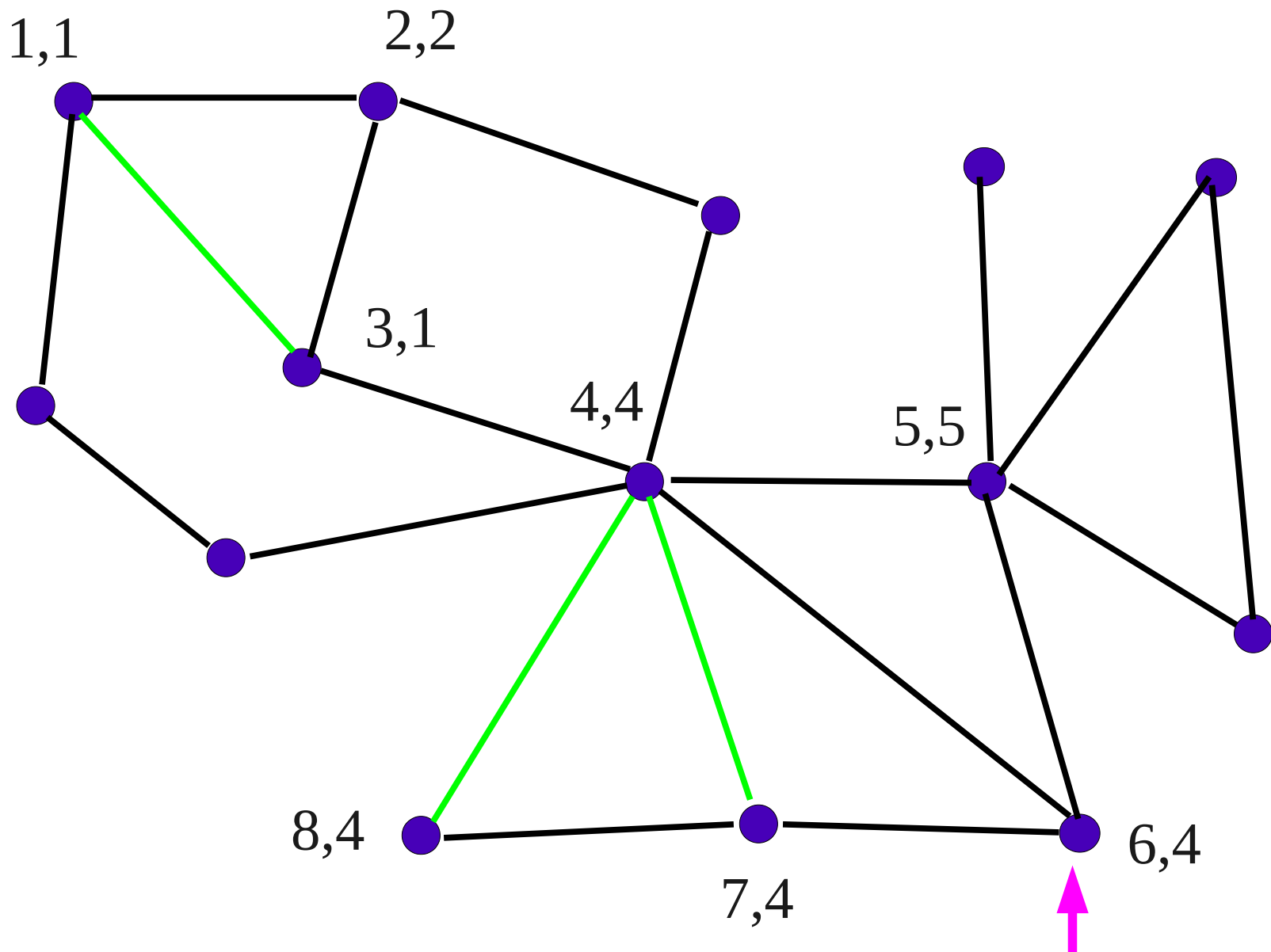


# Biconnected Components

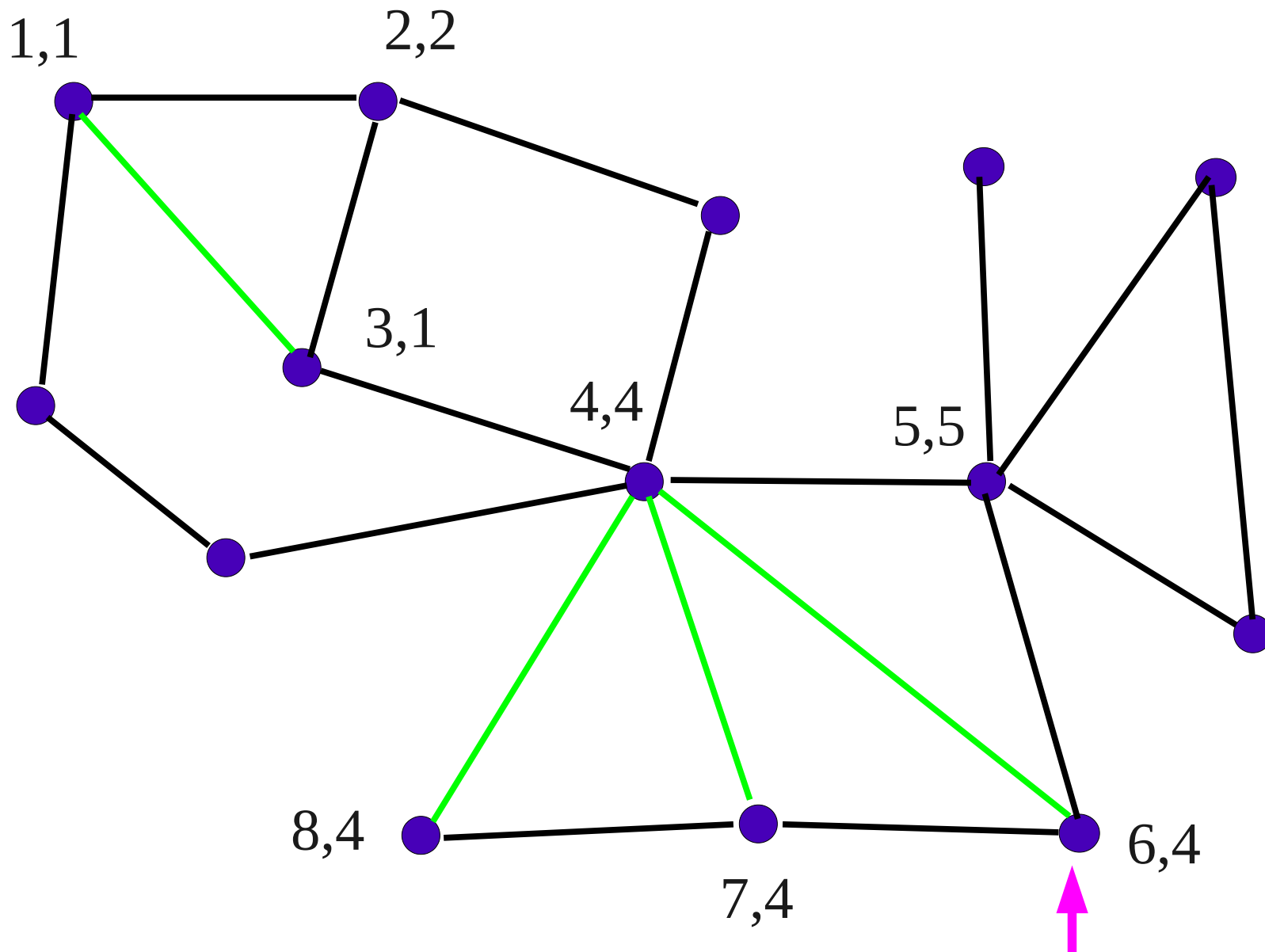




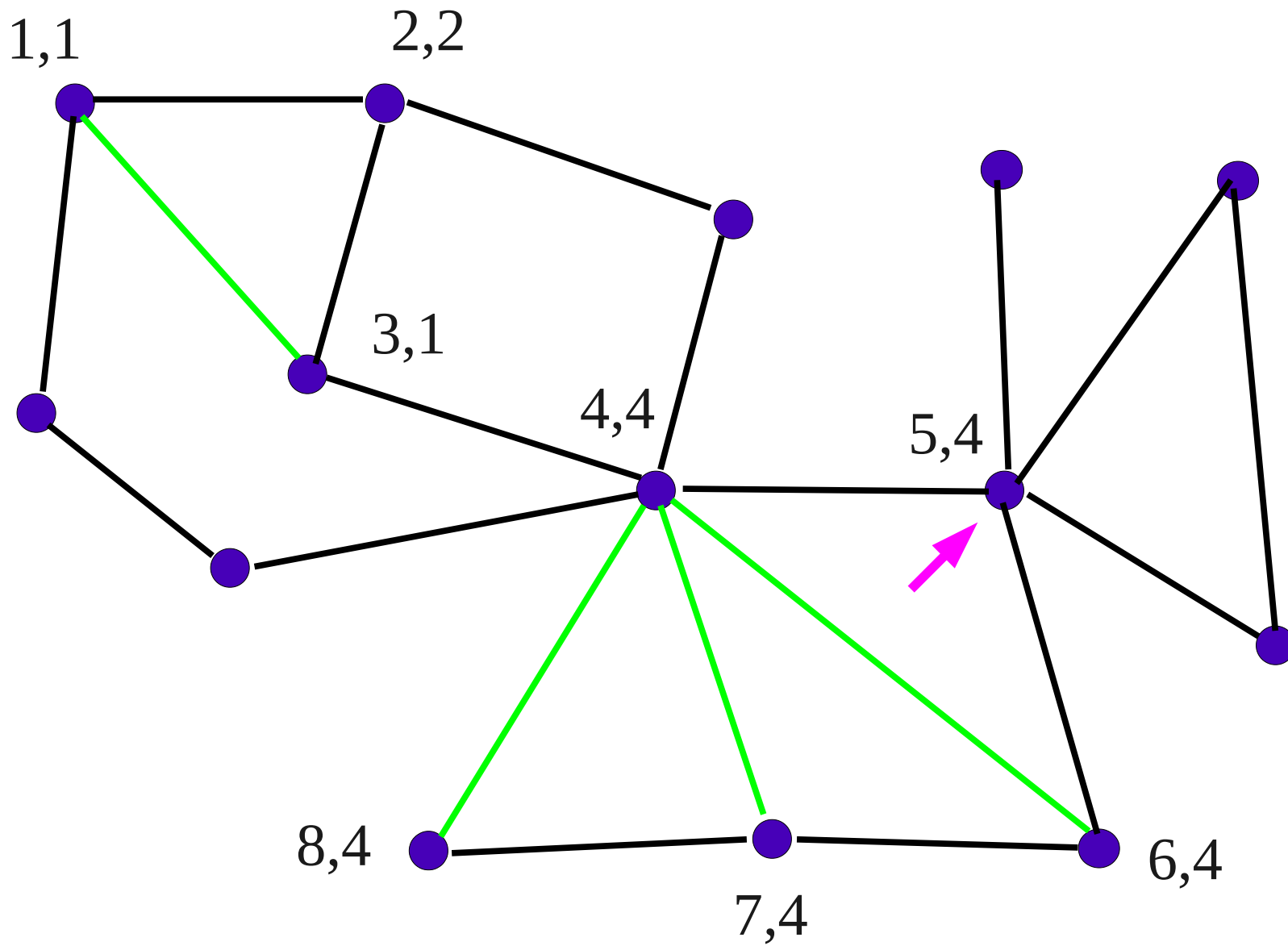
# Biconnected Components



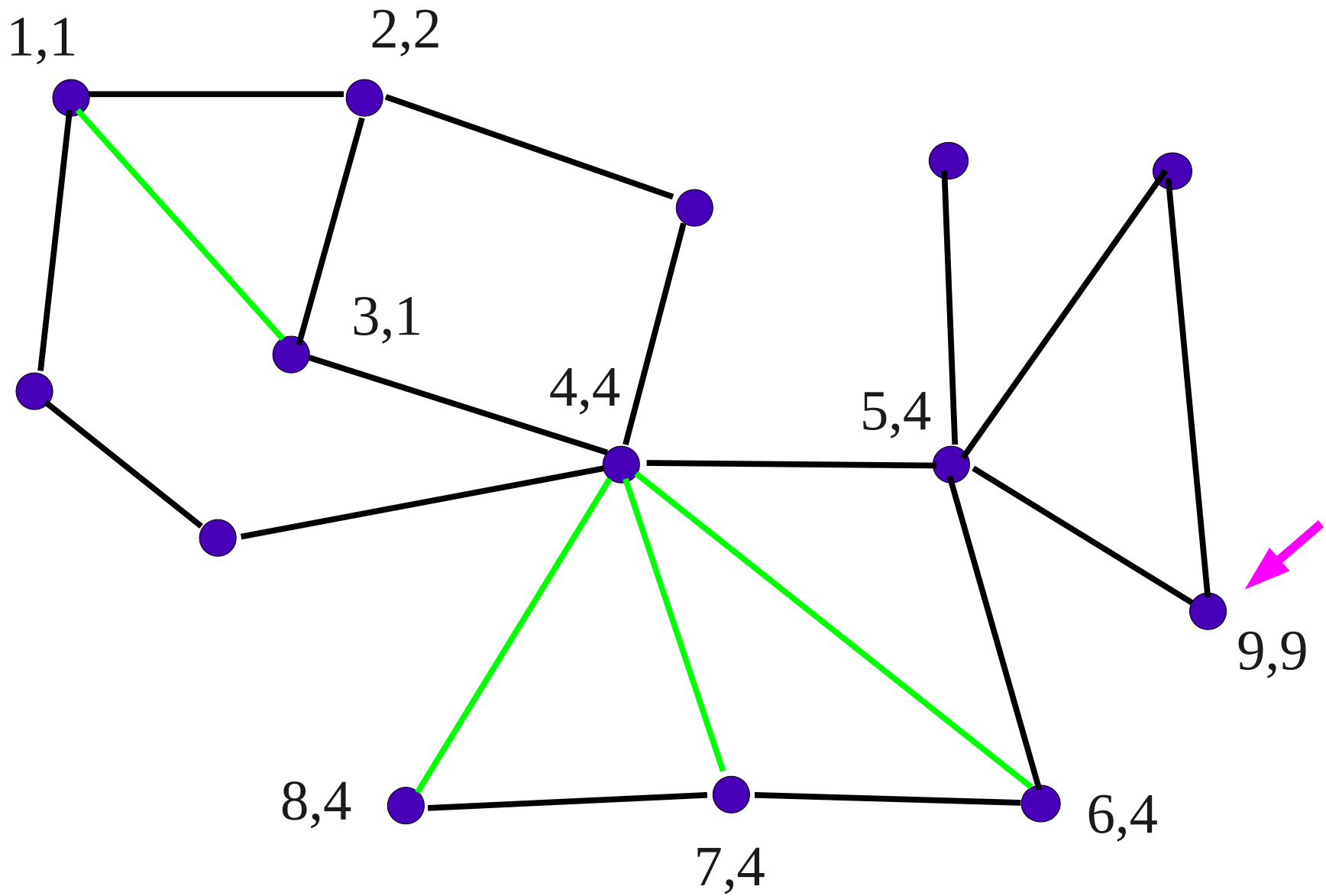
# Biconnected Components



# Biconnected Components

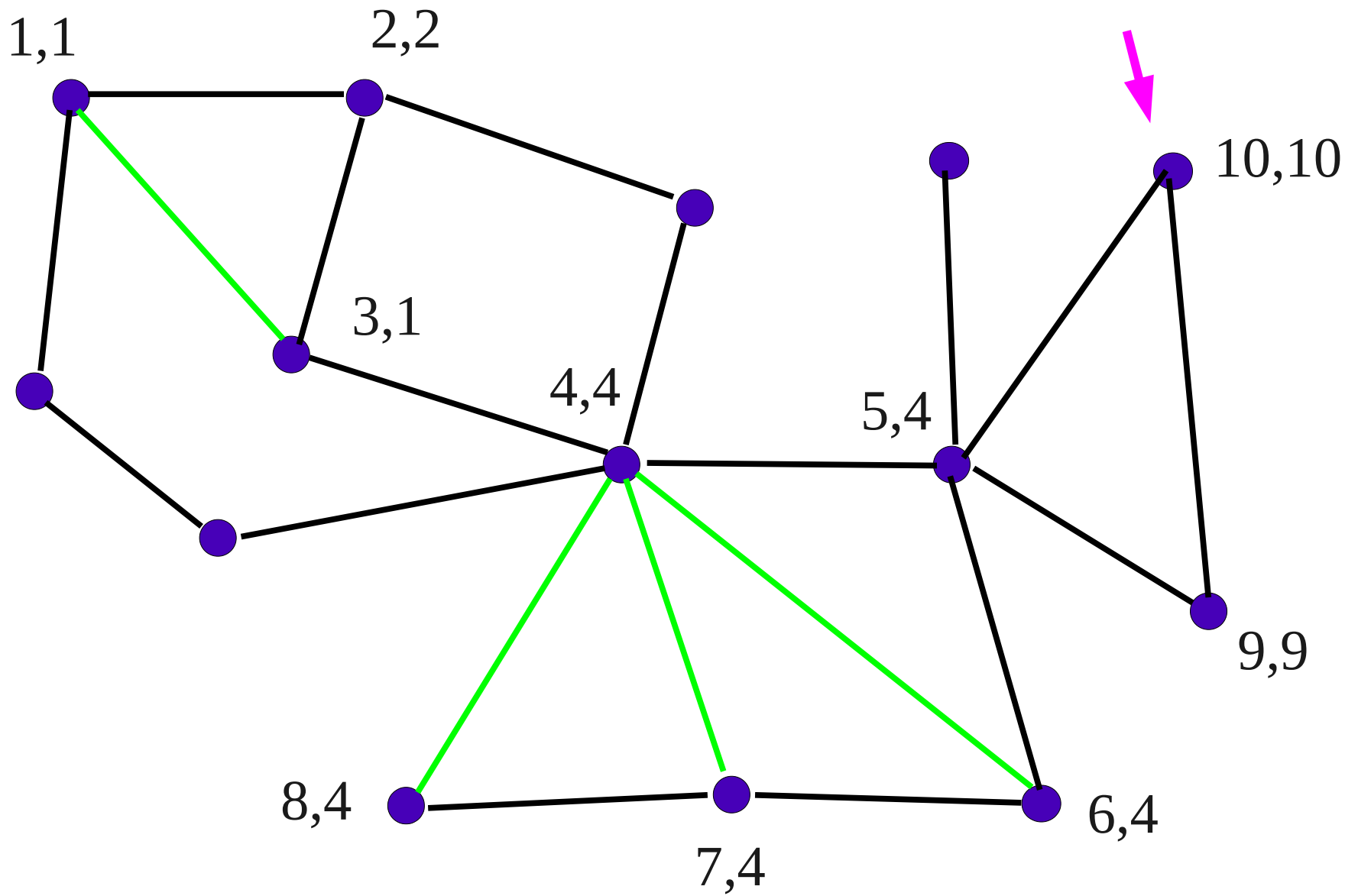


