

Radix Sort

Radix Sort

45834

6283

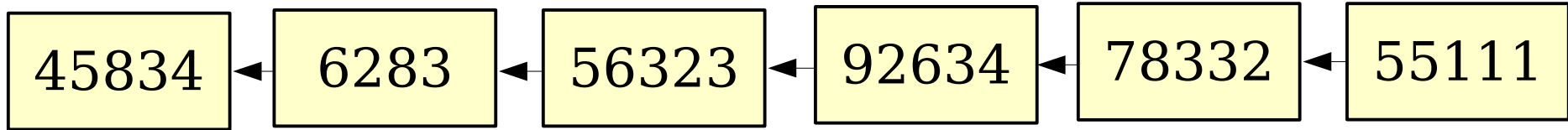
56323

92634

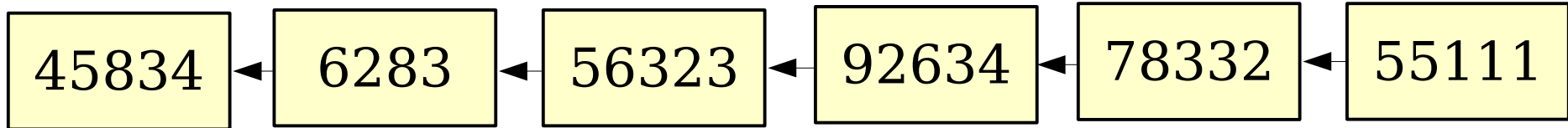
78332

55111

Radix Sort



Radix Sort



0:

1:

2:

3:

4:

5:

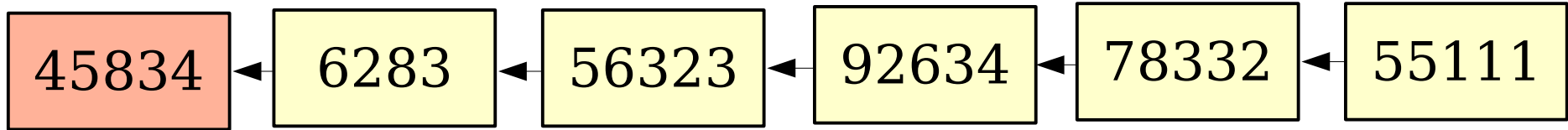
6:

7:

8:

9:

Radix Sort



0:

1:

2:

3:

4:

5:

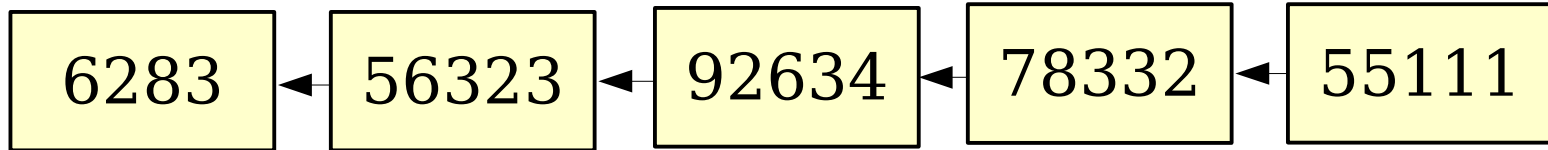
6:

7:

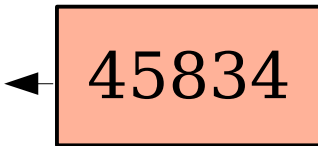
8:

9:

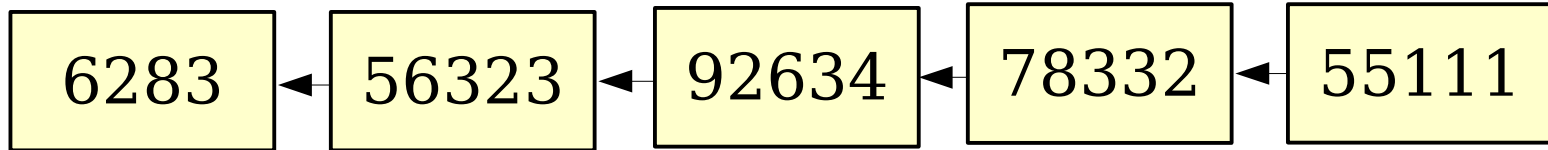
Radix Sort



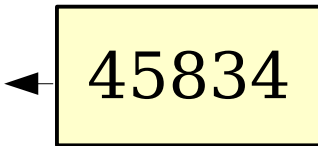
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



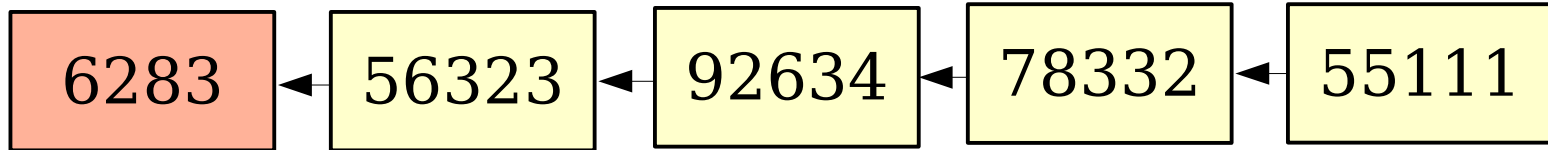
Radix Sort



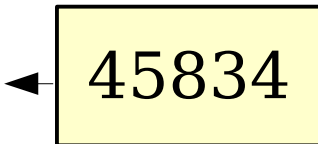
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



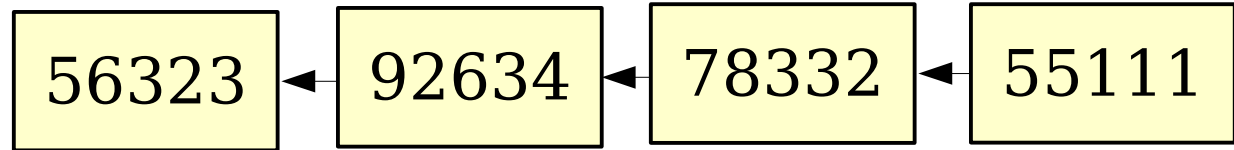
Radix Sort



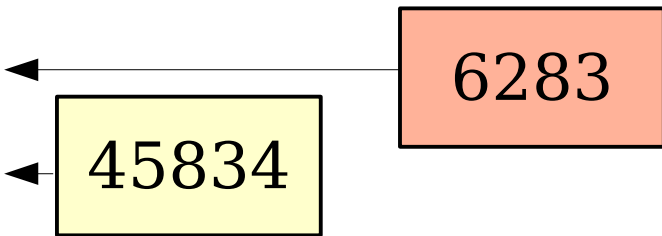
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



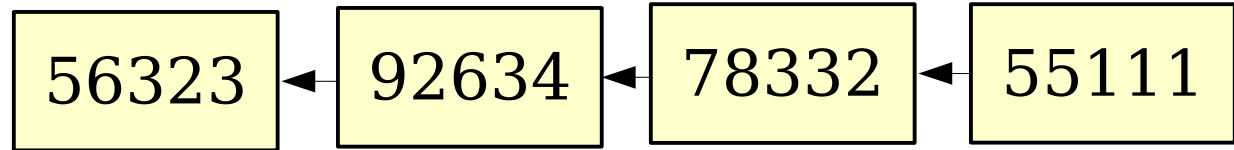
Radix Sort



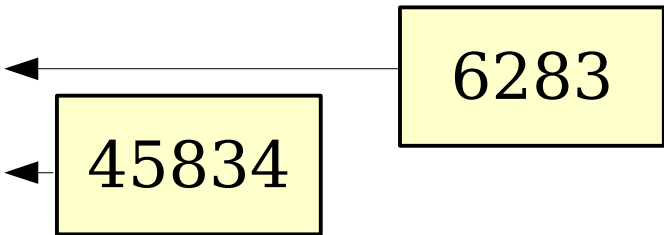
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



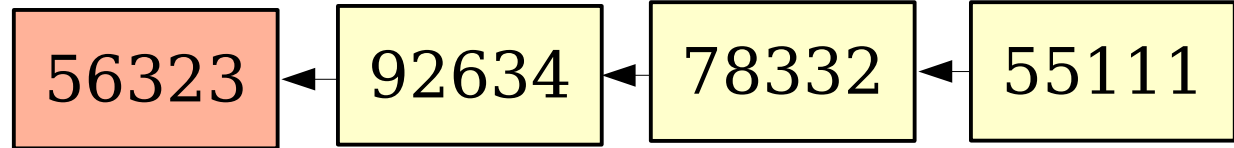
Radix Sort



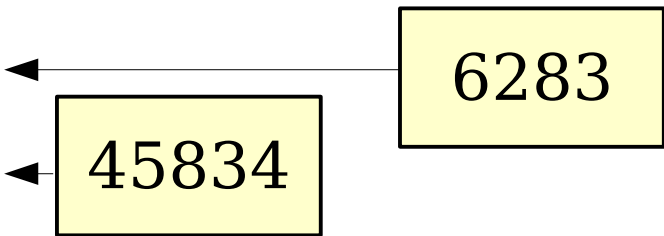
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



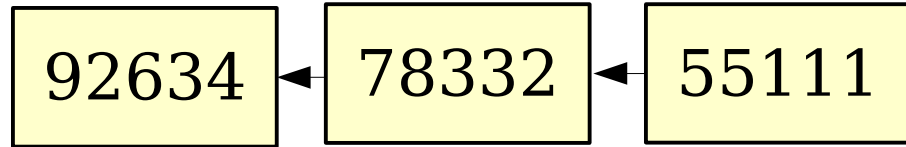
Radix Sort



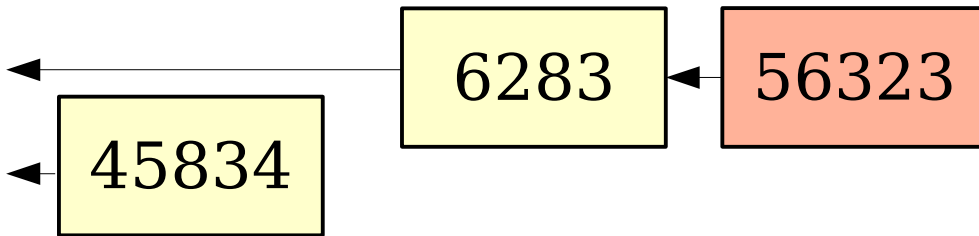
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



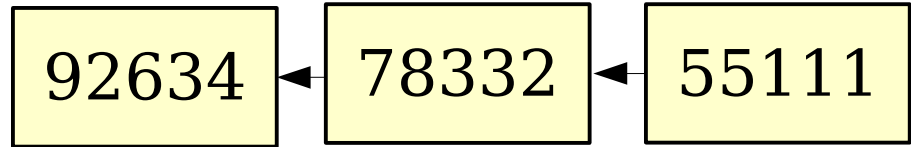
Radix Sort



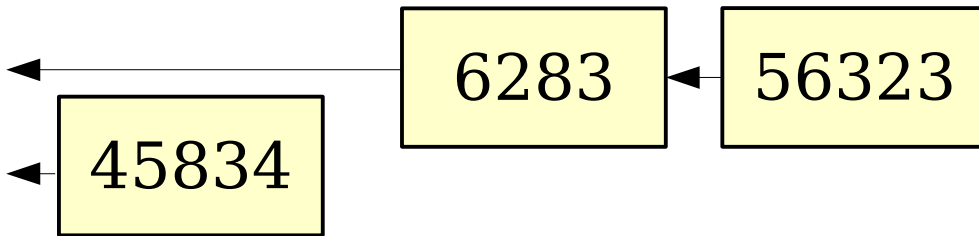
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



