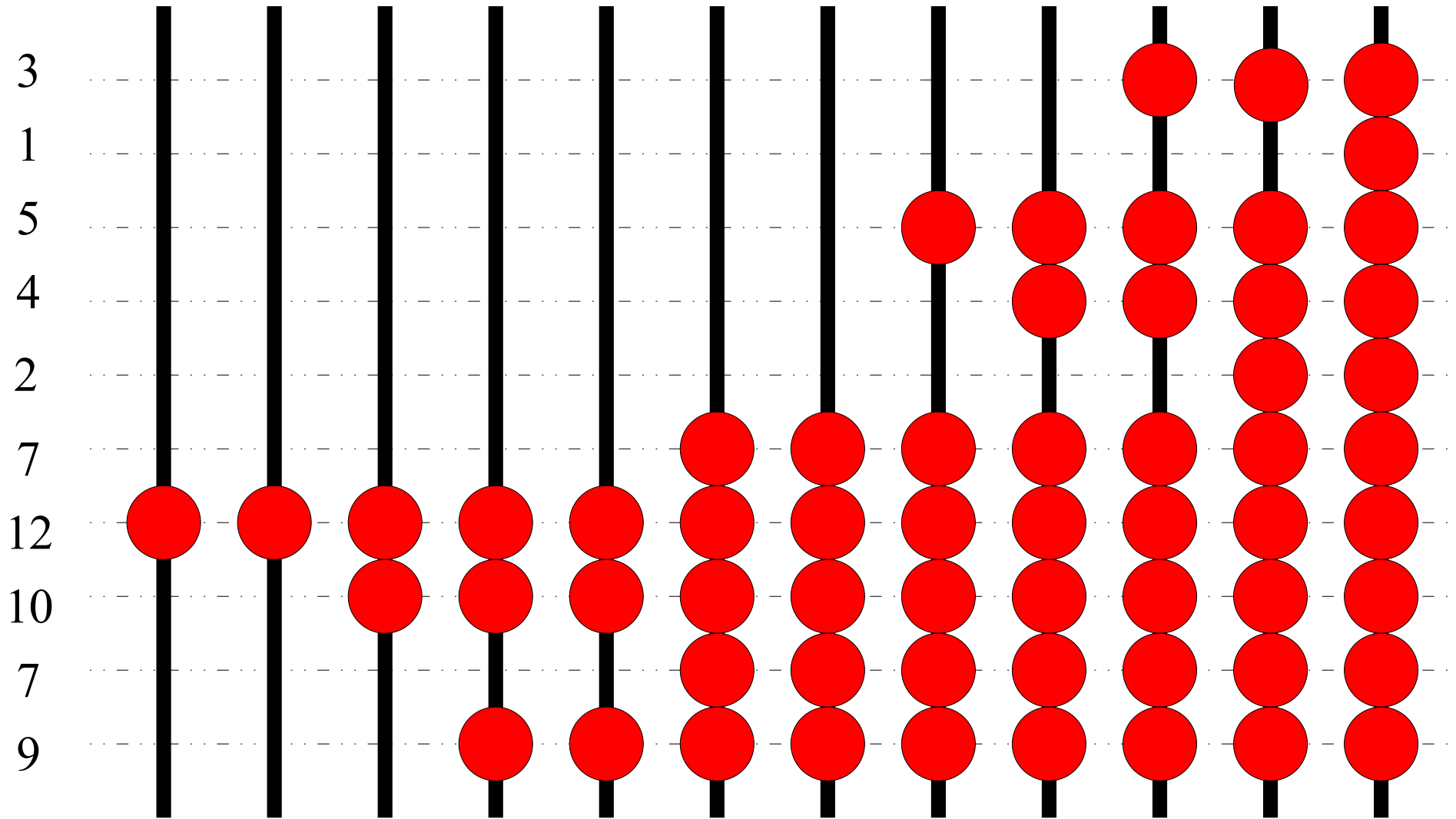


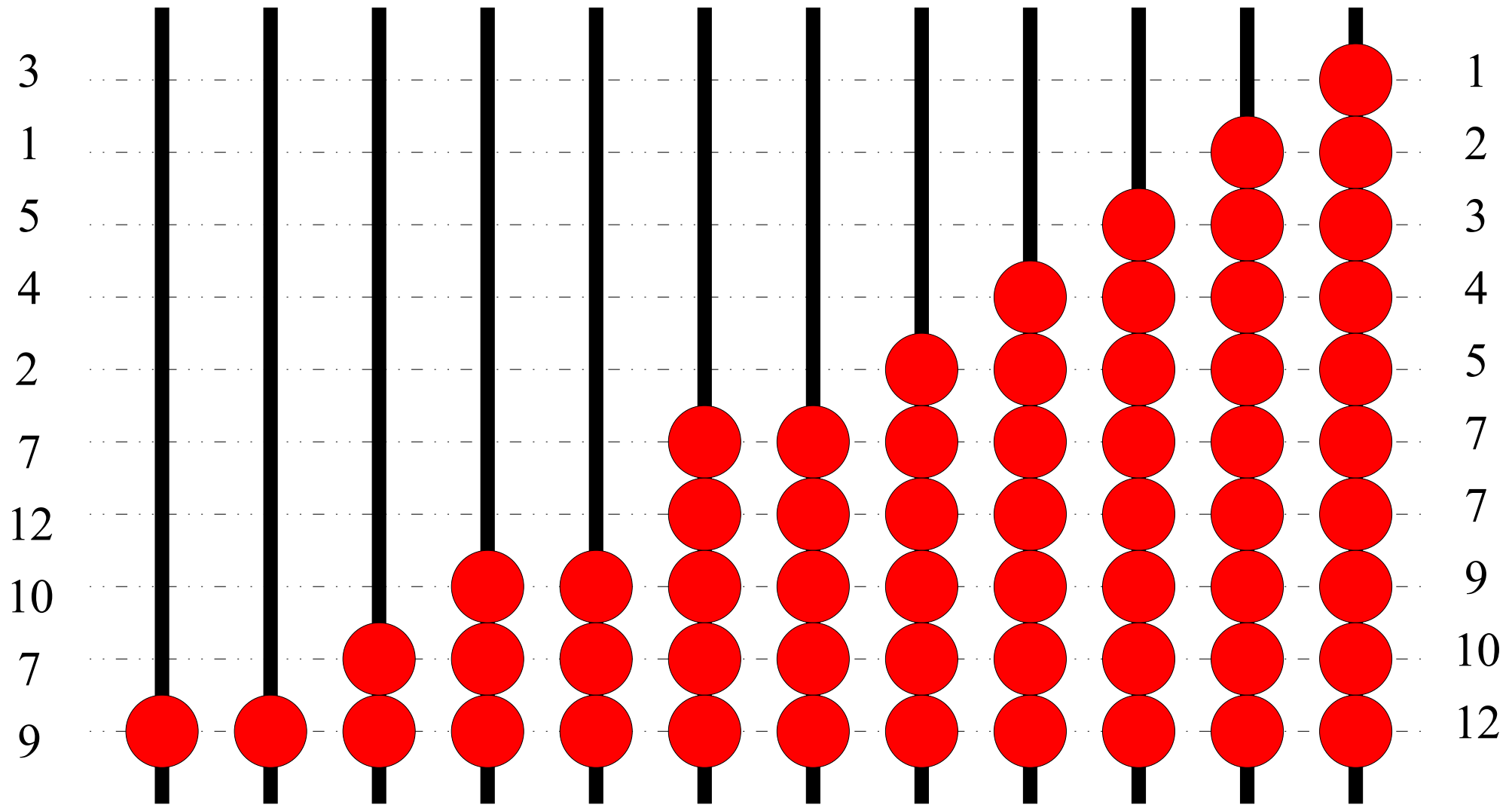
# **Impractical Sorting Algorithms**

# Outer Space Sort (OSS)

# Outer Space Sort (OSS)



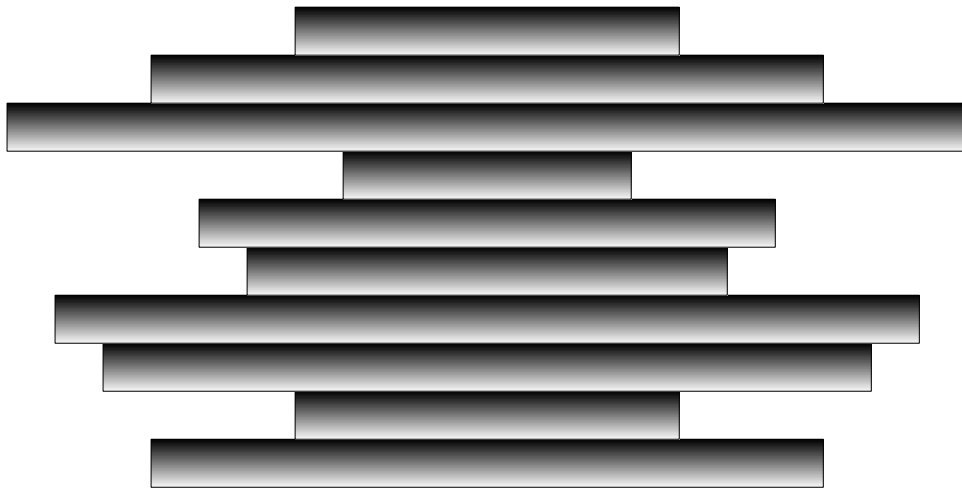