# Biconnected Components

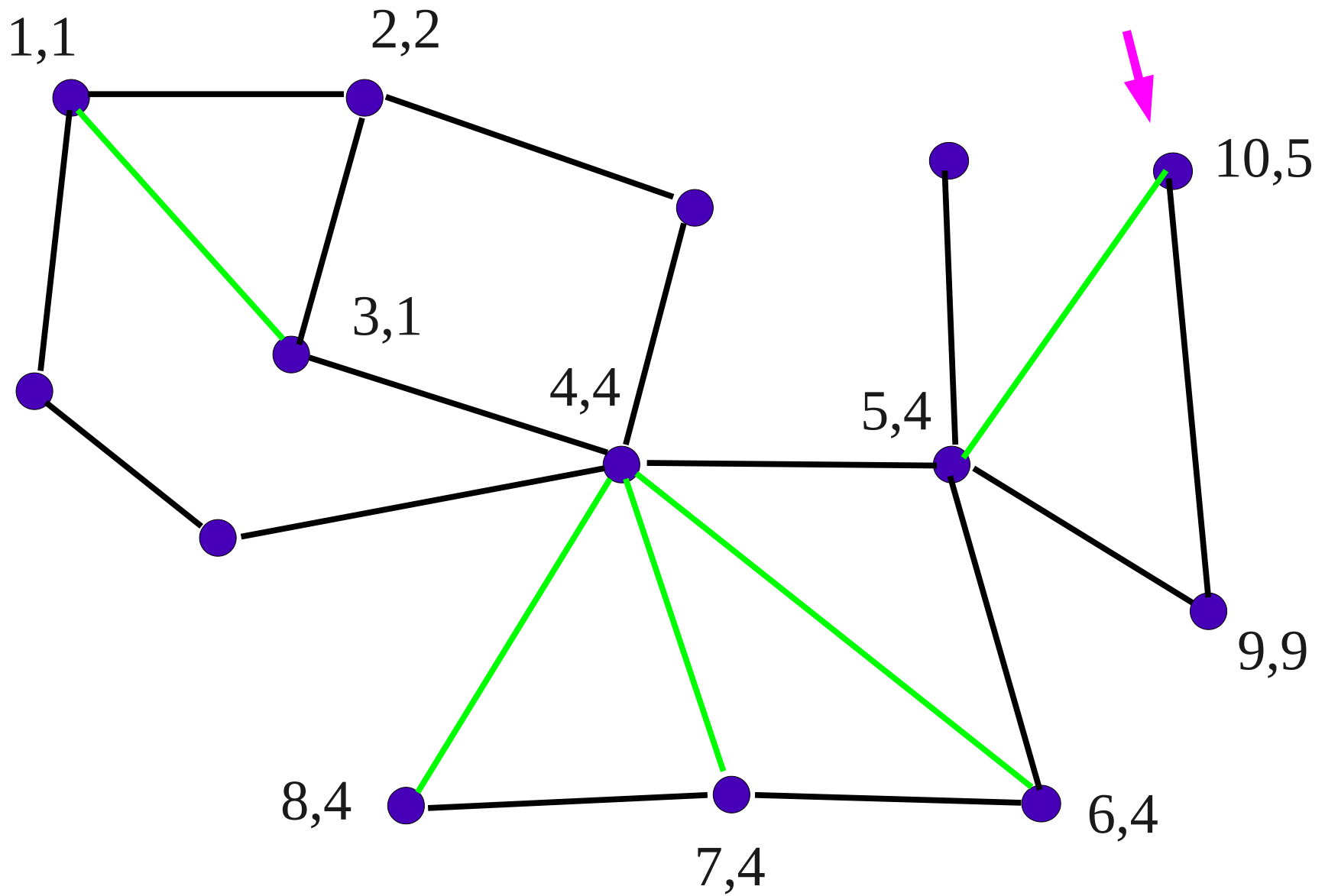




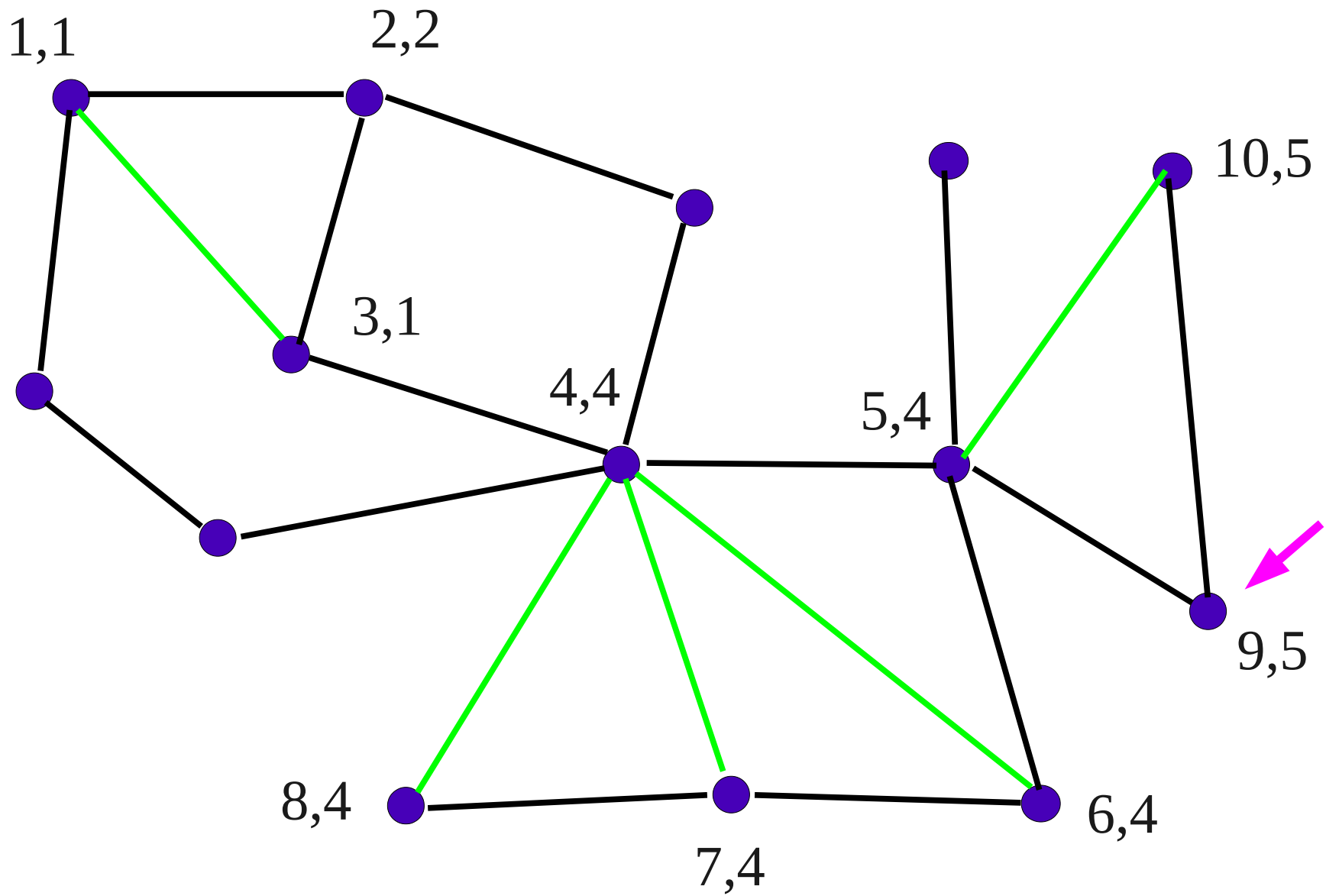
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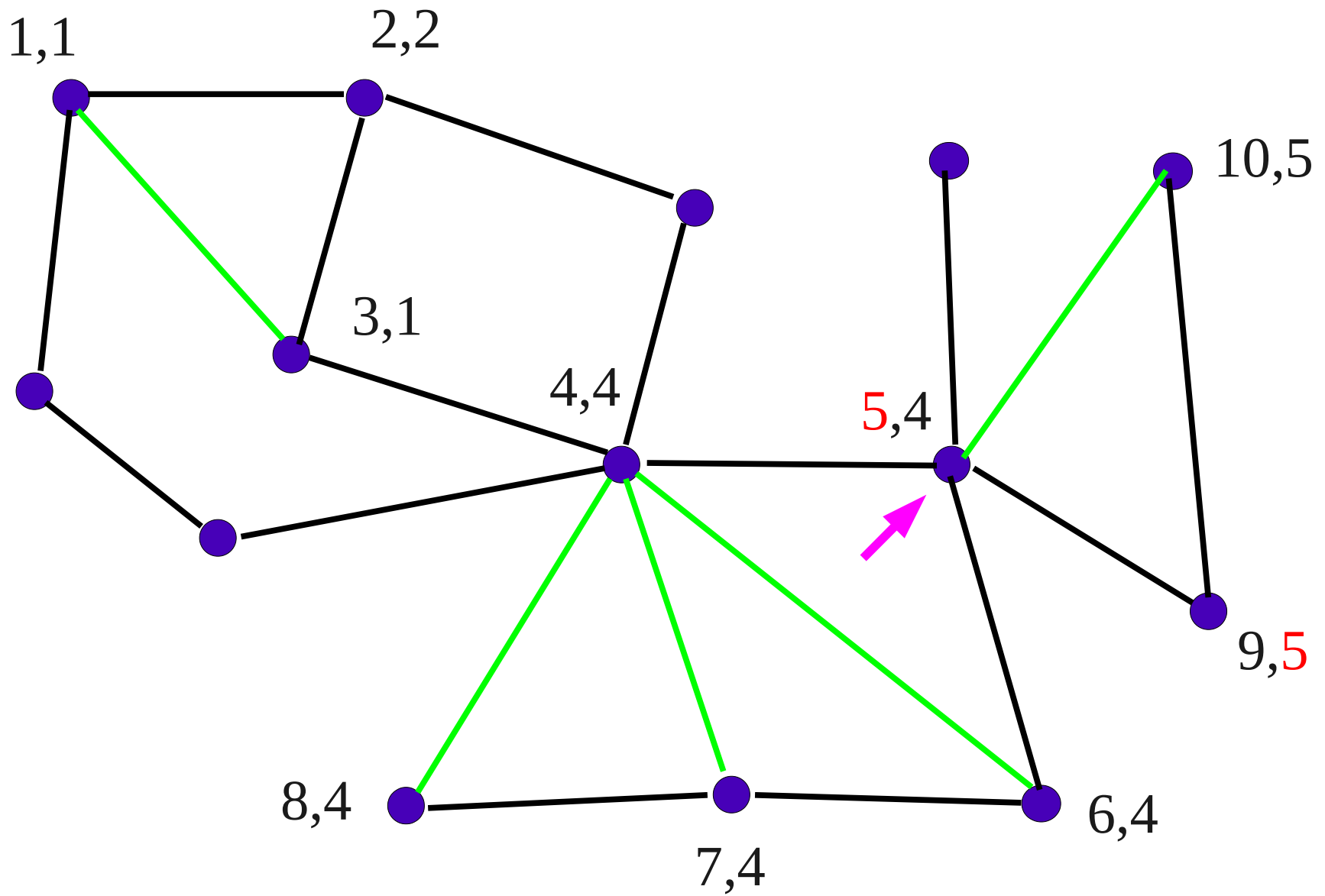
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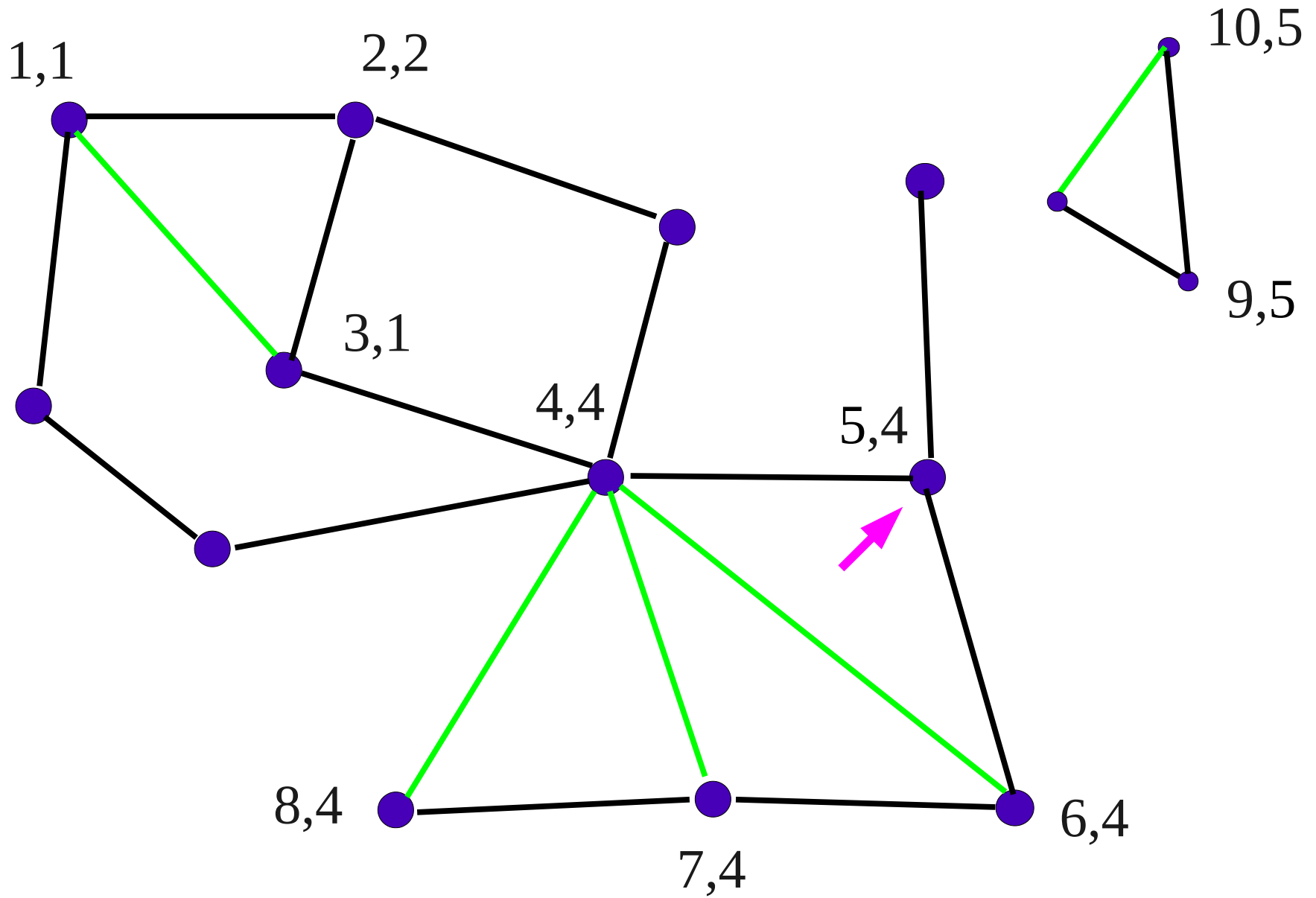