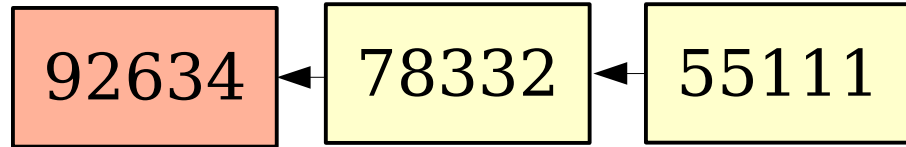
Radix Sort



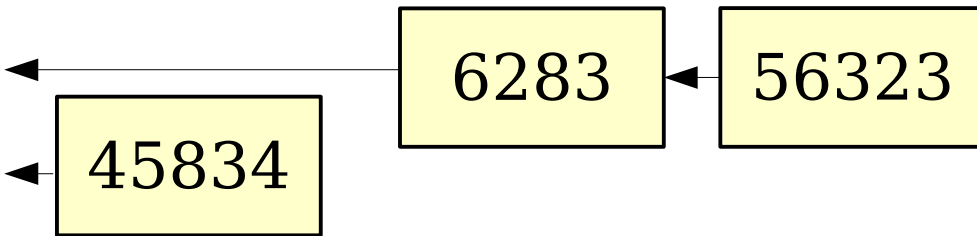
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



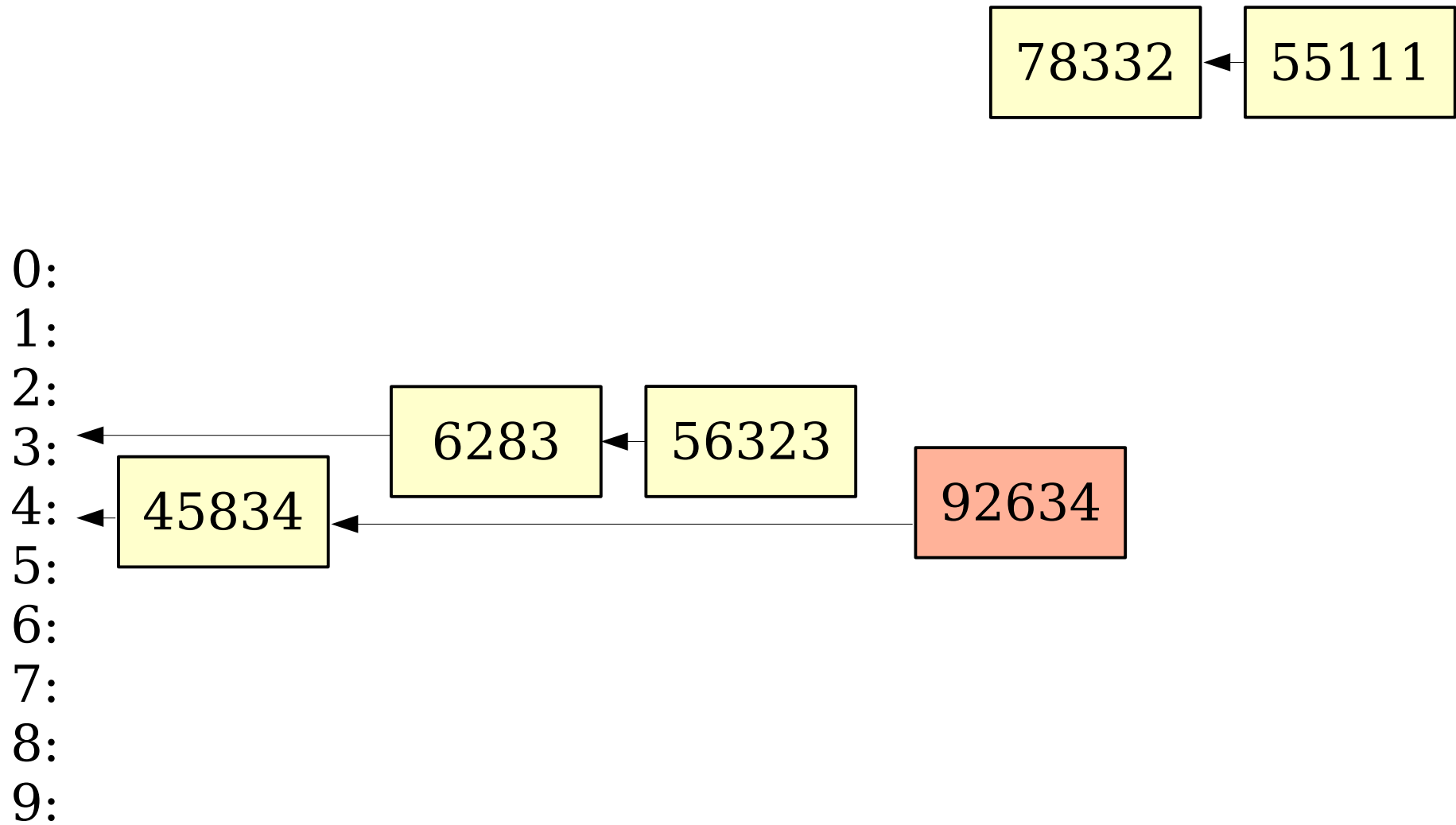
Radix Sort



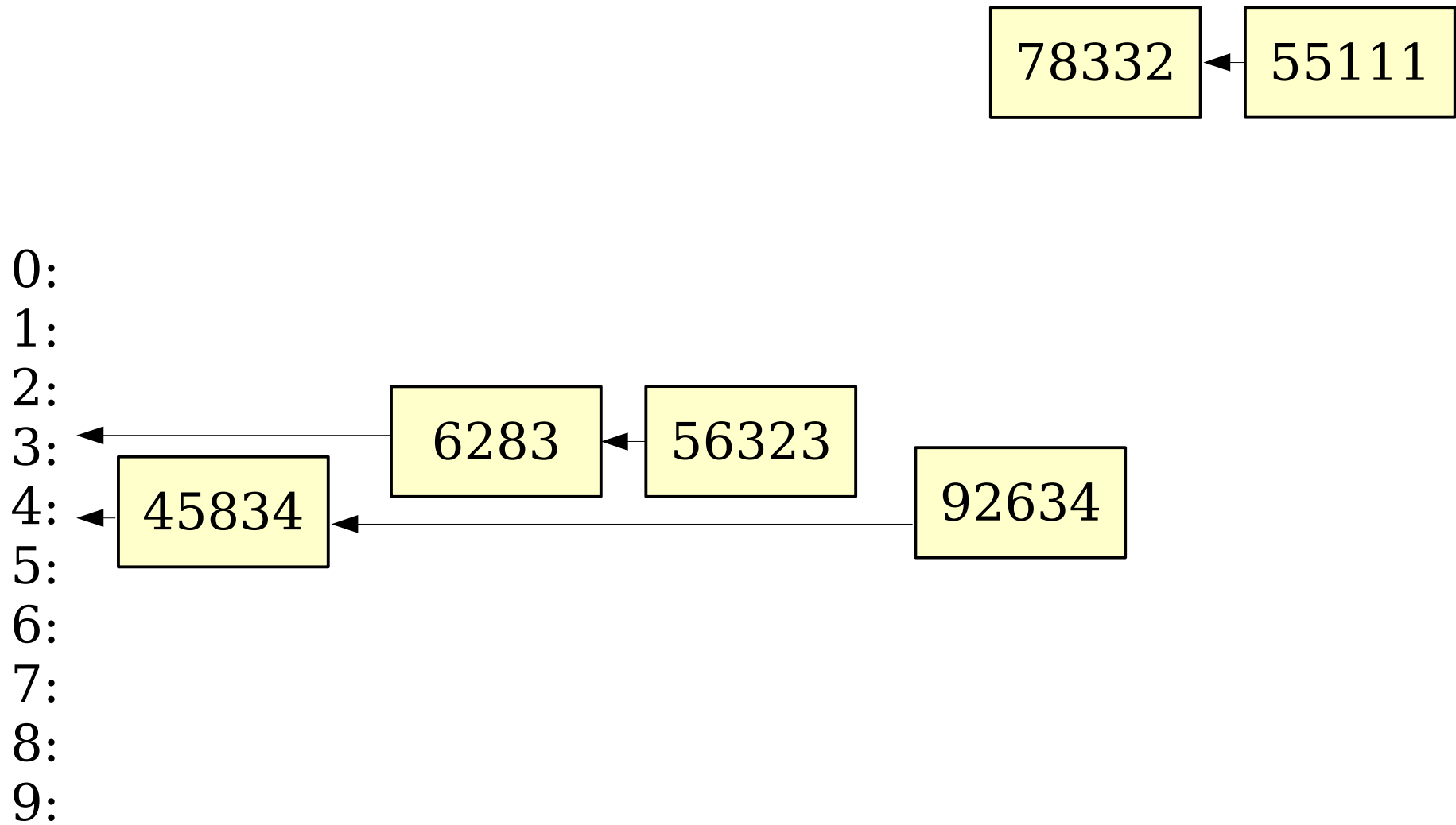
0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