# Outer Space Sort (OSS)



# Pancake Sort

# Pancake Sort

Numbers are represented as pancakes – list of numbers as a stack of pancakes



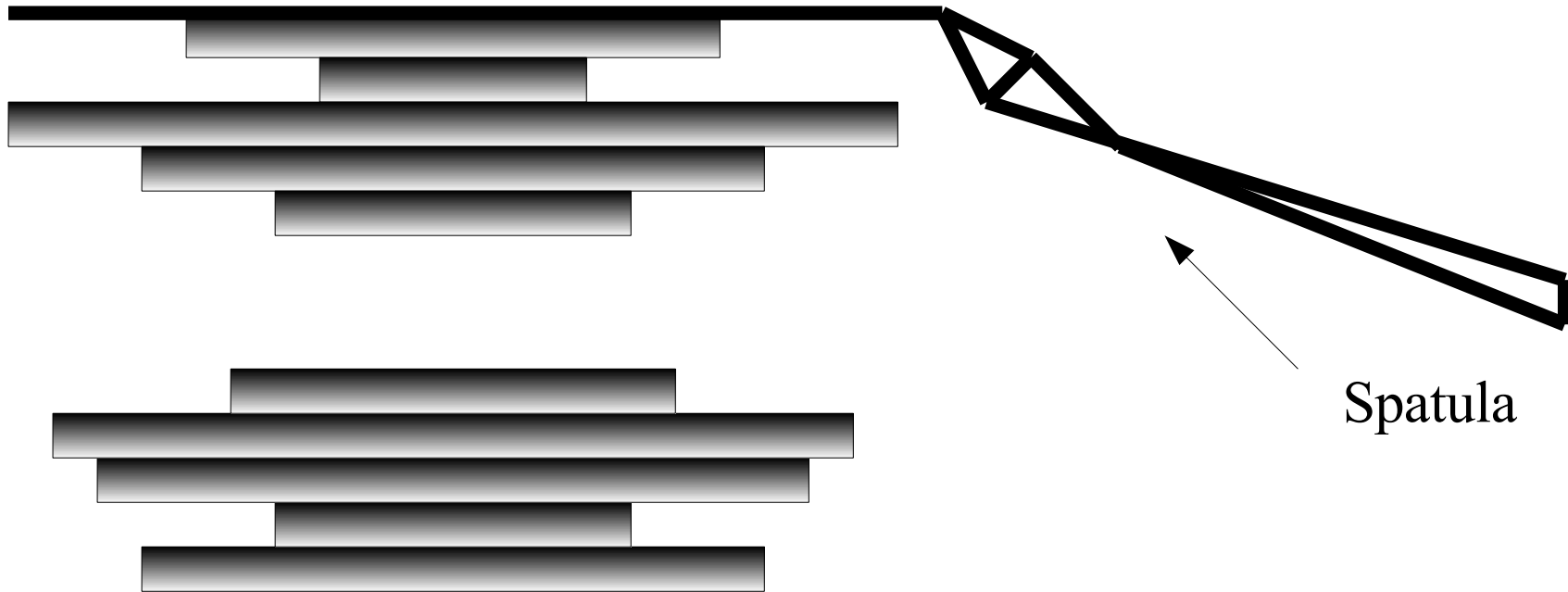
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# Pancake Sort