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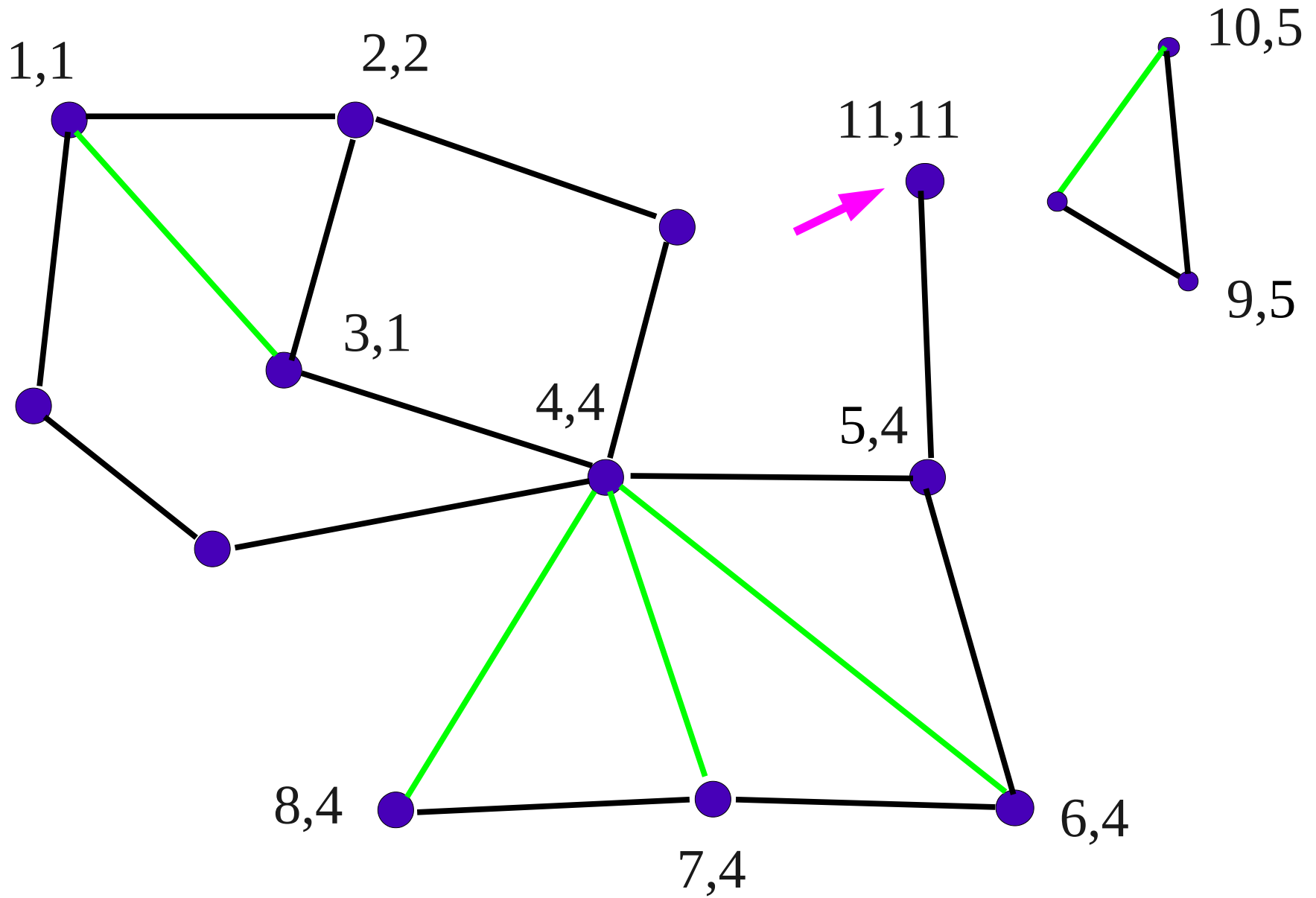
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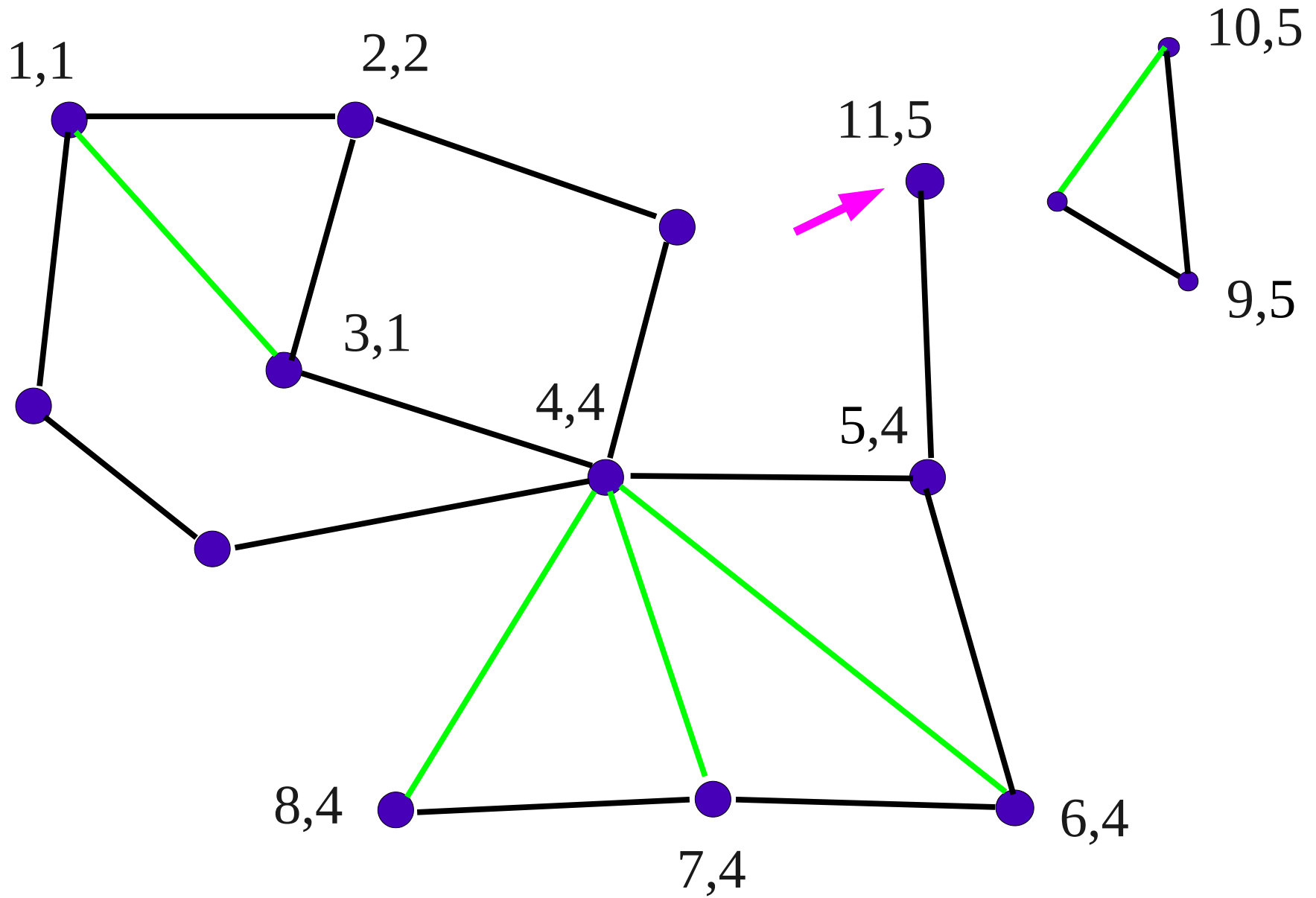
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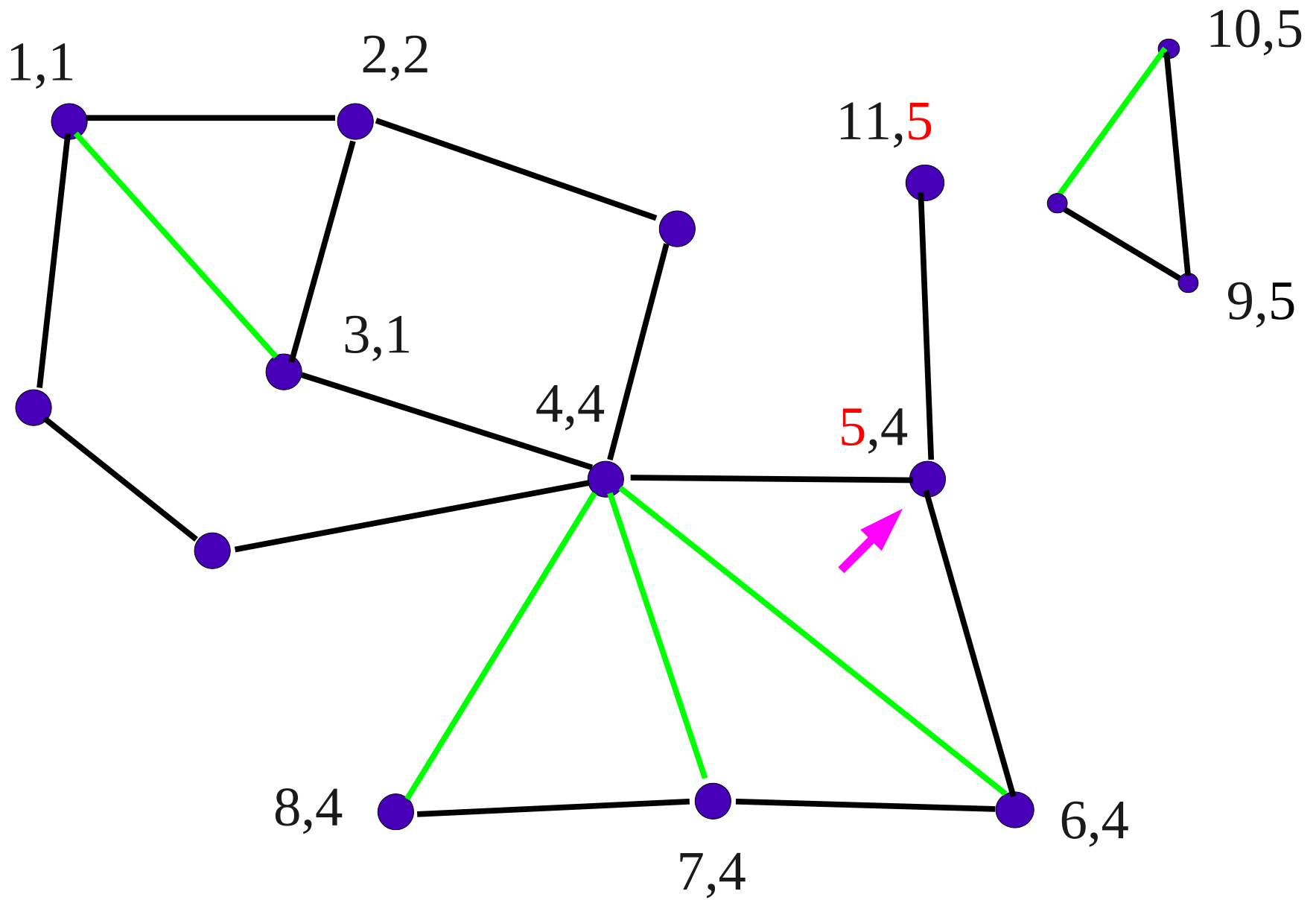
# Biconnected Components