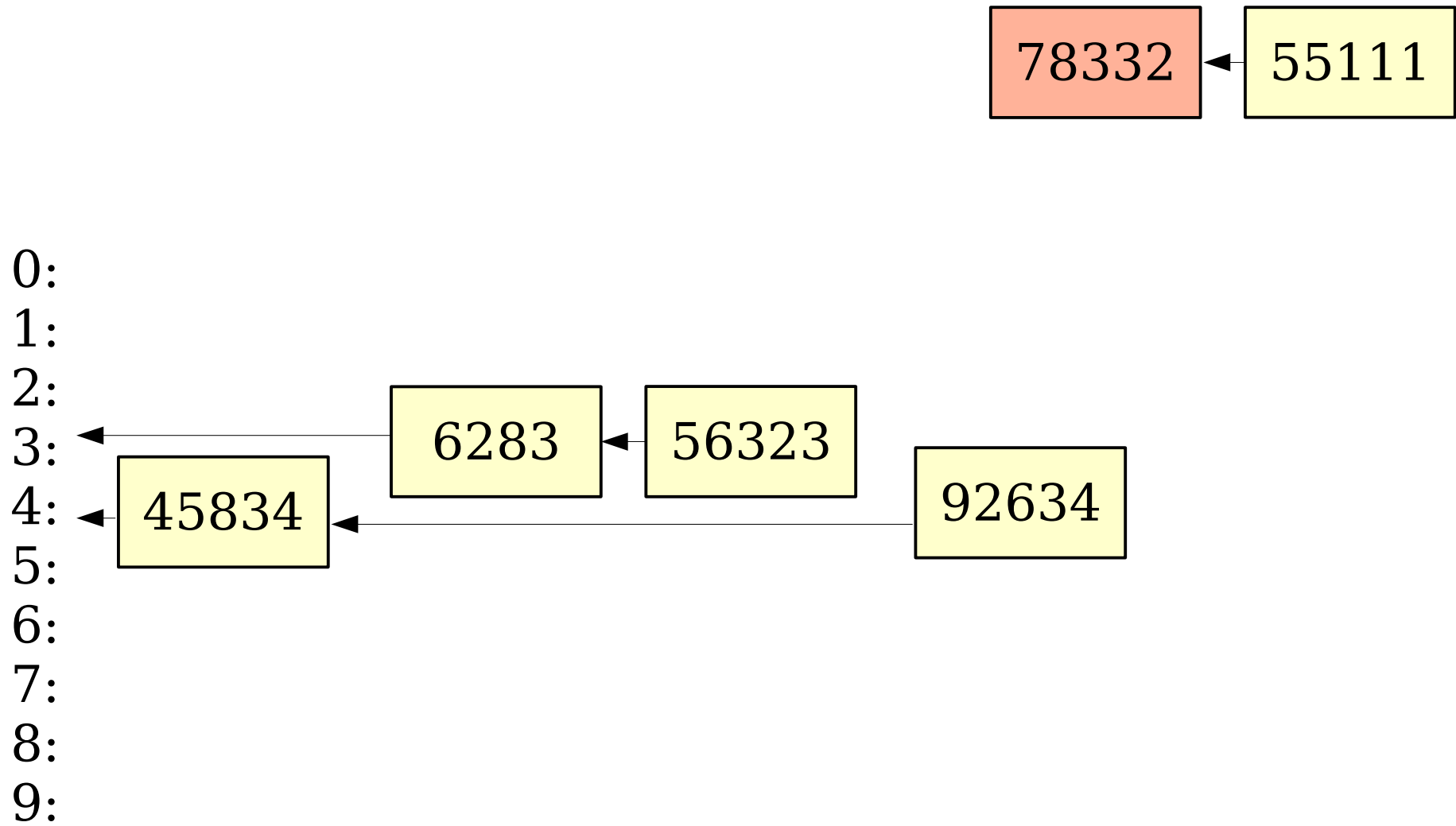
Radix Sort



Radix Sort

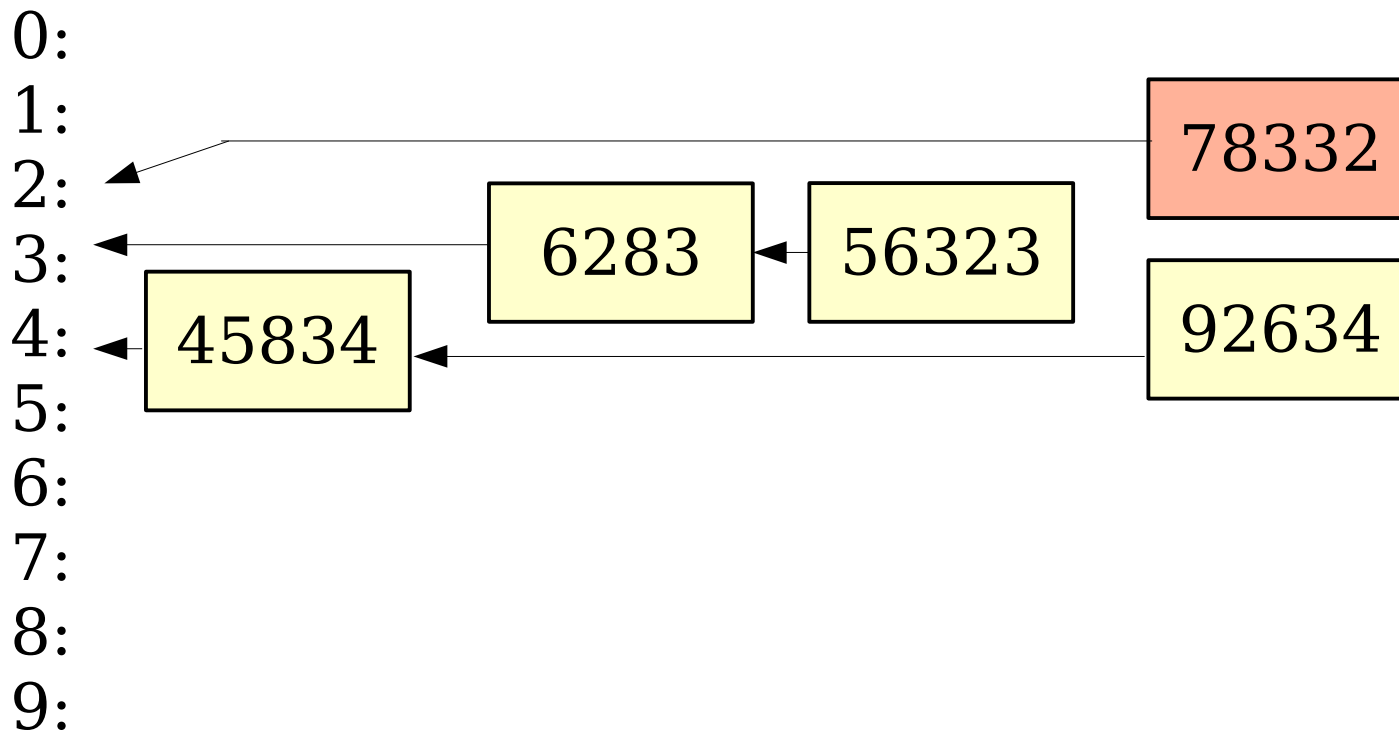


Radix Sort



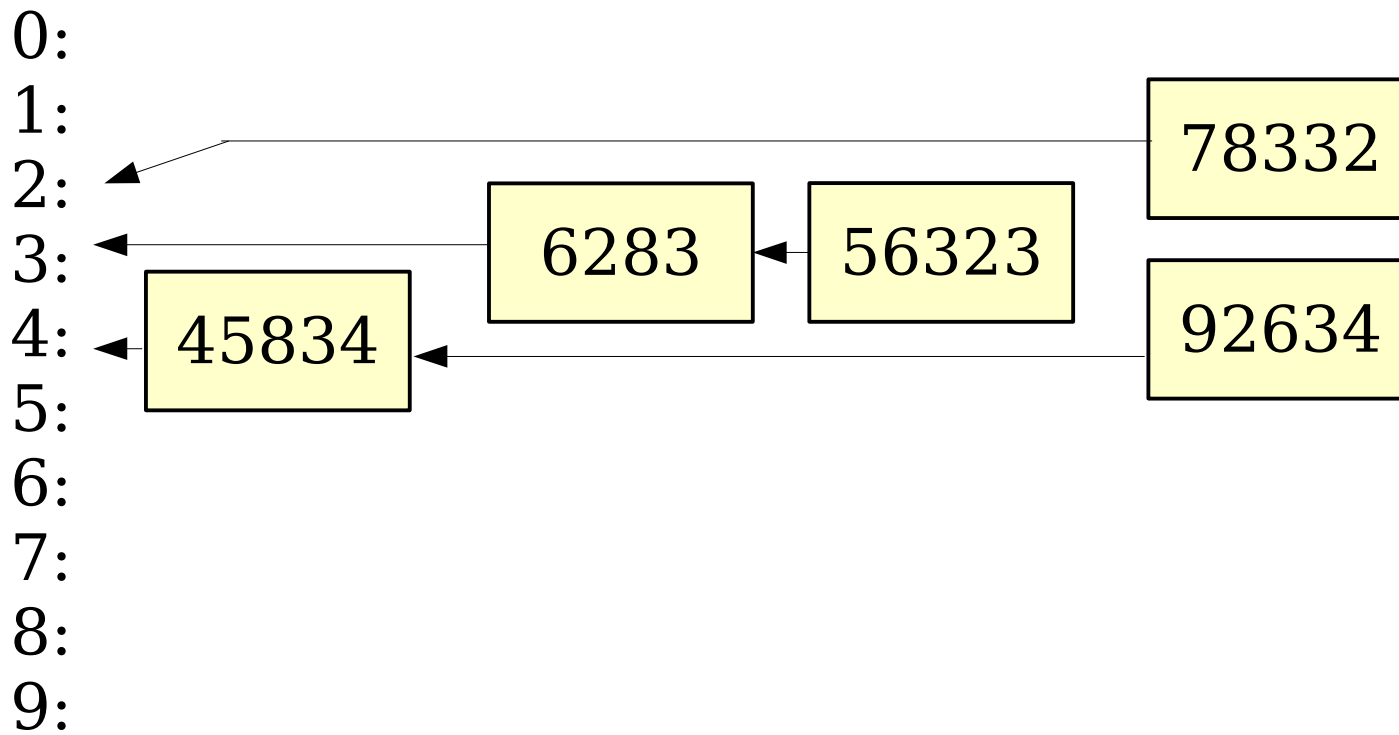
Radix Sort

55111



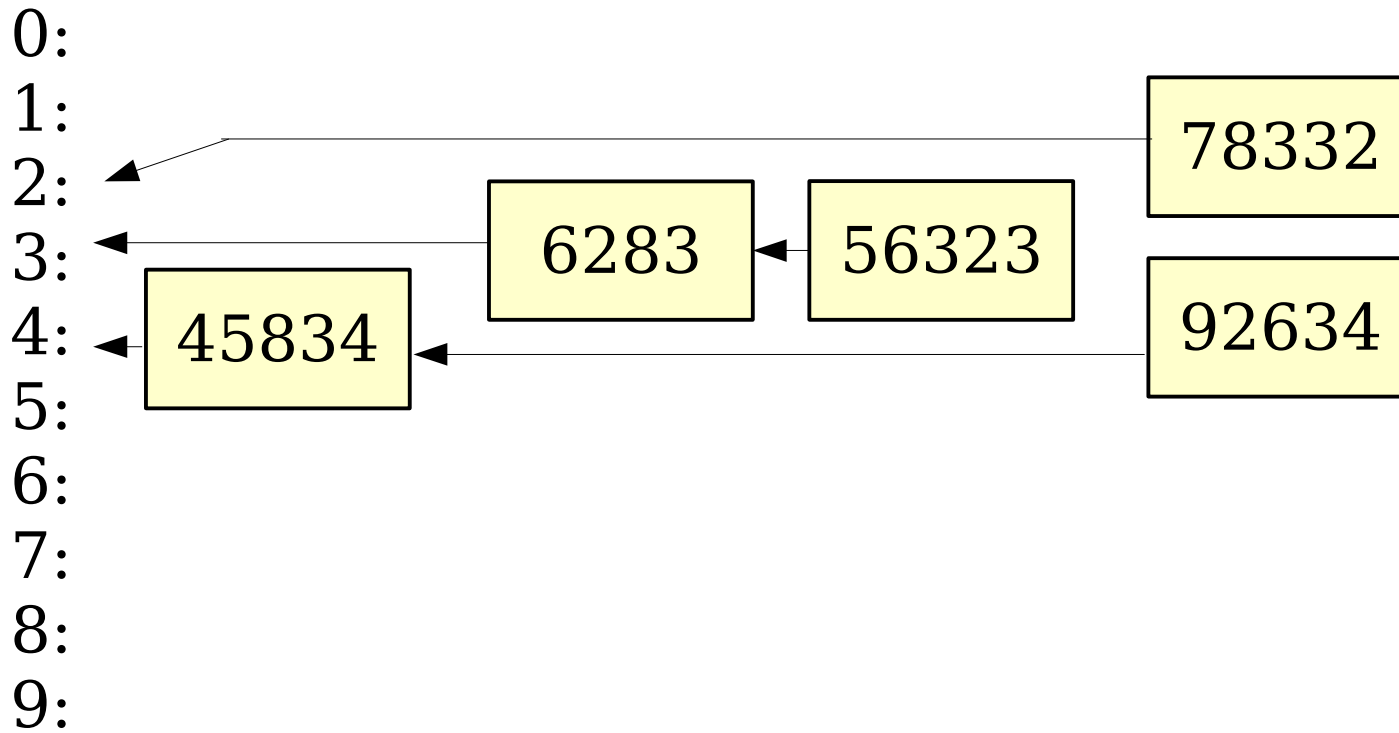
Radix Sort