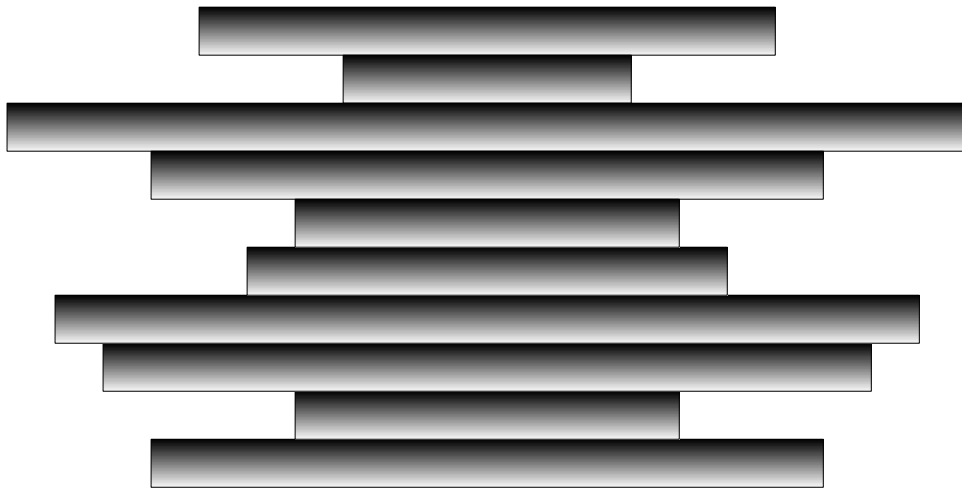
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# Pancake Sort

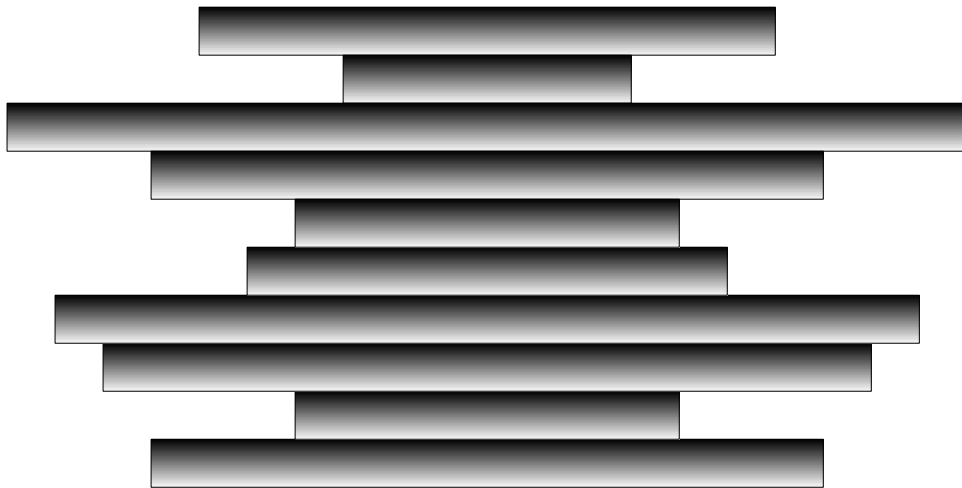
Numbers are represented as pancakes – list of numbers as a stack of pancakes