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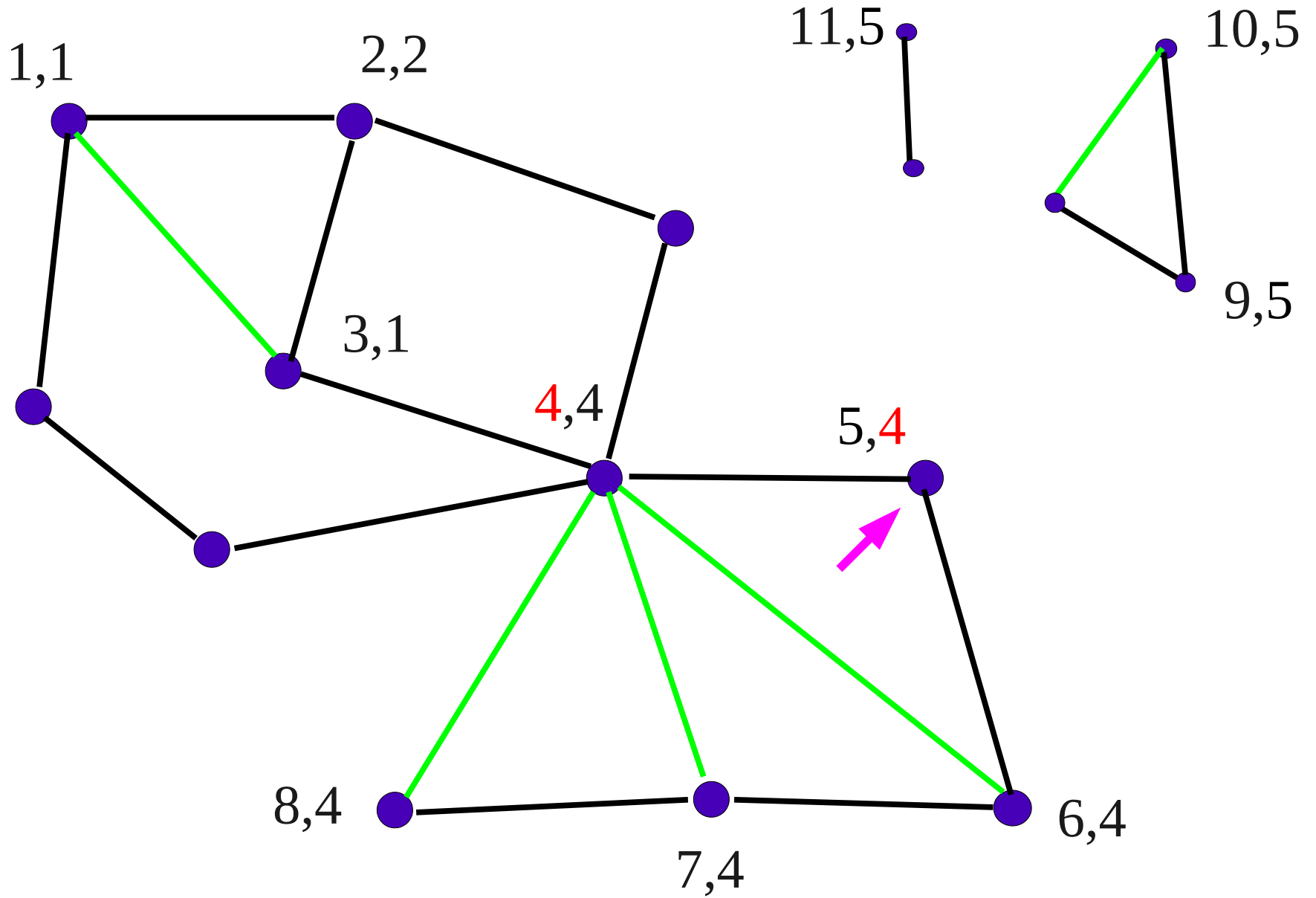