55111

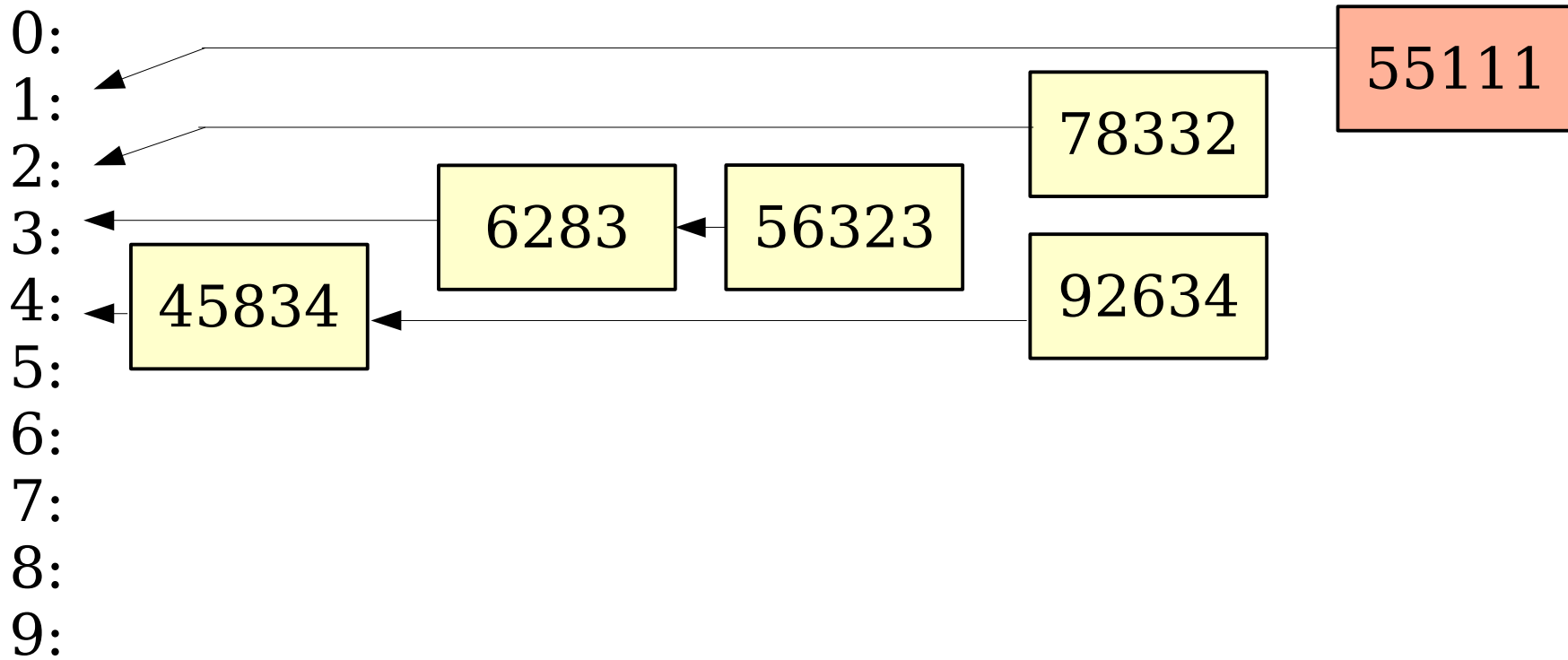


Radix Sort

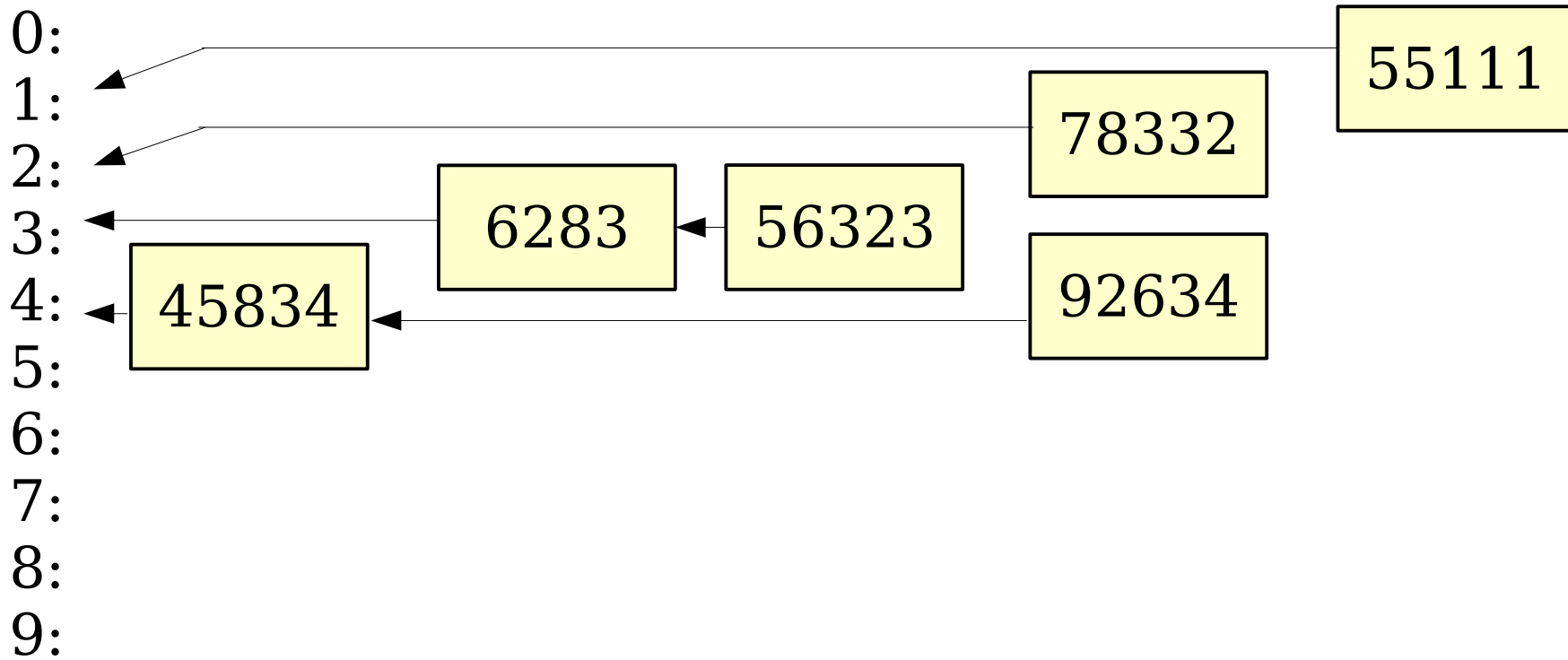
55111



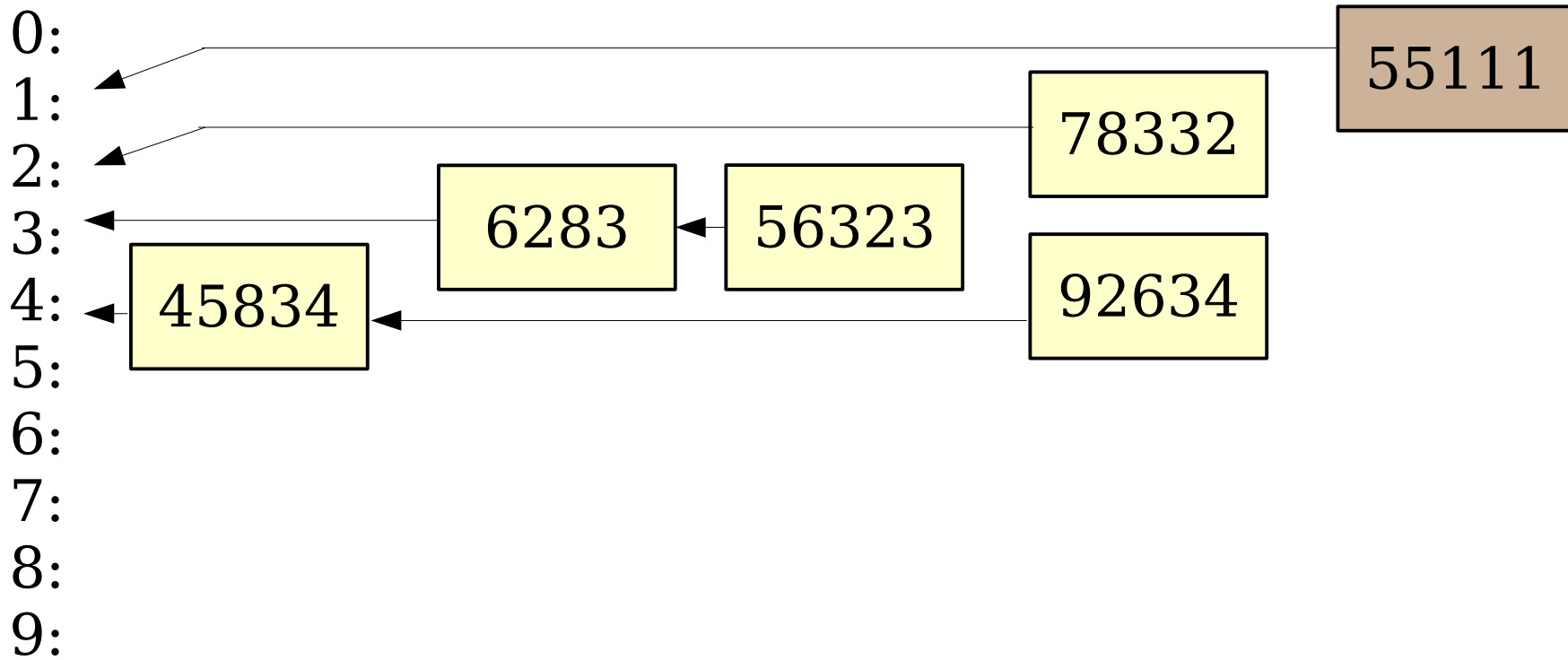
Radix Sort



Radix Sort

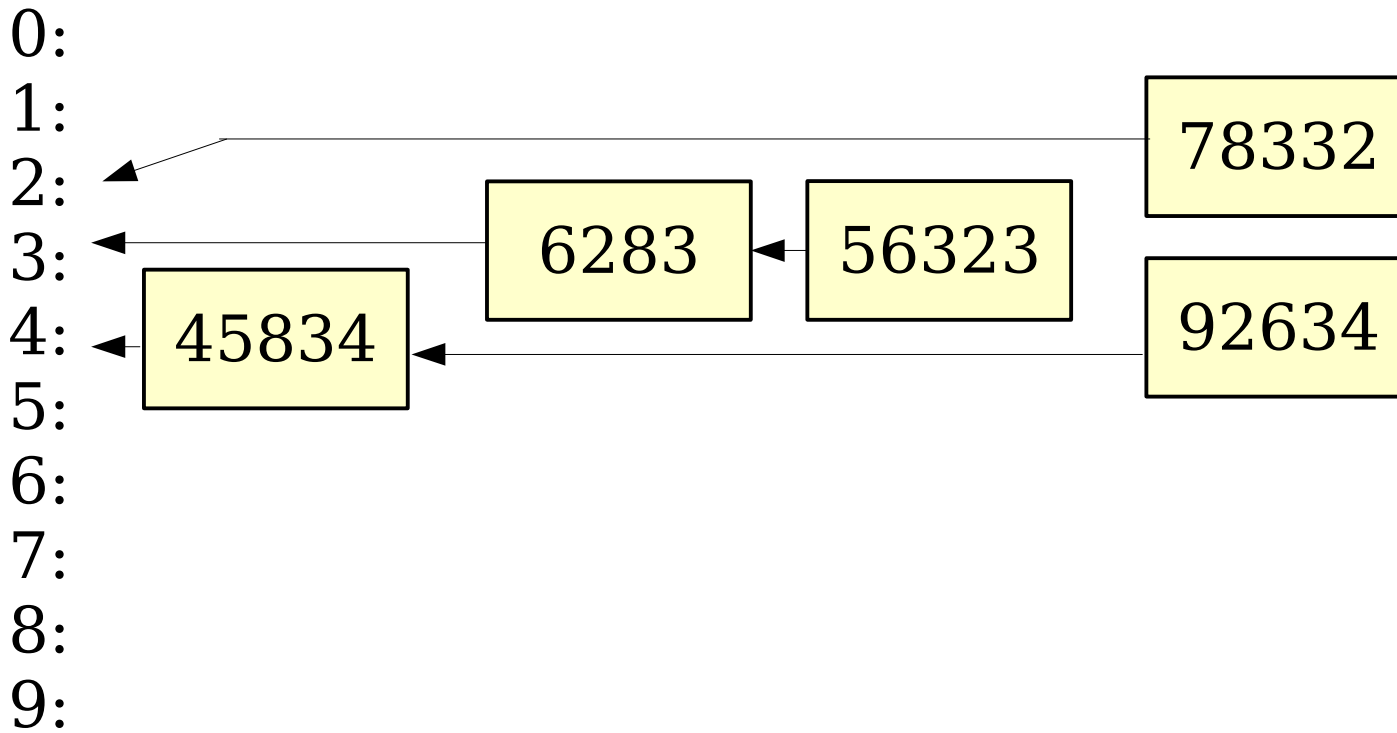


Radix Sort