Only operation: flip the pancakes from inside the stack somewhere

# Pancake Sort

Algorithm: find largest that is not yet sorted, flip to top, flip to bottom



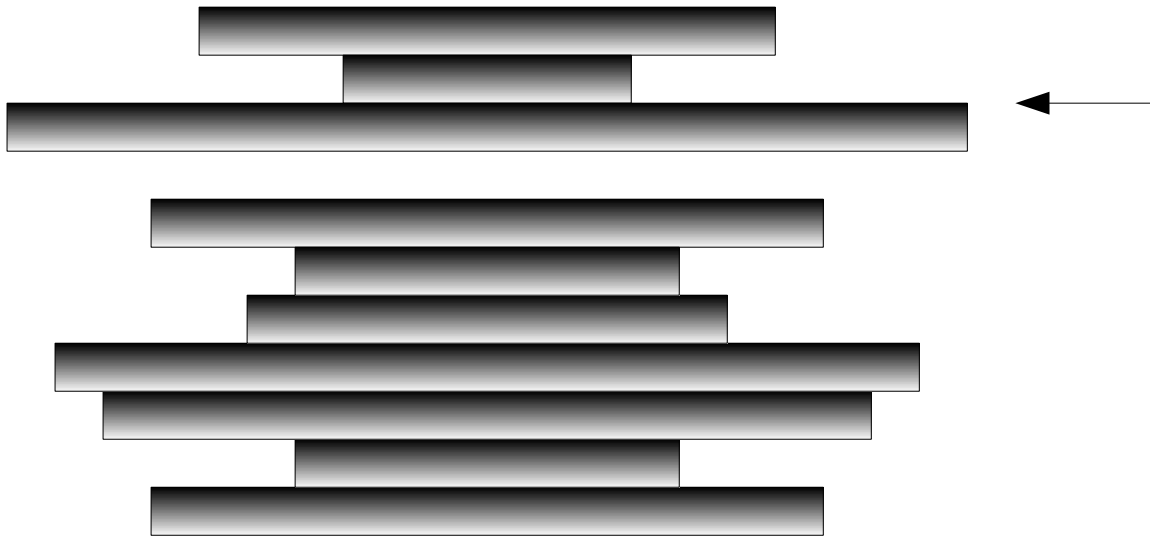