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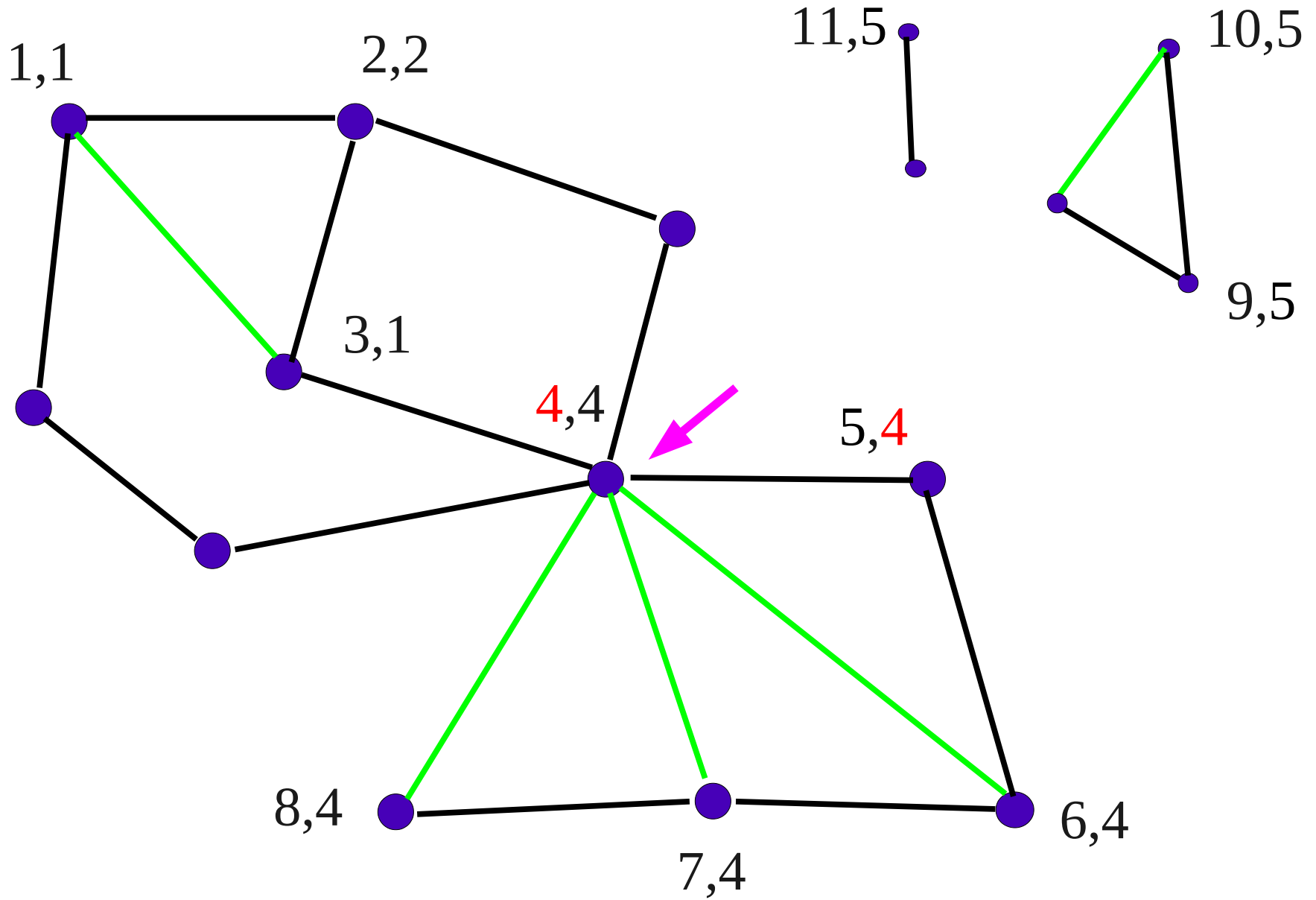