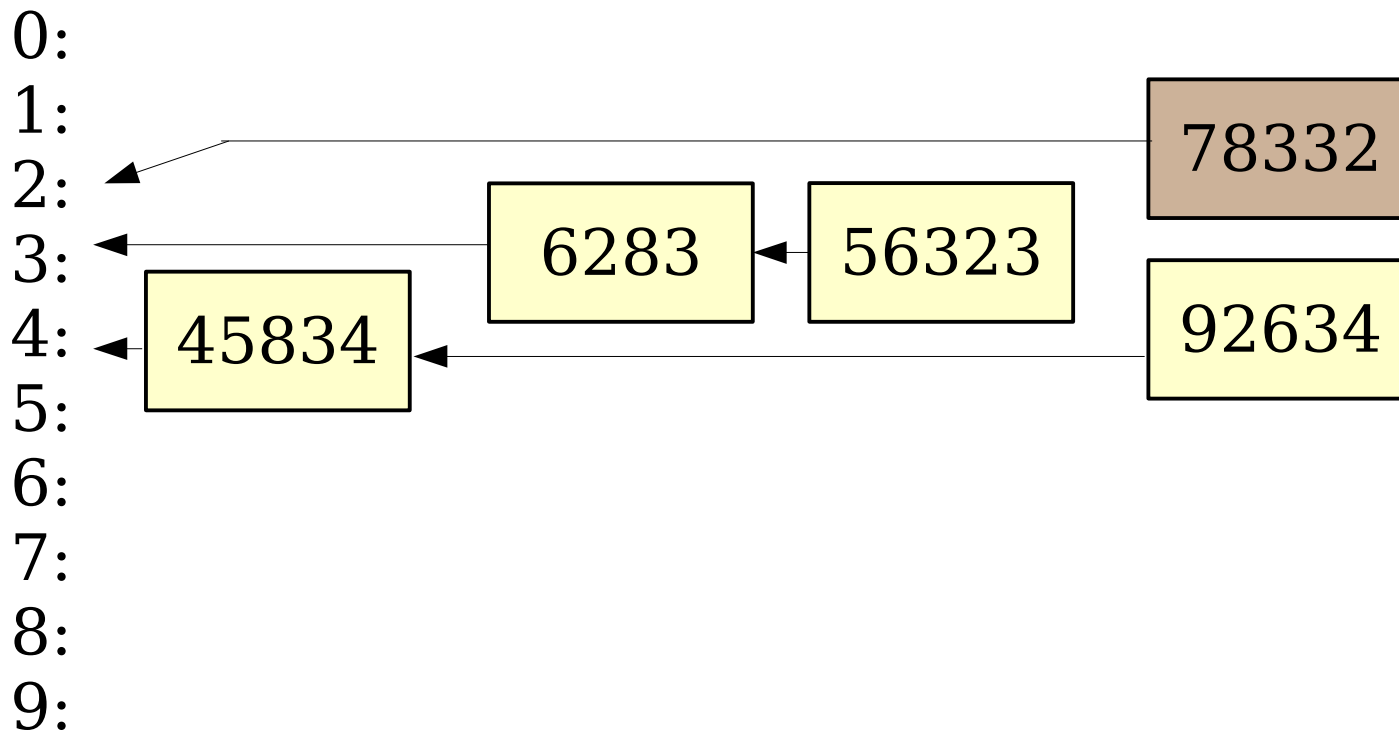
Radix Sort

55111

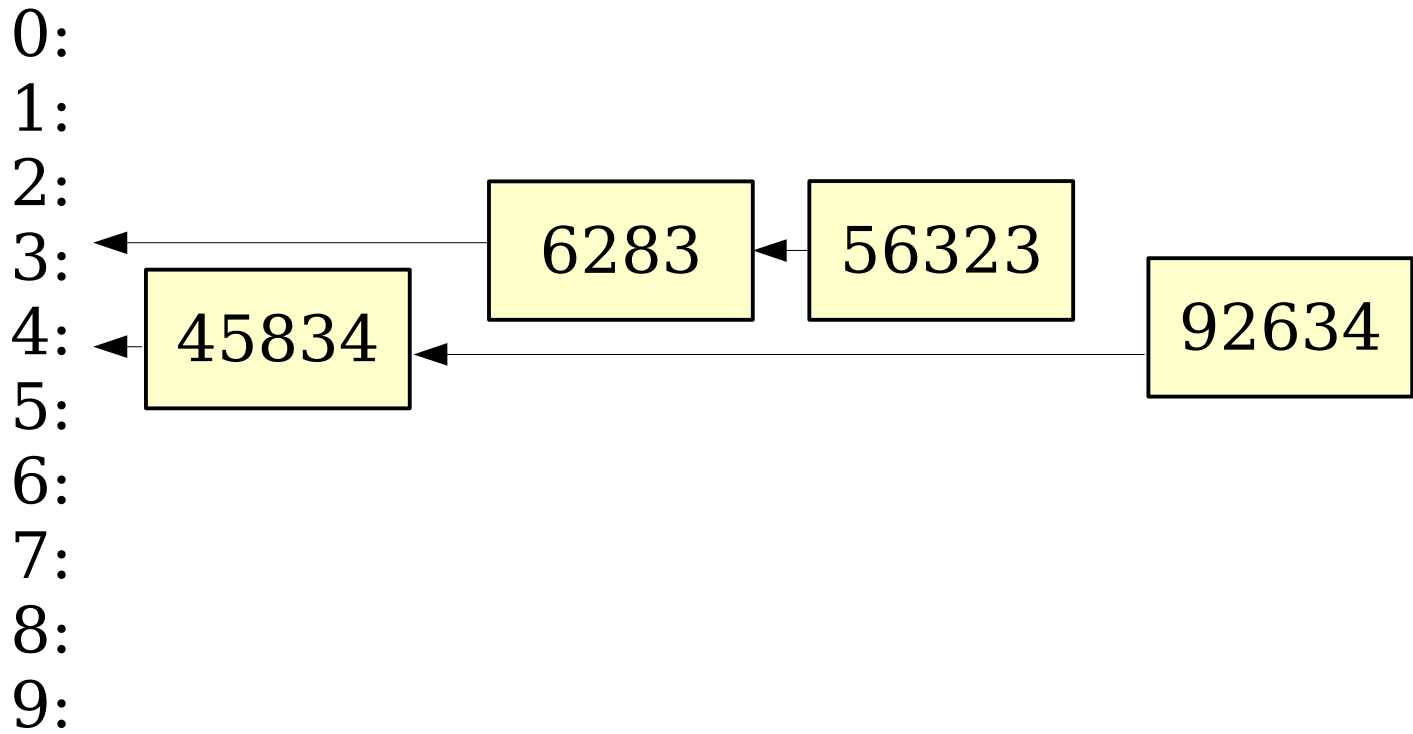
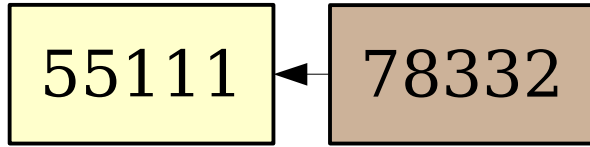


Radix Sort

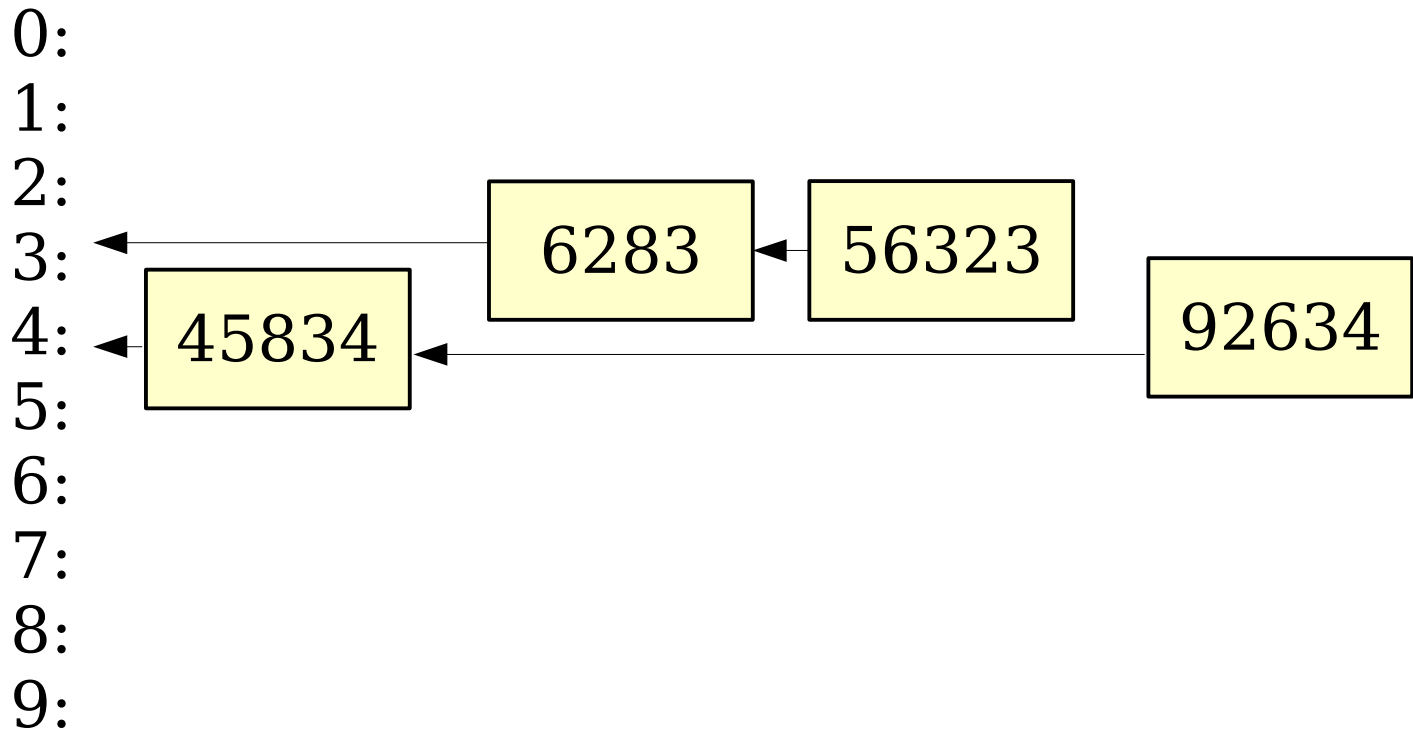
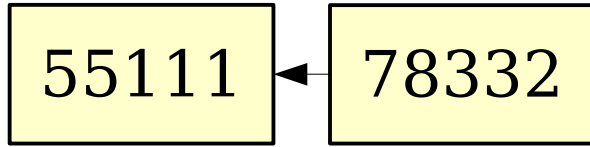
55111