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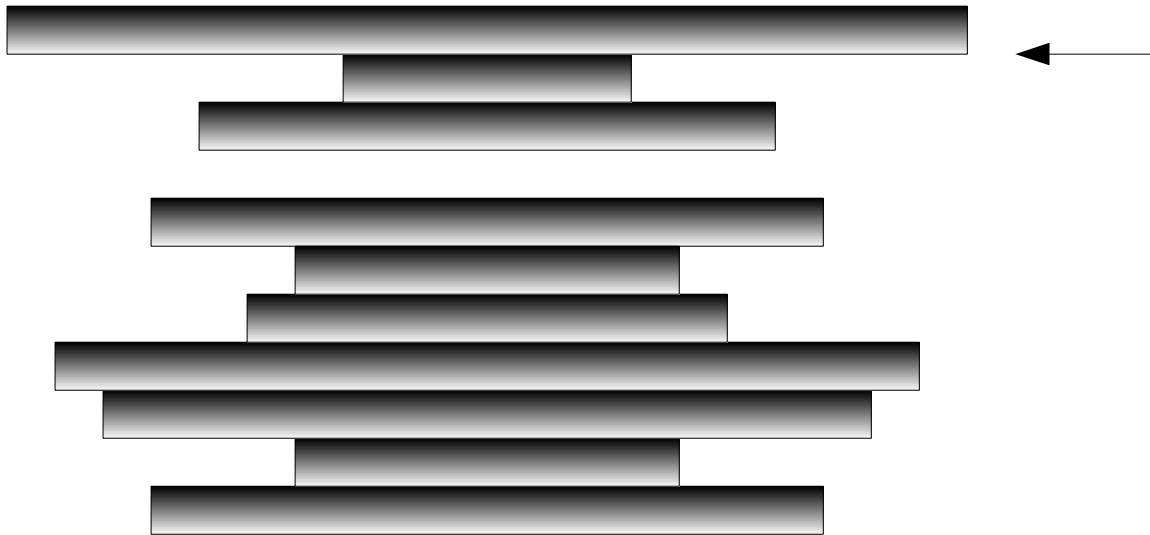
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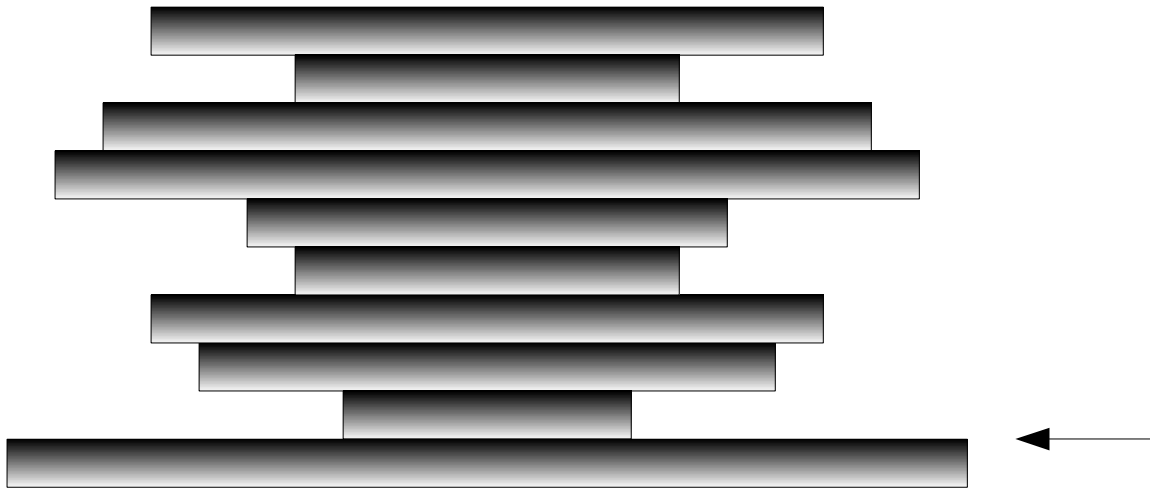
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