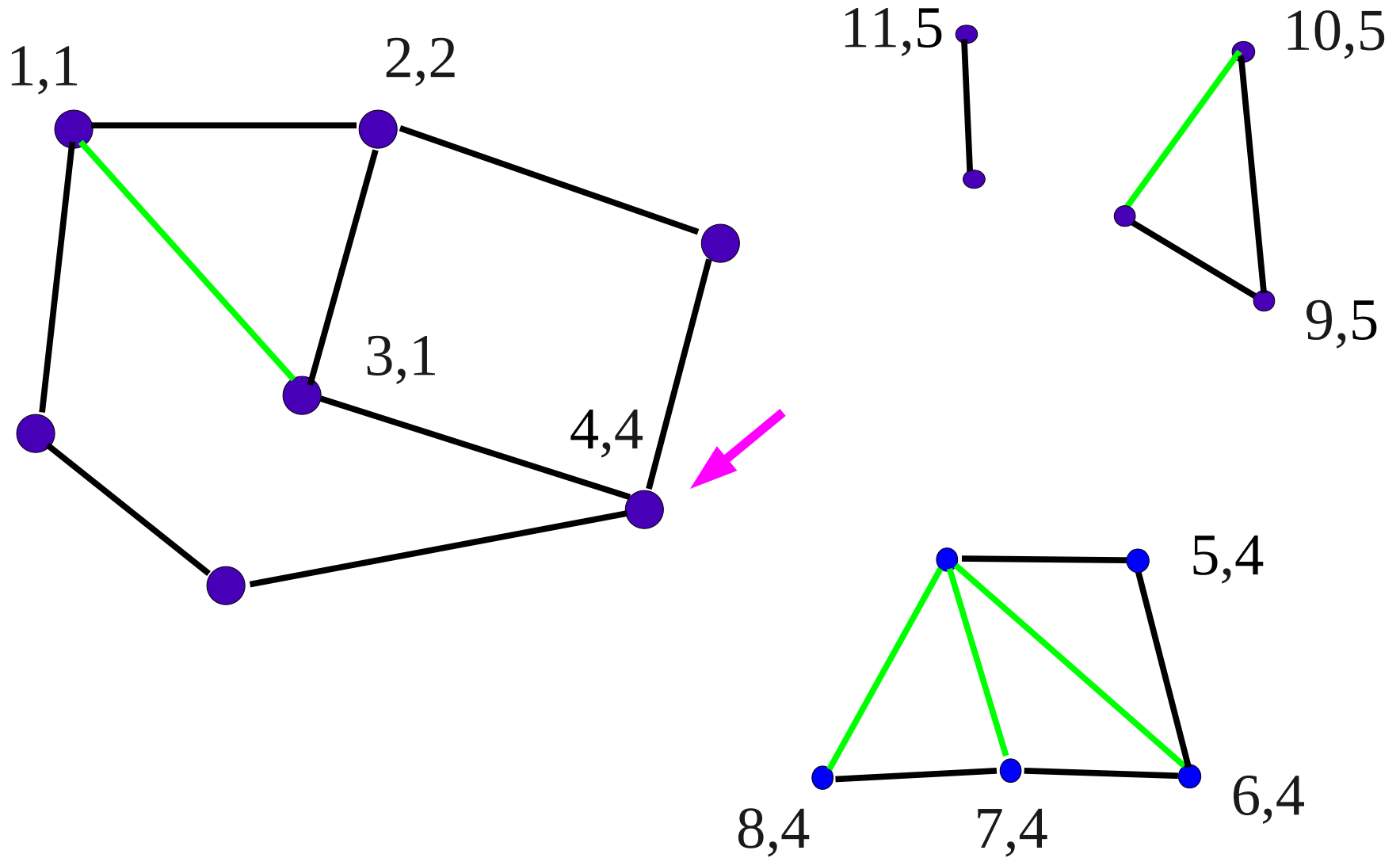
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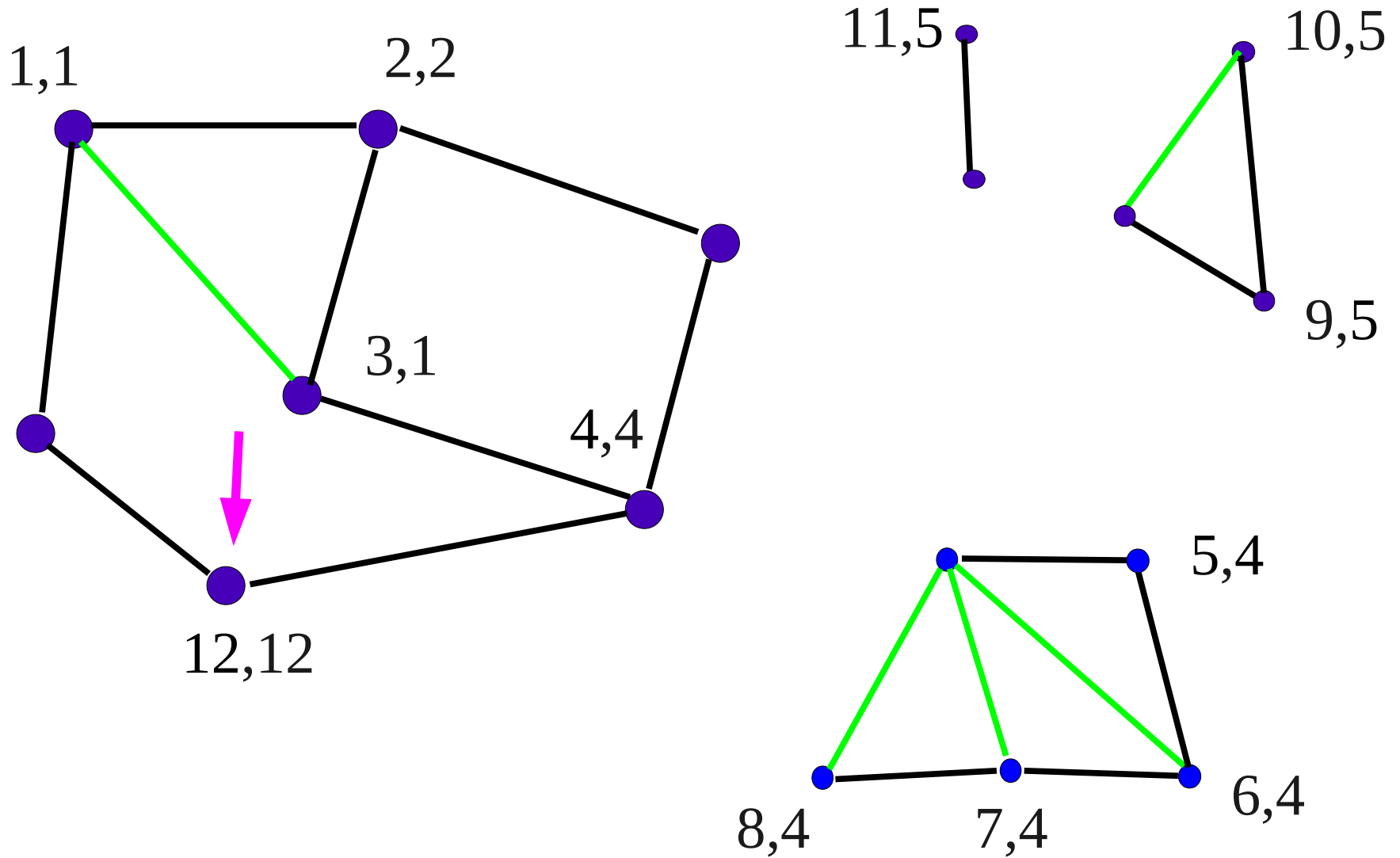
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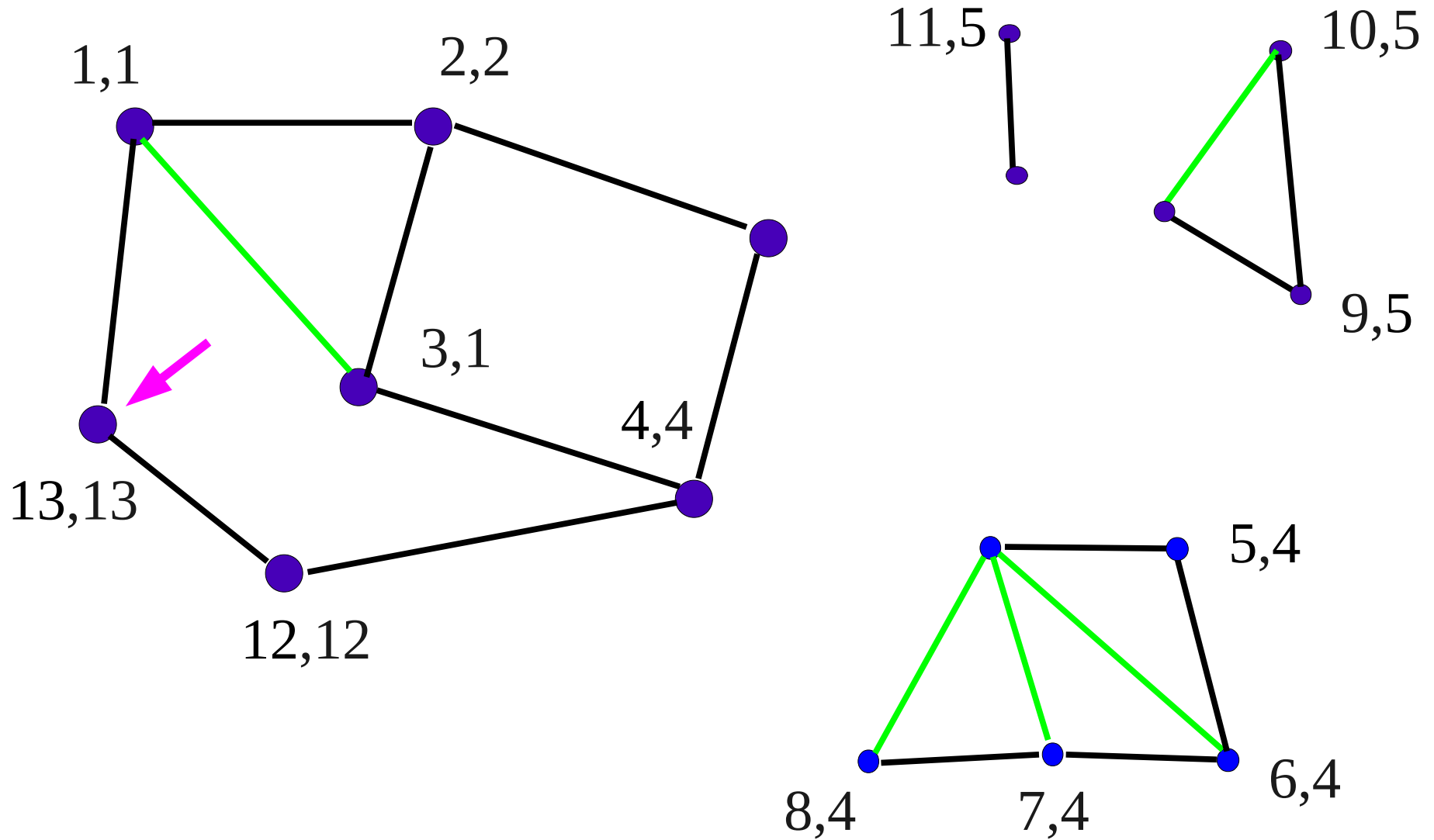
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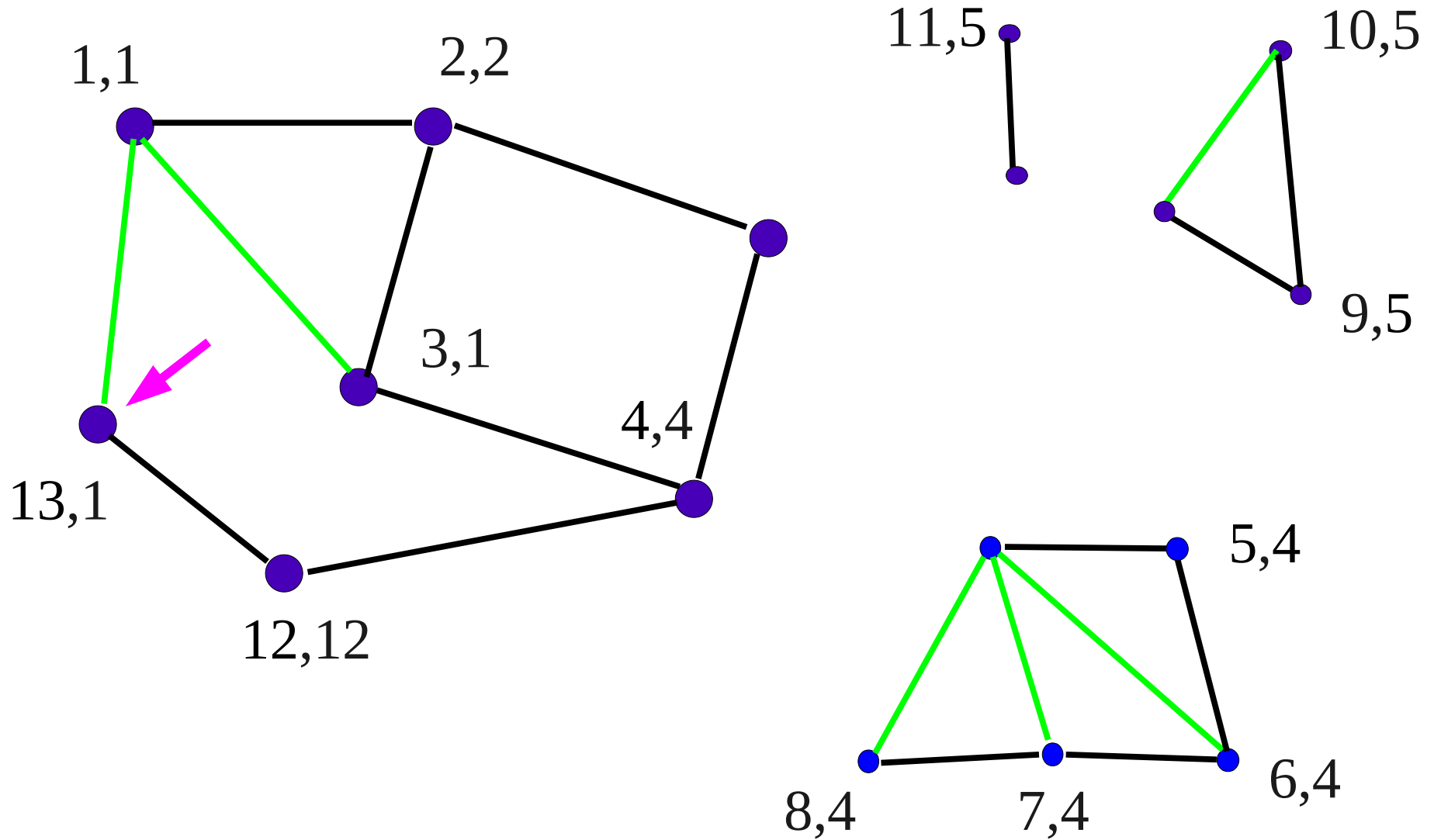
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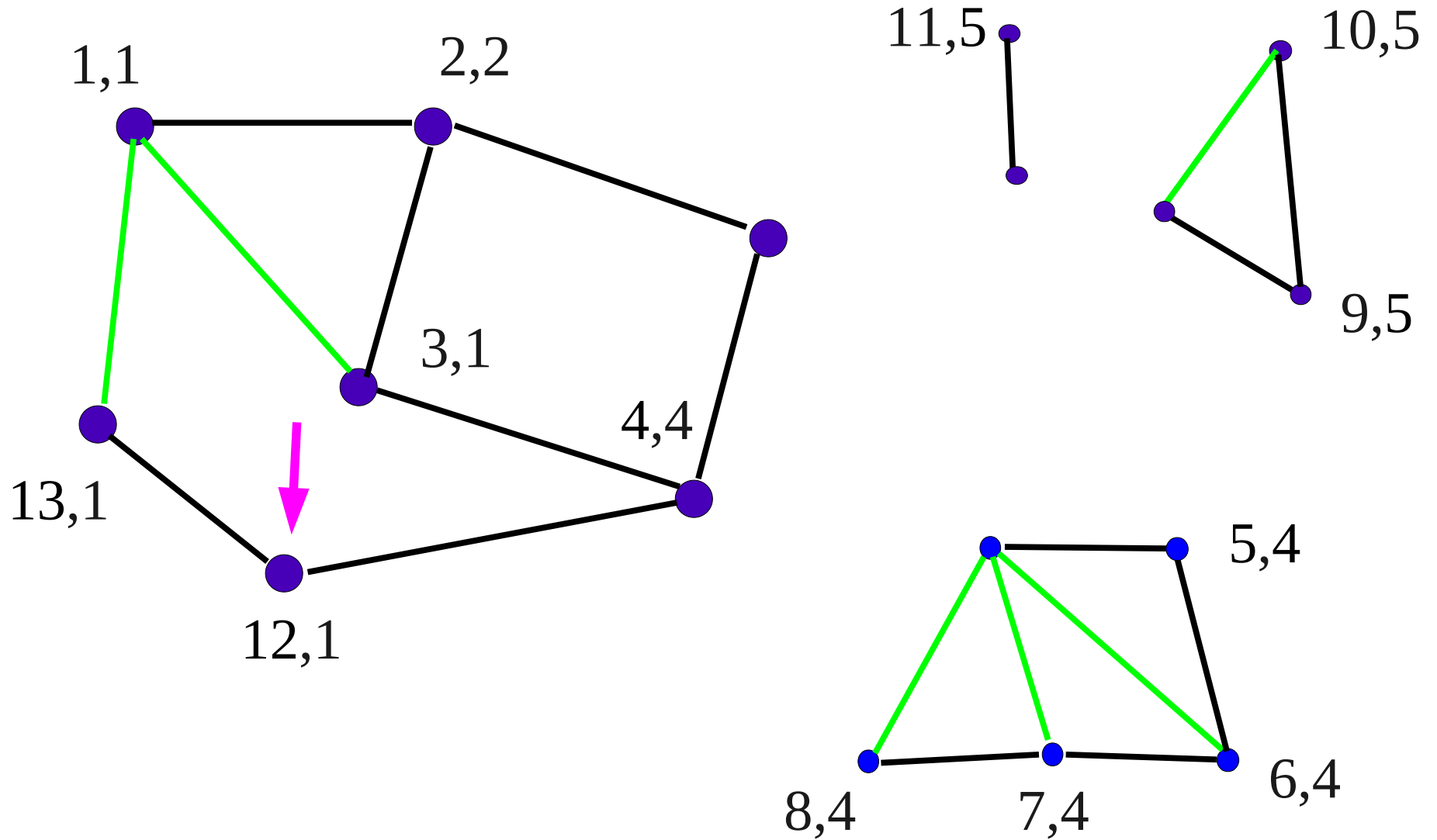
# Biconnected Components