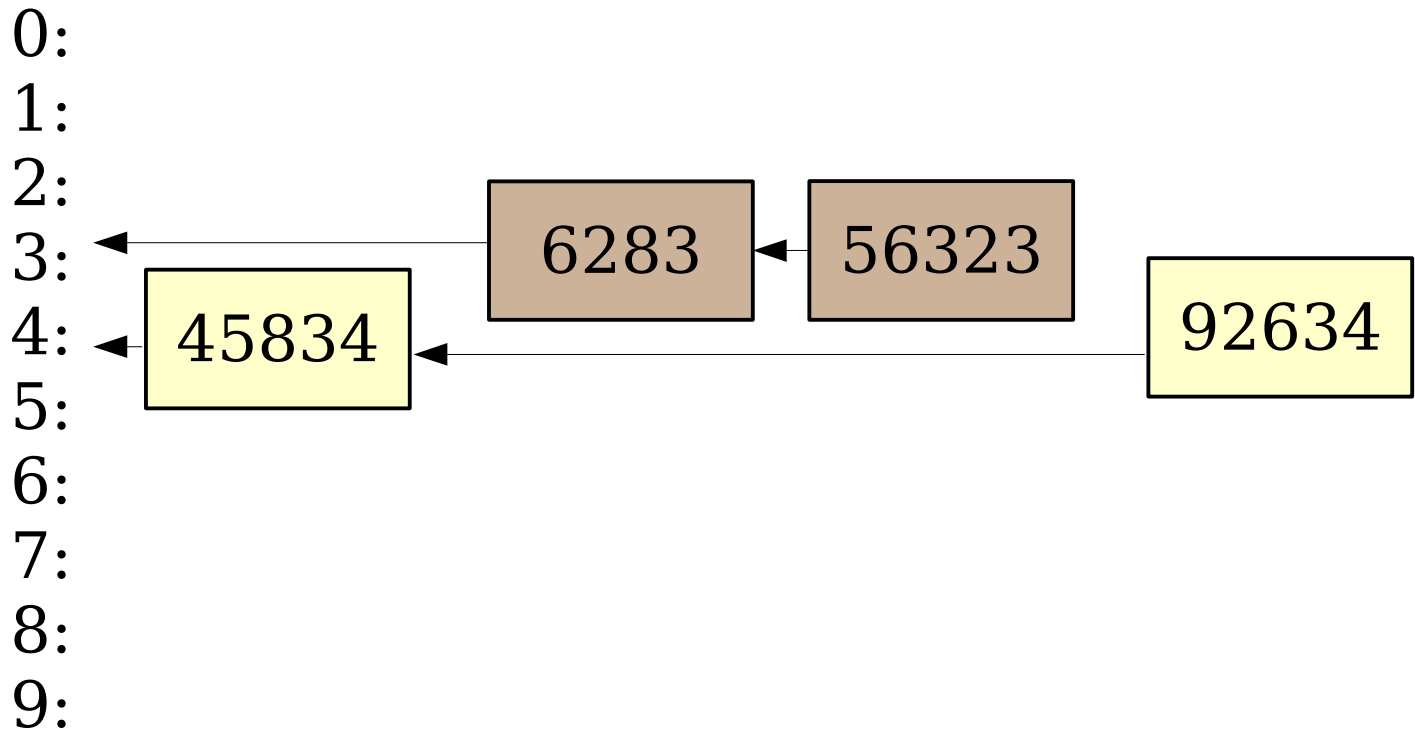
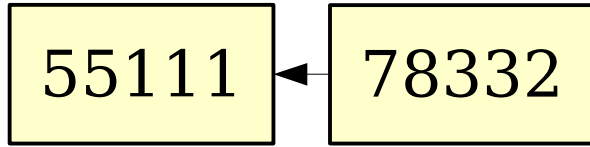
Radix Sort



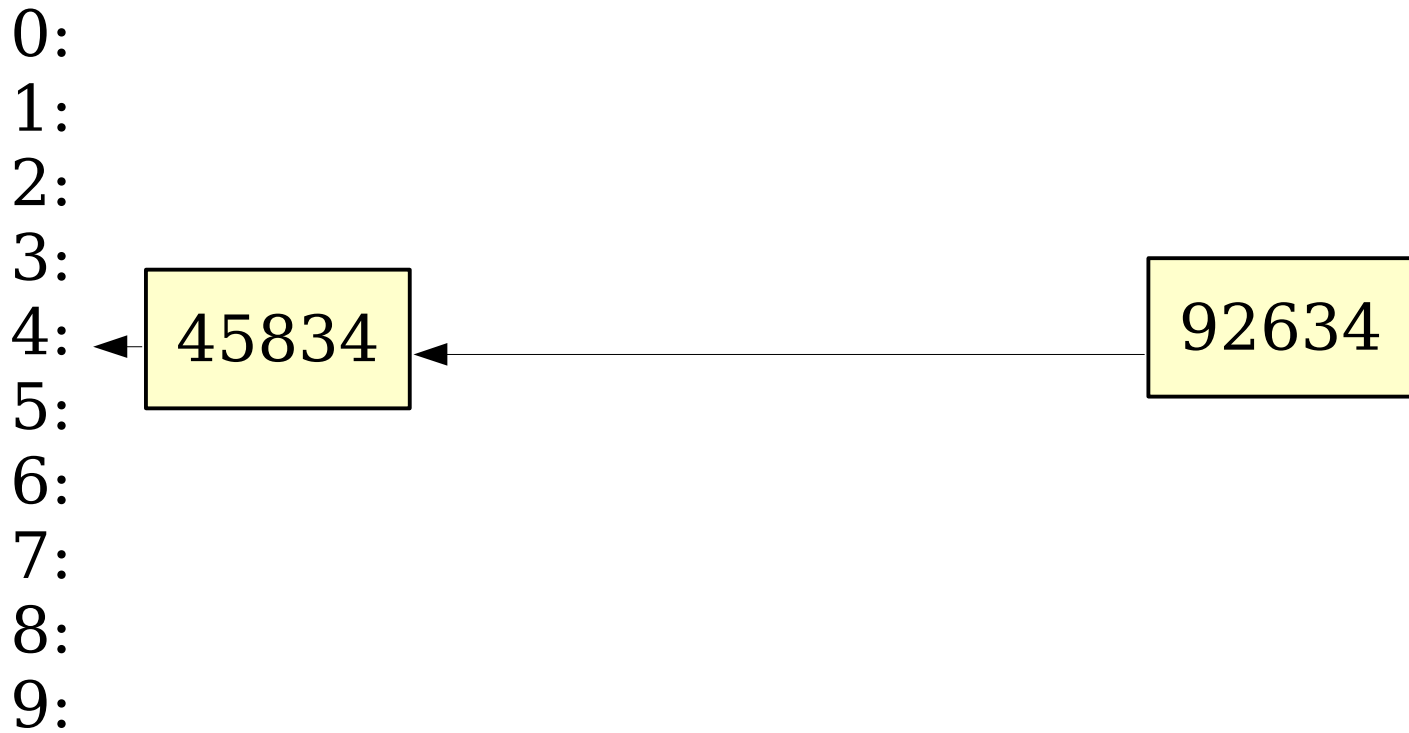
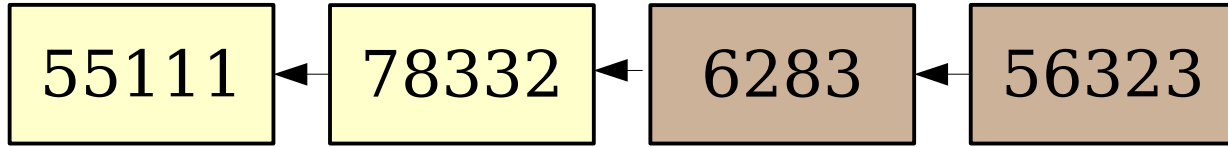
Radix Sort



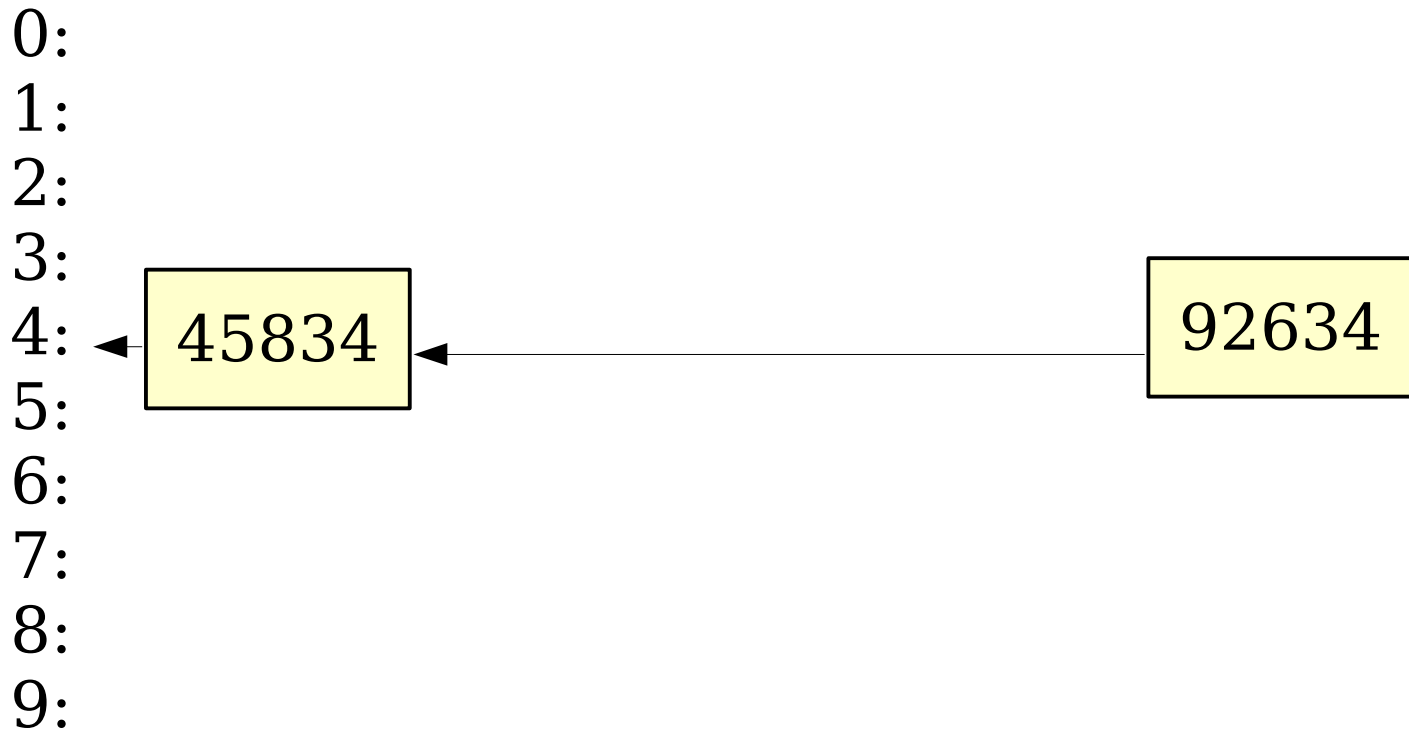
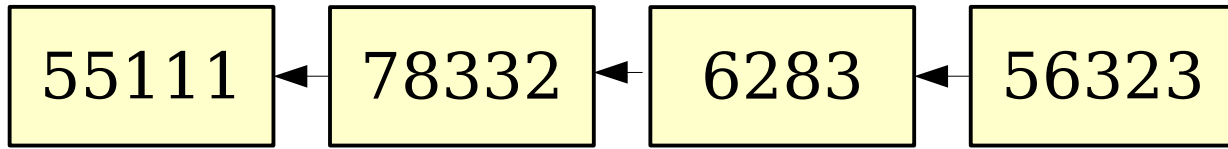
Radix Sort