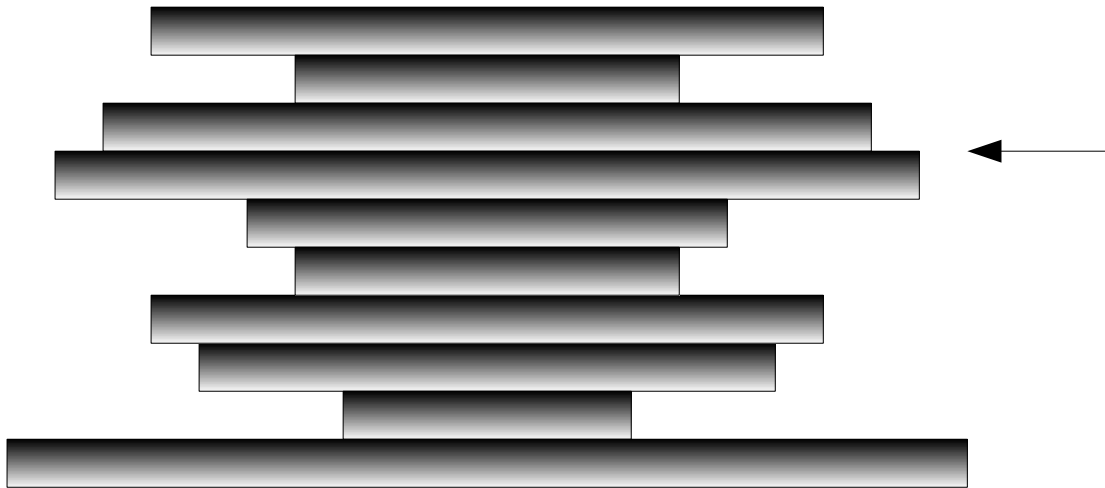
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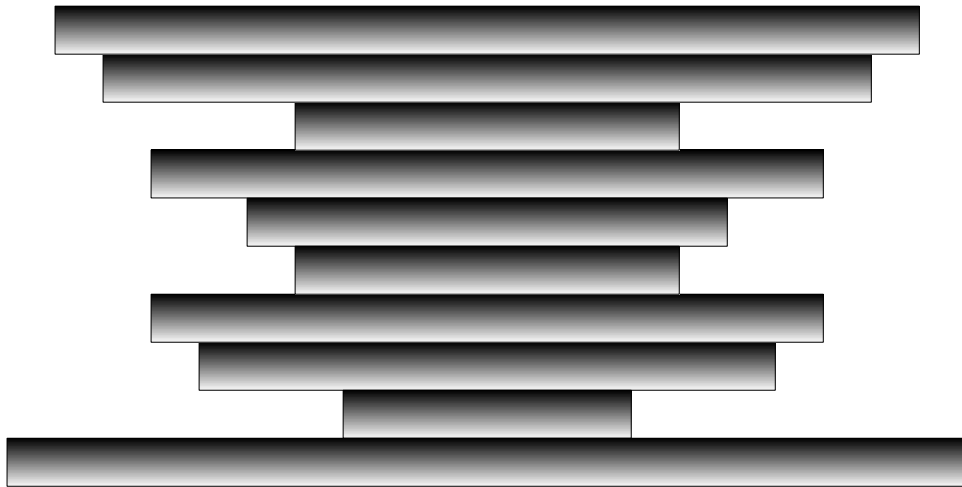
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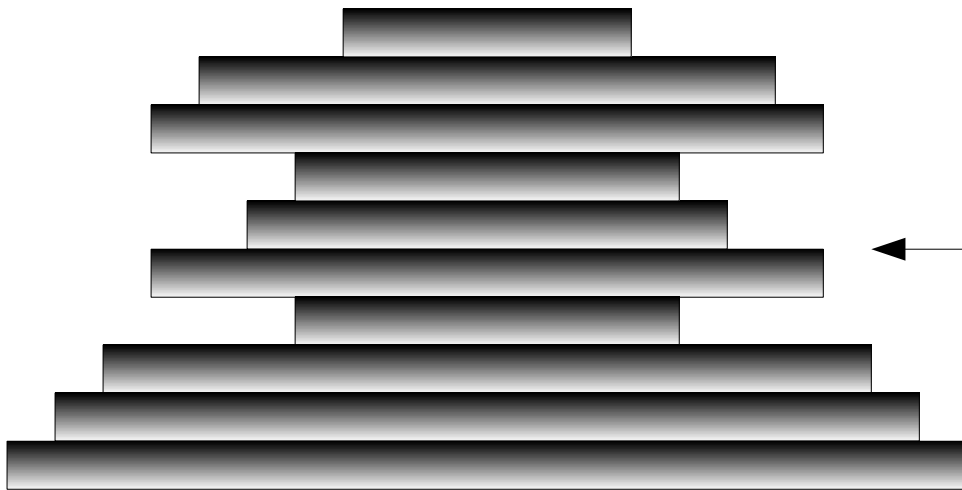