# Biconnected Components



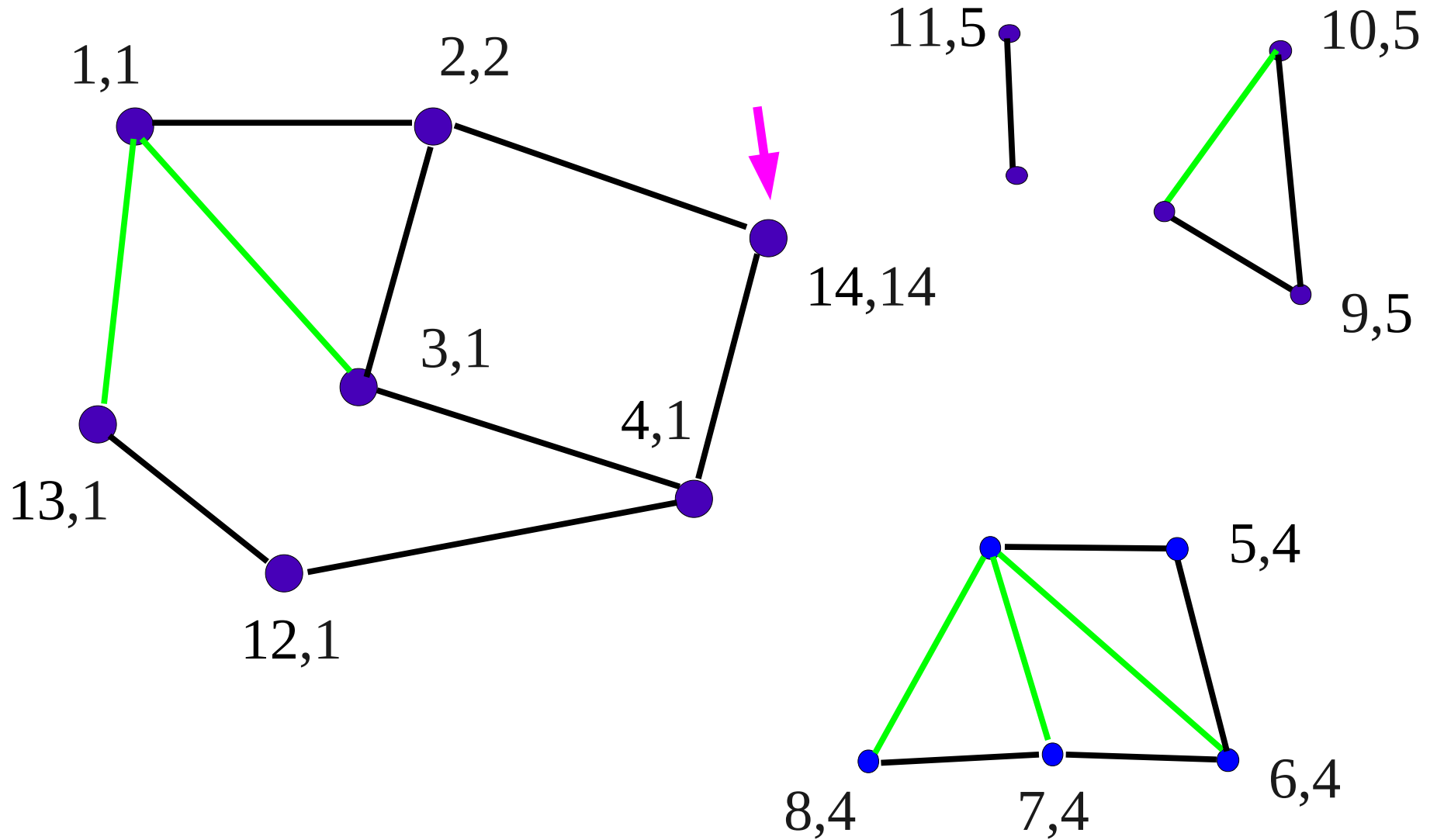
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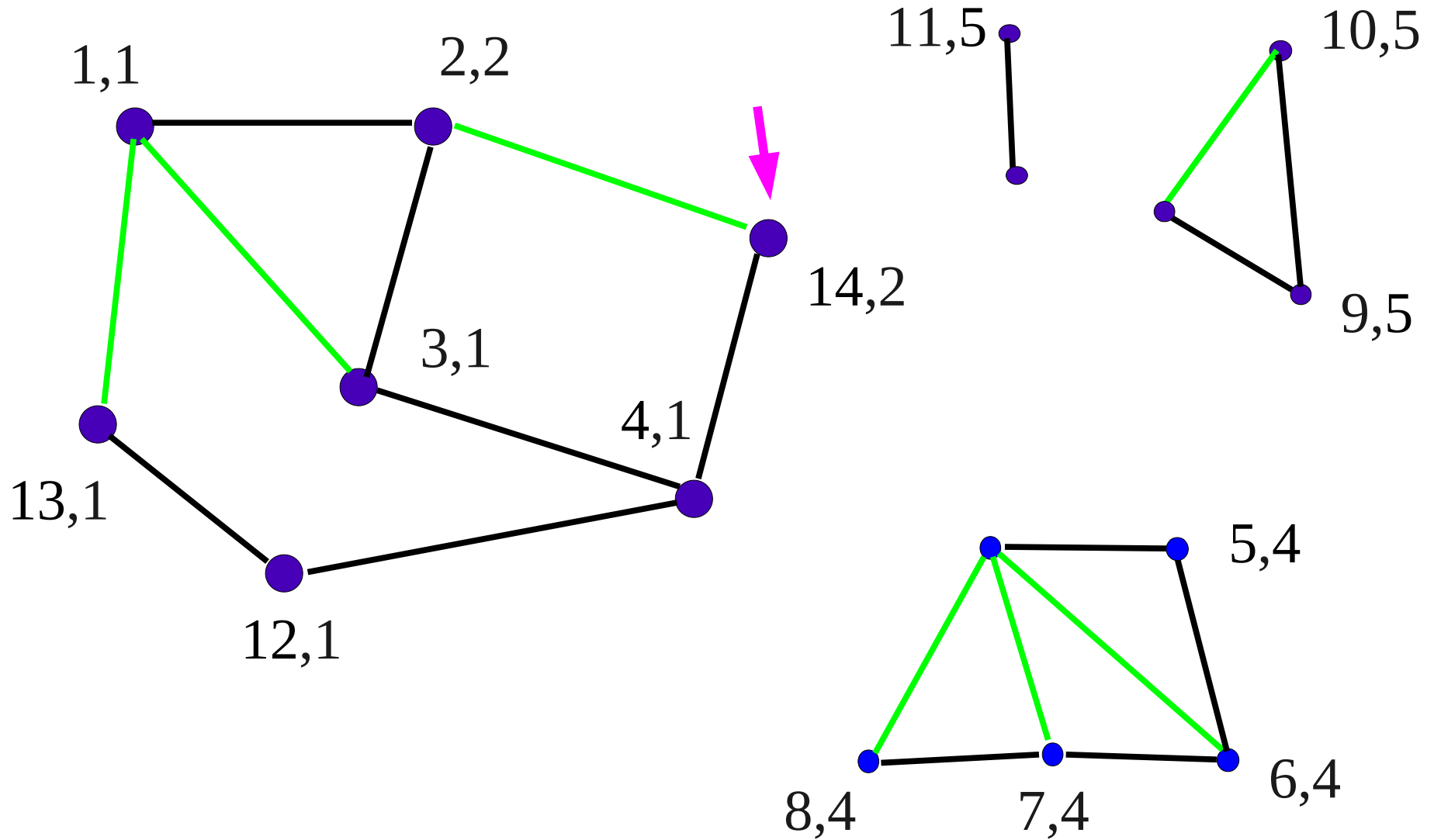




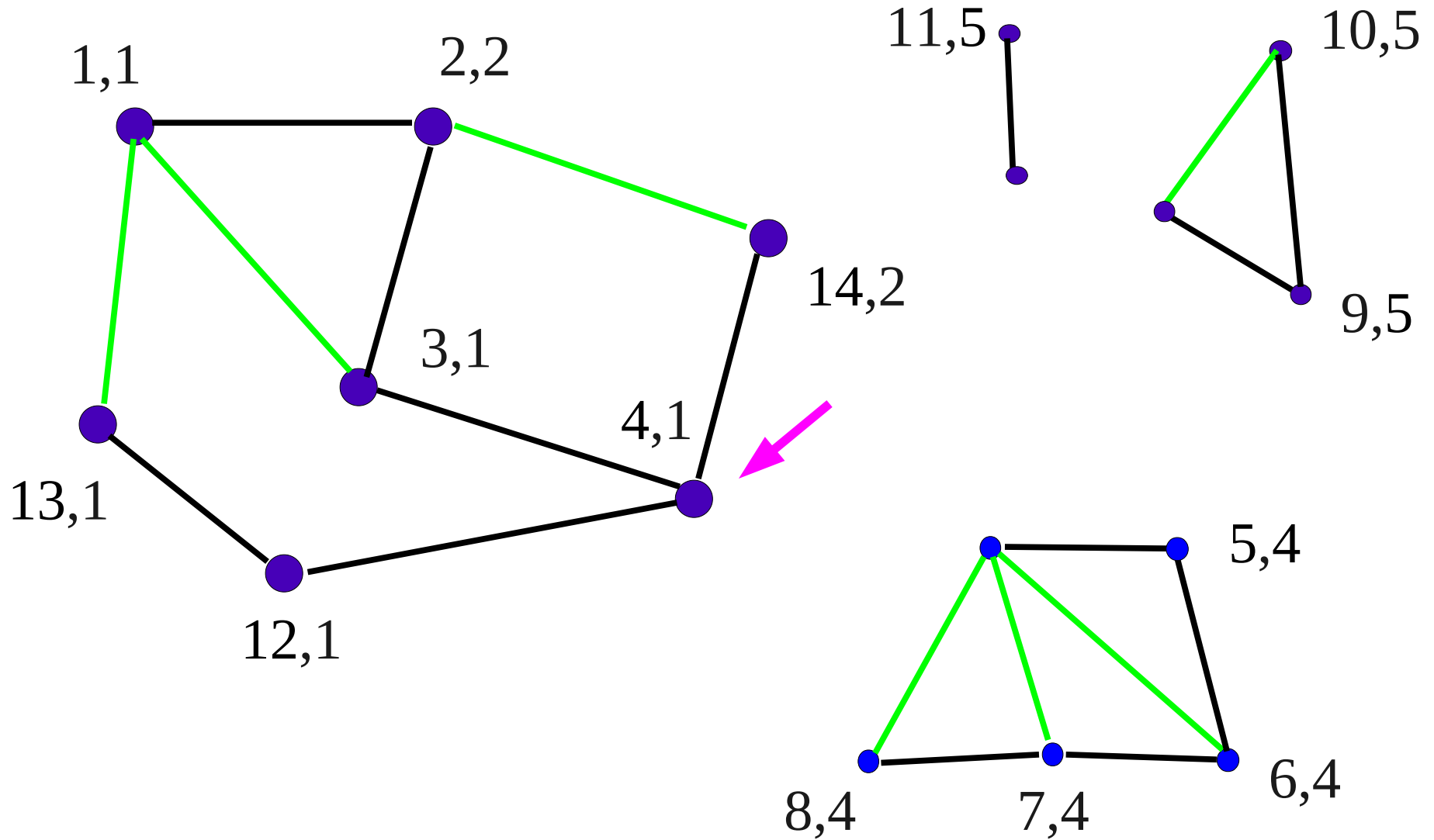
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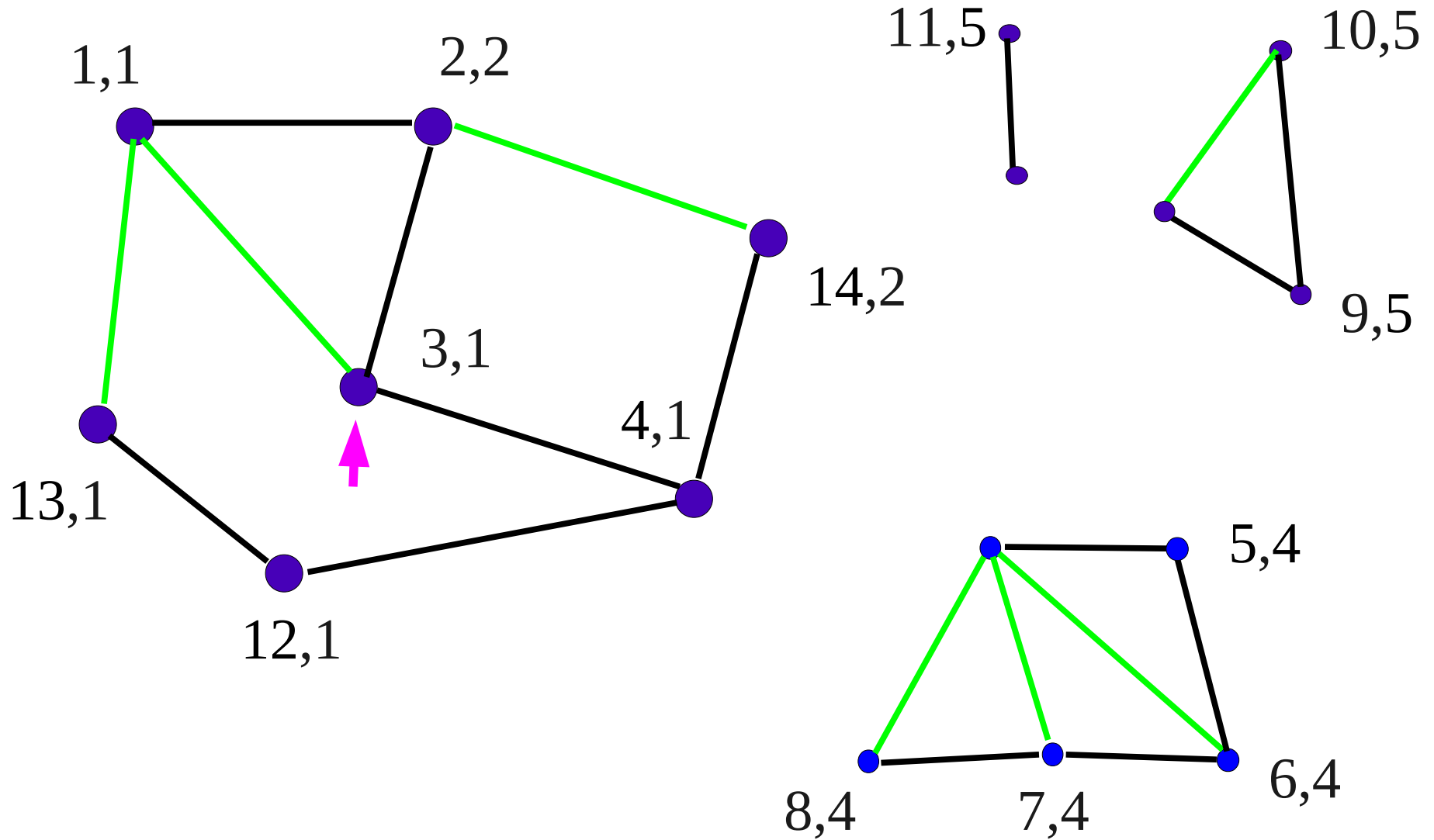
# Biconnected Components