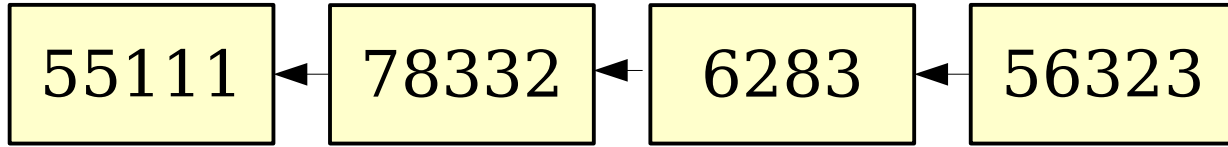
Radix Sort



Radix Sort



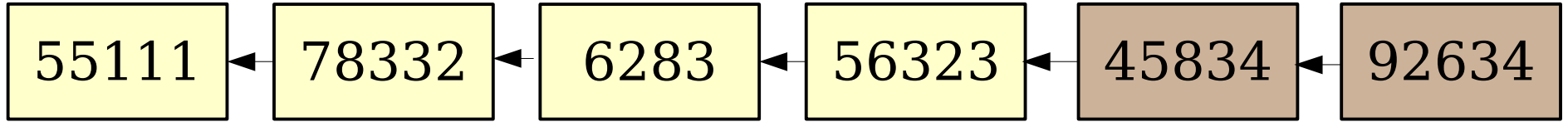
Radix Sort



0:
1:
2:
3:
4:
5:
6:
7:
8:
9:



Radix Sort



0:

1:

2:

3:

4:

5:

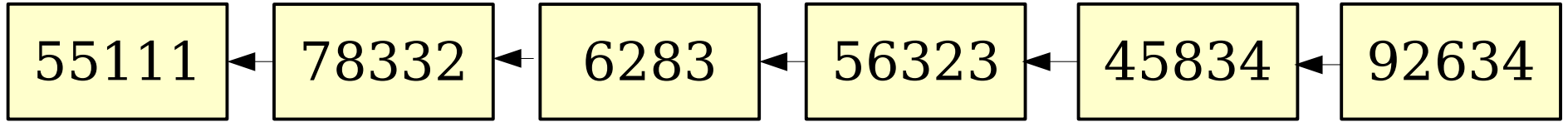
6:

7:

8:

9:

Radix Sort



0:

1:

2:

3:

4:

5:

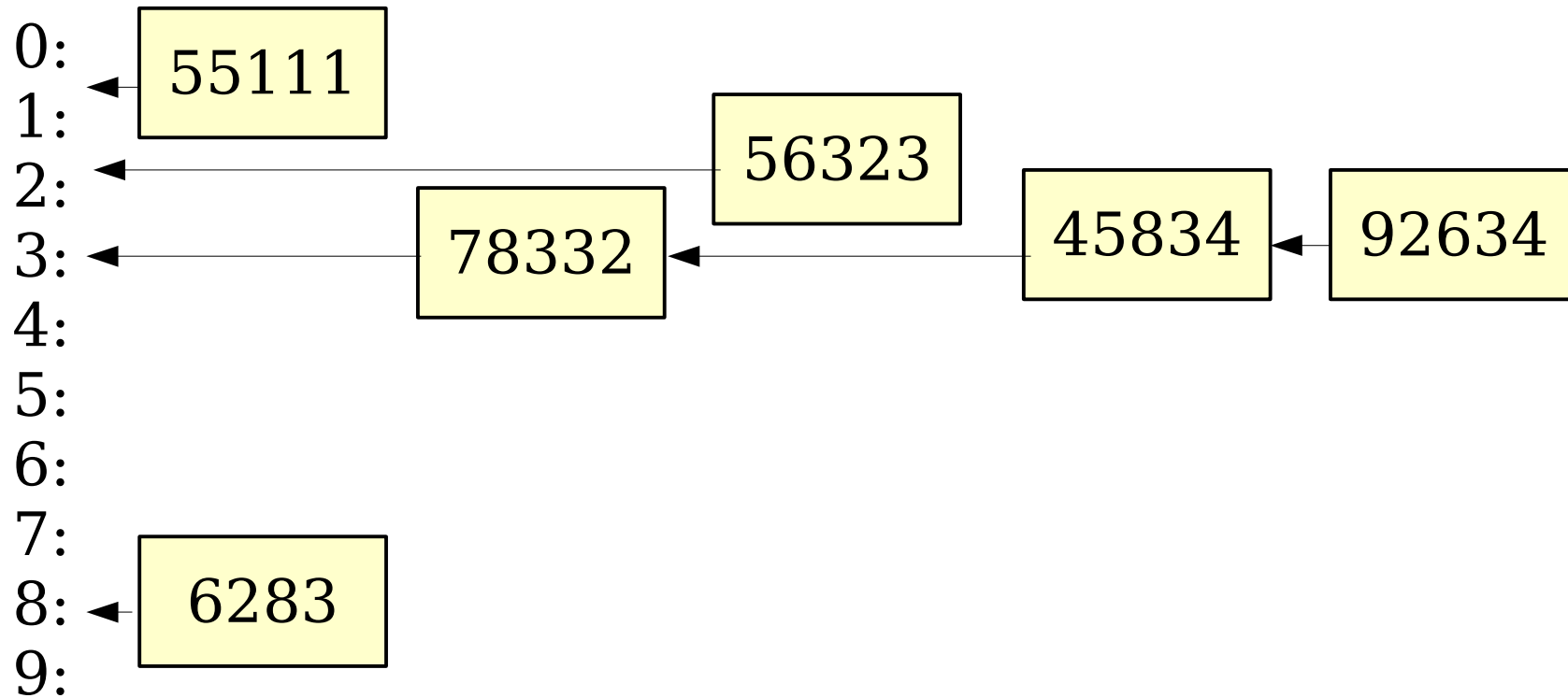
6:

7:

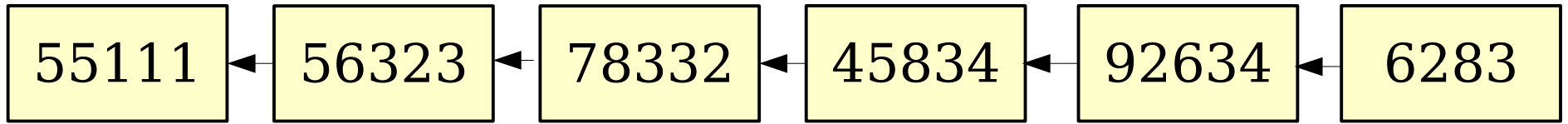
8:

9:

Radix Sort



Radix Sort



0:

1:

2:

3:

4:

5:

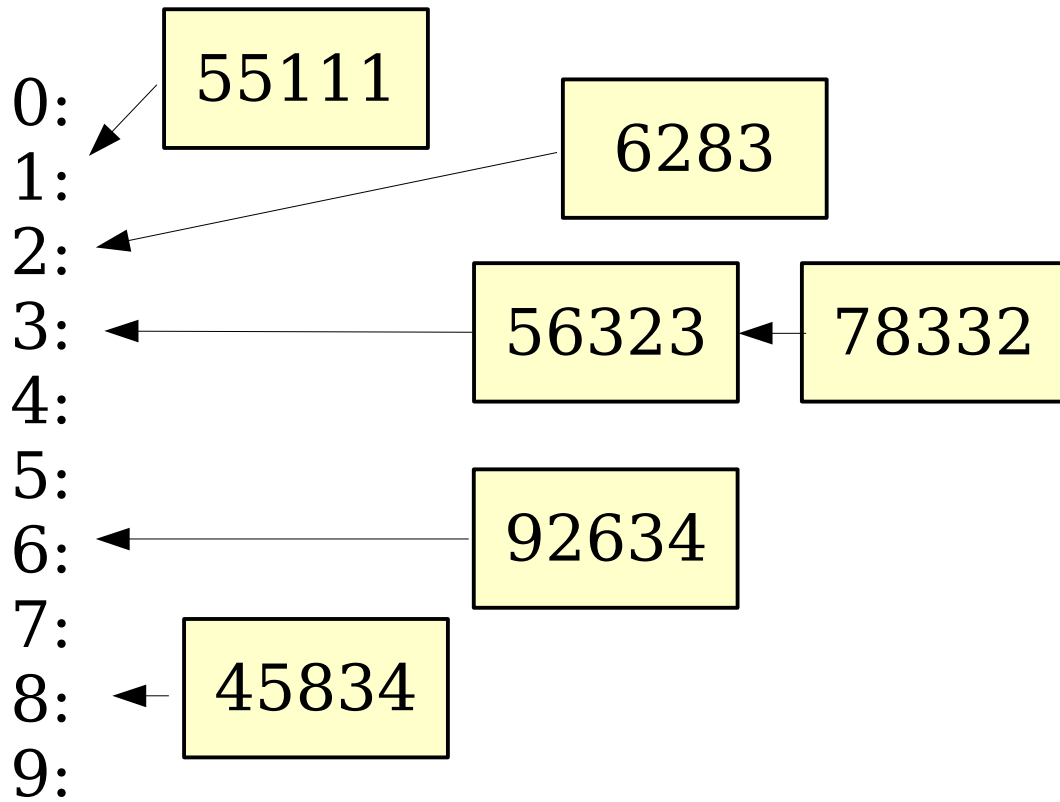
6:

7:

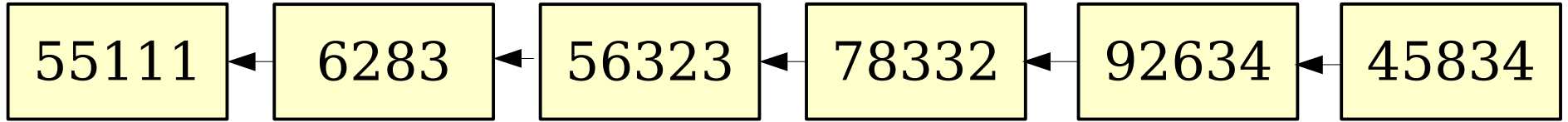
8:

9:

Radix Sort



Radix Sort



0:

1:

2:

3:

4:

5:

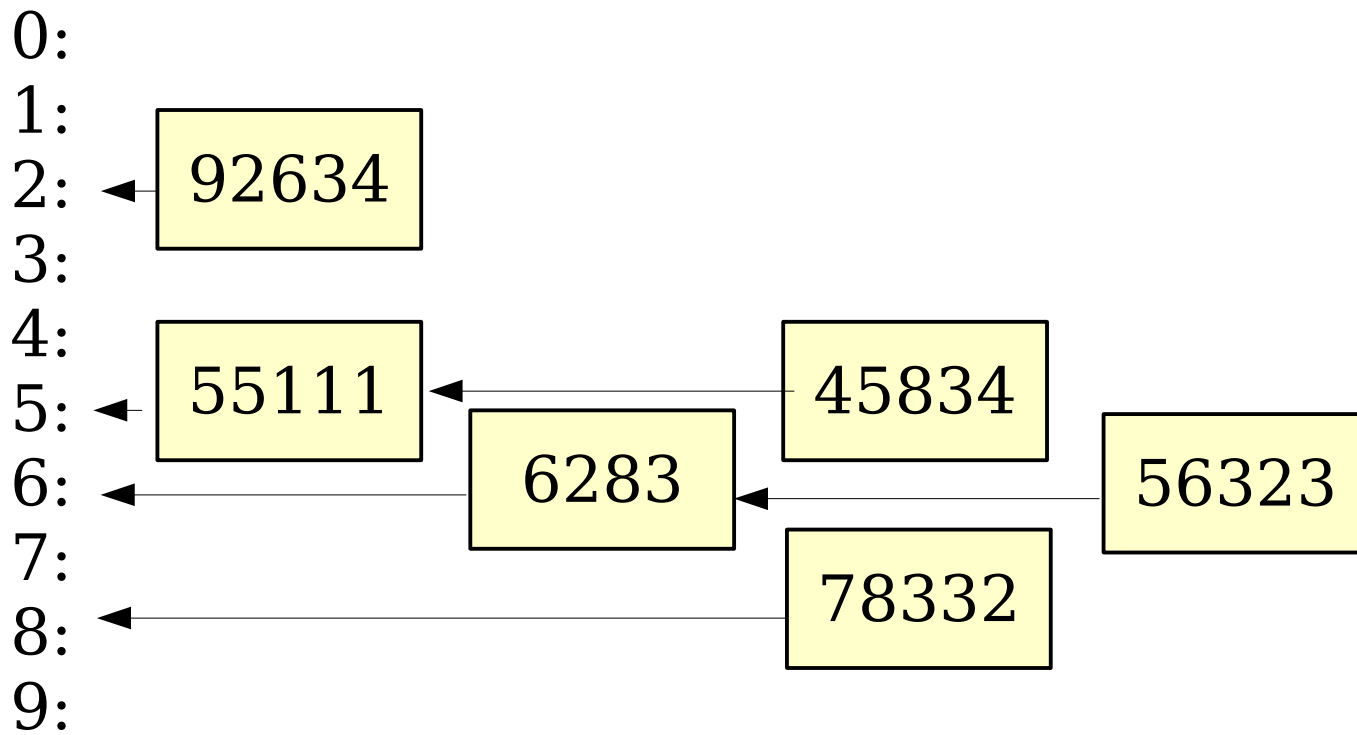
6:

7:

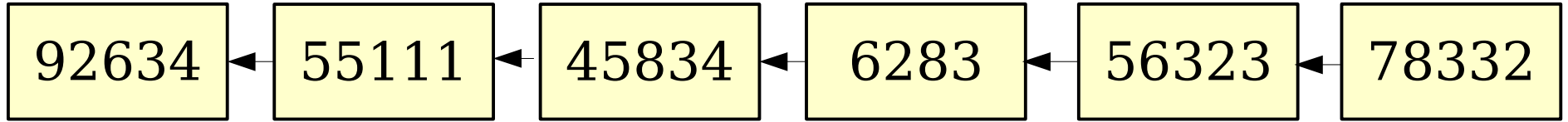
8:

9:

Radix Sort



Radix Sort



0:

1:

2:

3:

4:

5:

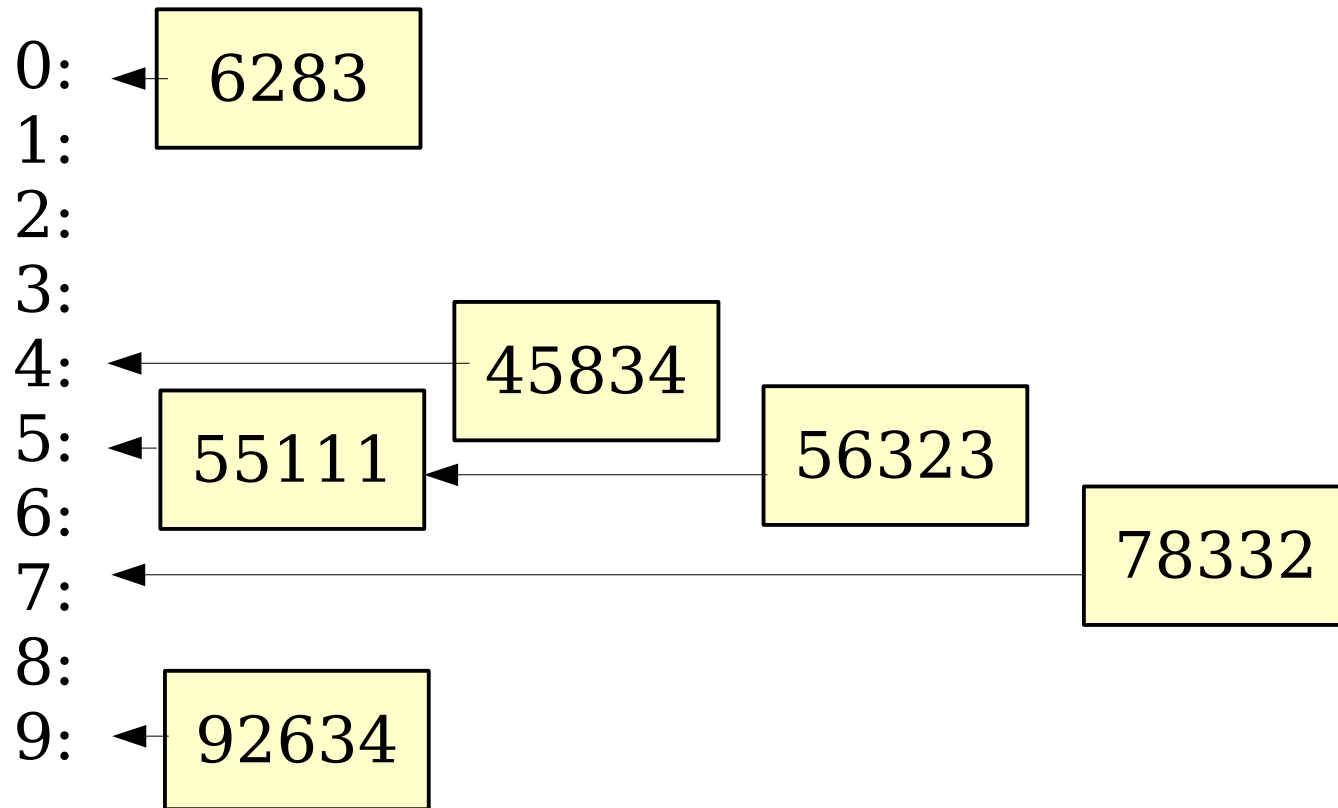
6:

7:

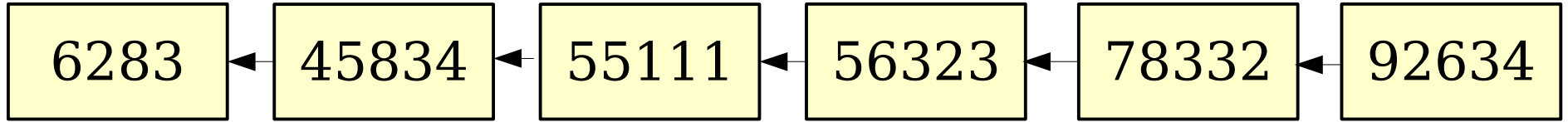
8:

9:

Radix Sort



Radix Sort



0:

1:

2:

3:

4:

5:

6:

7:

8:

9:

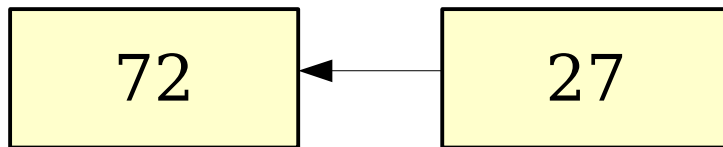
Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

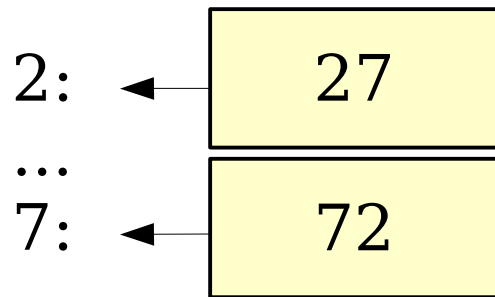
No! Here is a counter-example:



Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

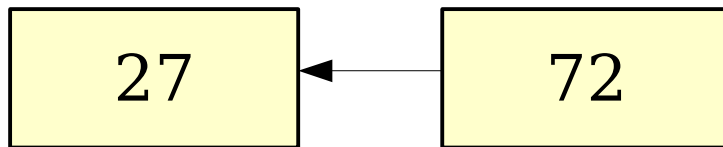
No! Here is a counter-example:



Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

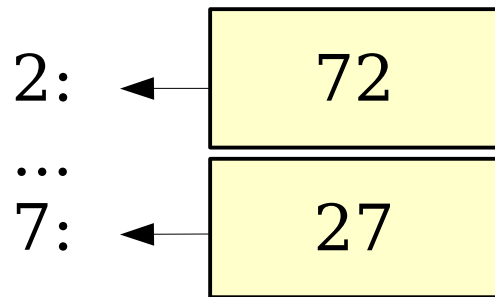
No! Here is a counter-example:



Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

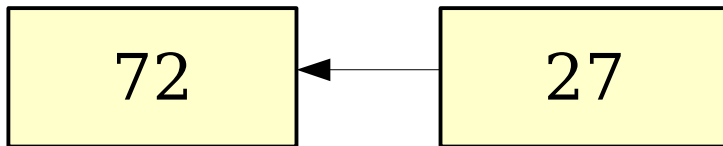
No! Here is a counter-example:



Radix Sort

Example shows working from LSD to MSD. Is radix sort correct working from MSD to LSD?

No! Here is a counter-example - numbers not increasing:



Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Base step: After 1st step – all numbers in order on LSD

Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Base step: After 1st step – all numbers in order on LSD

Induction step: suppose (P) after kth step that all numbers are in non-decreasing order on k least significant digits.

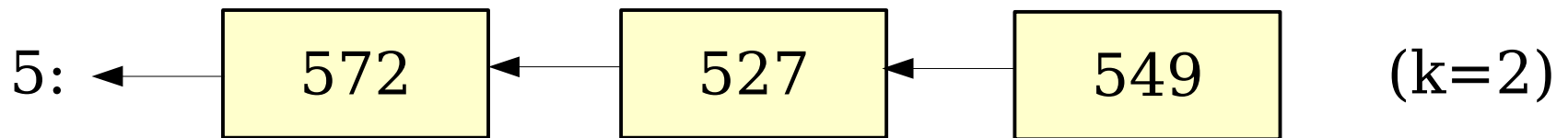
Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Base step: After 1st step – all numbers in order on LSD

Induction step: suppose (P) after kth step that all numbers are in non-decreasing order on k least significant digits. Consider a queue on the k+1st step where at least two numbers are out of order in the k least significant digits. For example,



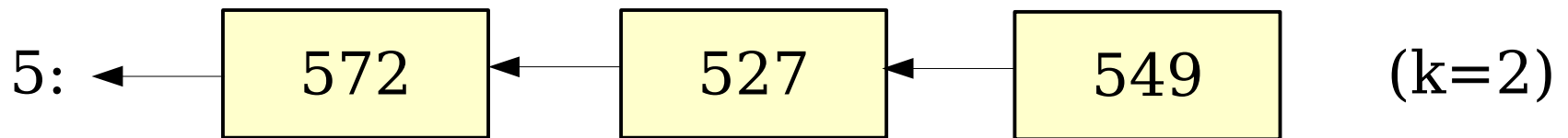
Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Base step: After 1st step – all numbers in order on LSD

Induction step: suppose (P) after k^{th} step that all numbers are in non-decreasing order on k least significant digits. Consider a queue on the $k+1^{\text{st}}$ step where at least two numbers are out of order in the k least significant digits. For example,



The numbers in that queue are in the same order they were in the list following the k^{th} step. But that is a violation of (P). Hence, all numbers in a queue are in non-decreasing order.

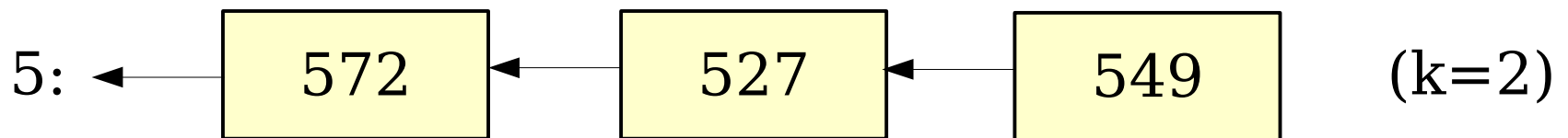
Radix Sort

Can we prove that radix sort is correct when working from LSD to MSD?

Yes! By induction on the digit being sorted

Base step: After 1st step – all numbers in order on LSD

Induction step: suppose (P) after k^{th} step that all numbers are in non-decreasing order on k least significant digits. Consider a queue on the $k+1^{\text{st}}$ step where at least two numbers are out of order in the k least significant digits. For example,



The numbers in that queue are in the same order they were in the list following the k^{th} step. But that is a violation of (P). Hence, all numbers in a queue are in non-decreasing order. Since assembling the list after the $k+1^{\text{st}}$ step is by increasing queue rank ($k+1^{\text{st}}$ digit) all numbers in the list are in non-decreasing order.