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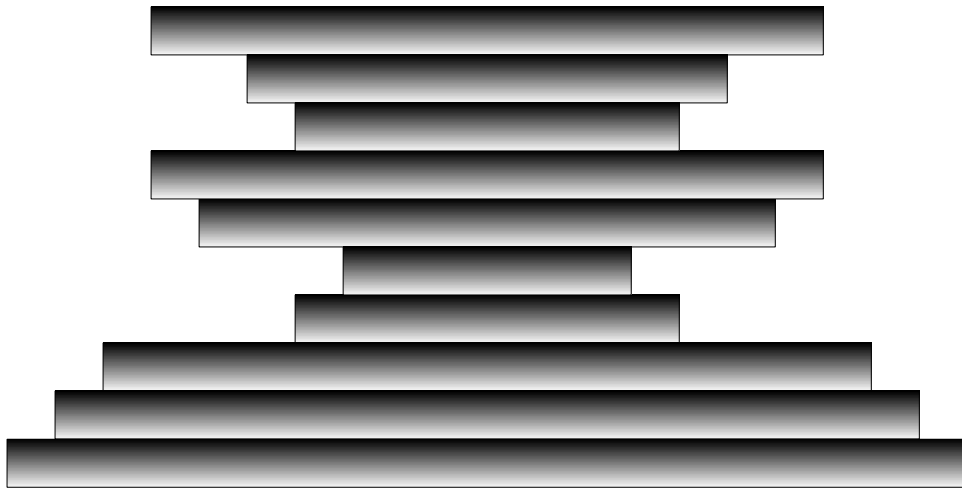
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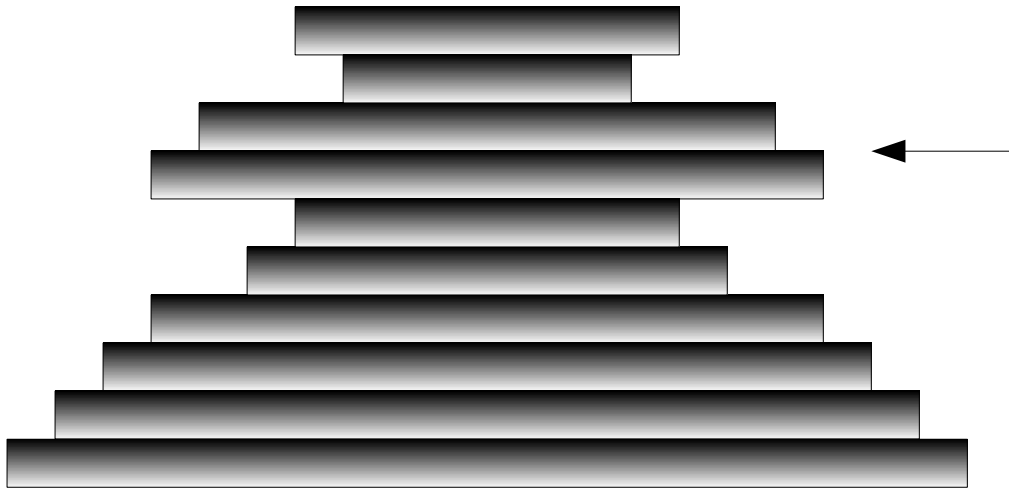