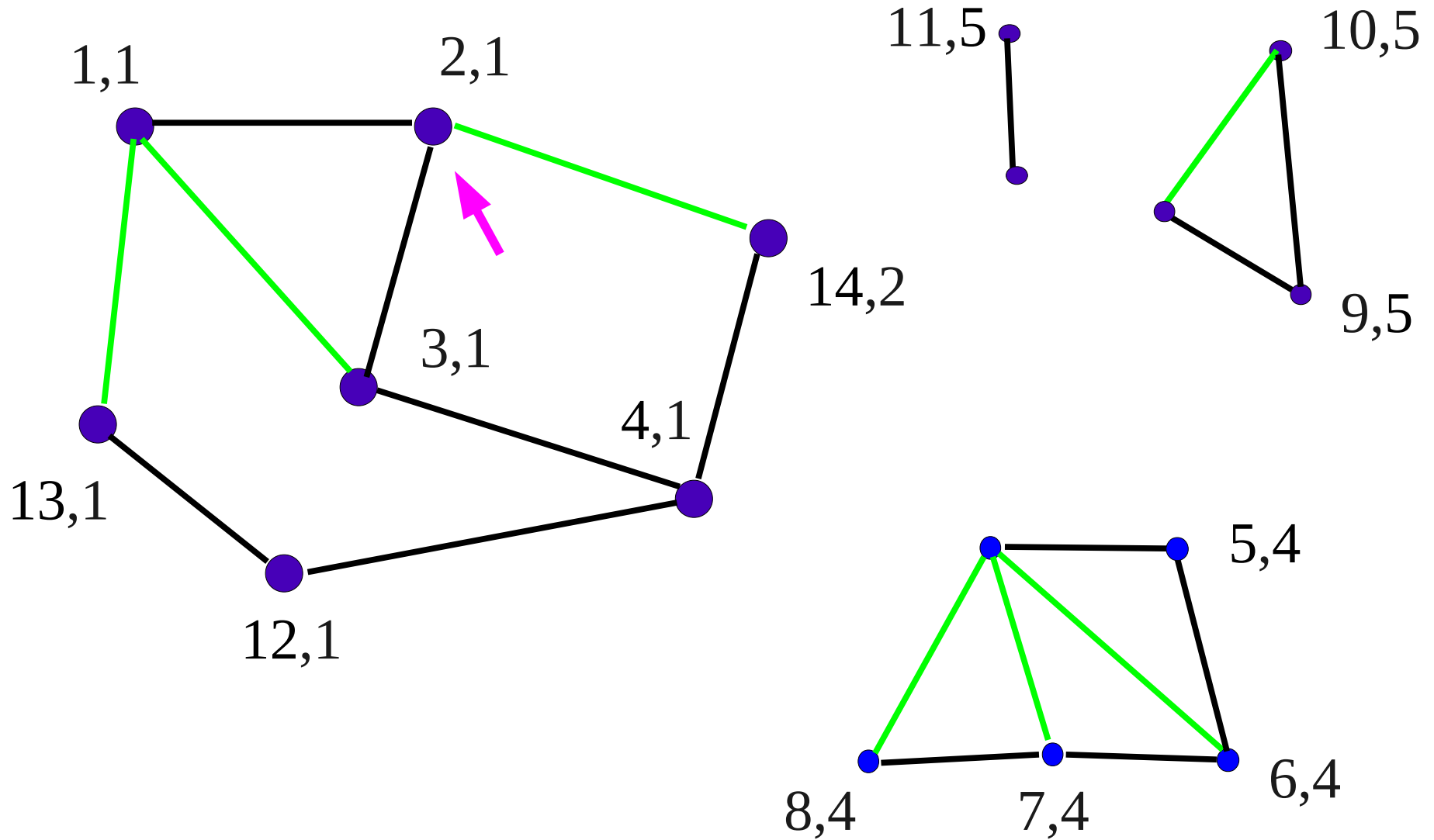
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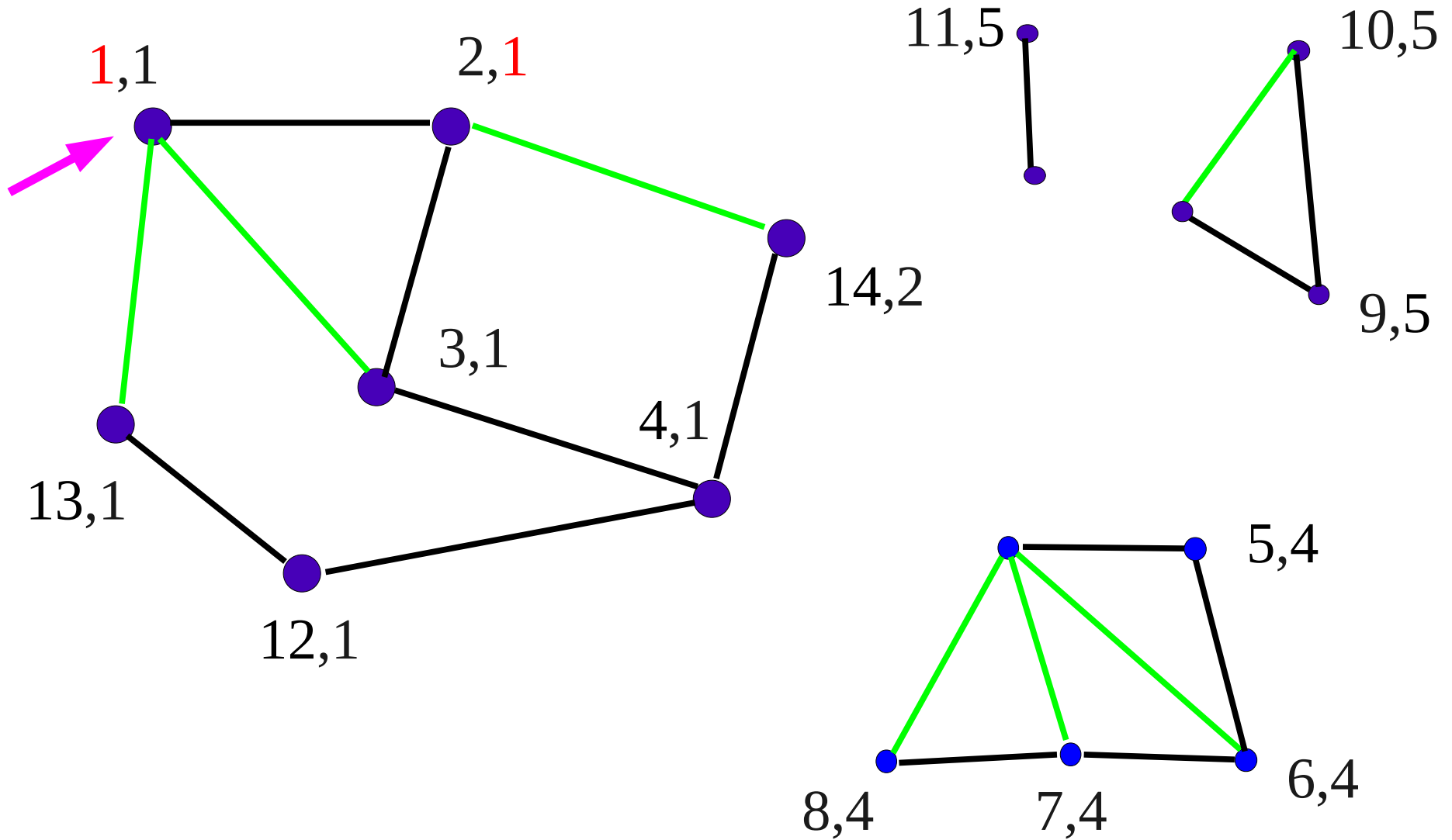
# Biconnected Components



# Biconnected Components



# Biconnected Components



# Biconnected Components

```
BICONN( $V,E$ ) {
  count = 1;
  for all  $v \in V$  mark  $v$  "new";
  while there is a vertex  $v \in V$  marked "new" SEARCH( $v$ );
}

SEARCH( $v$ ) {
  mark  $v$  "old";
  low( $v$ ) = DFnumber( $v$ ) = count++;
  for each vertex  $w \in V$  adjacent to and not the parent of  $v$  {
    if DFnumber( $w$ ) < DFnumber( $v$ ) then push  $\langle v,w \rangle$  onto STACK;
    if  $w$  is marked "new" then {
      SEARCH( $w$ );
      if low( $v$ )  $\geq$  DFnumber( $v$ ) then pop from STACK all edges to  $\langle v,w \rangle$ ;
      low( $v$ ) = min{low( $v$ ),low( $w$ )};
    } else {
      low( $v$ ) = min{low( $v$ ), DFnumber( $w$ )}
    }
  }
}
```