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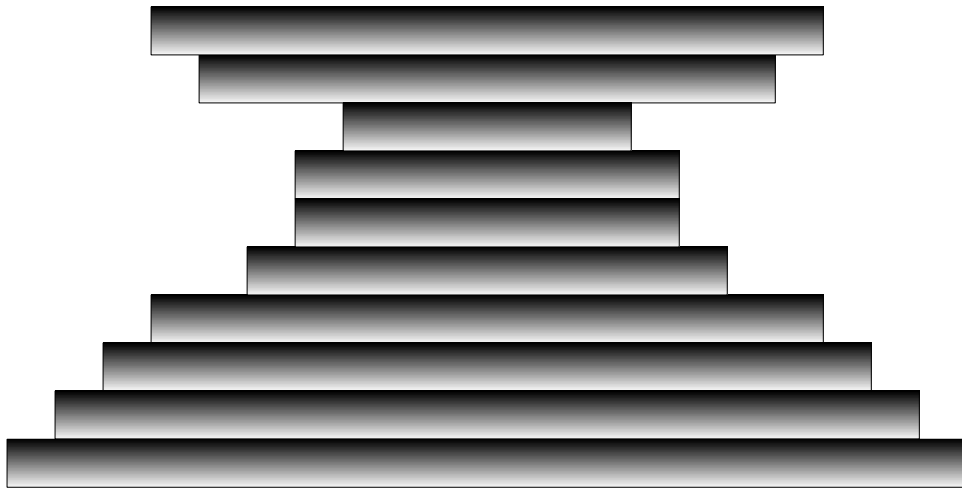
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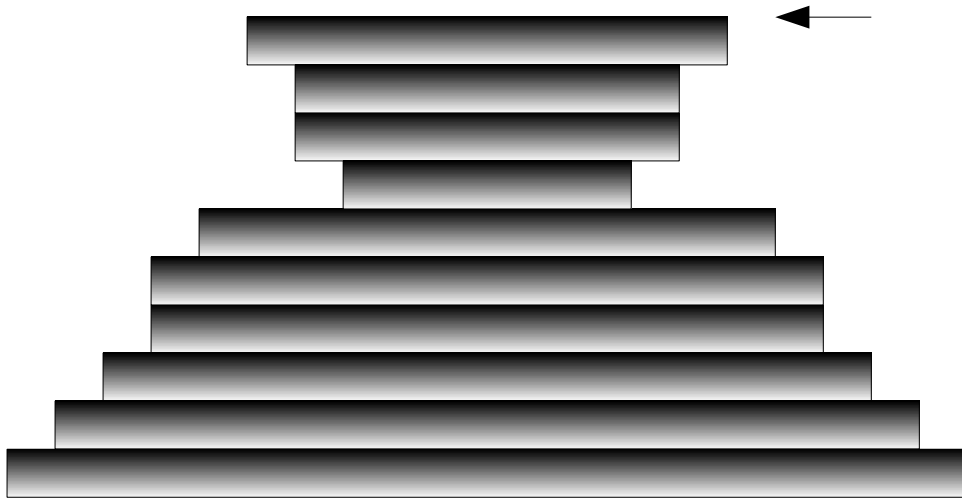
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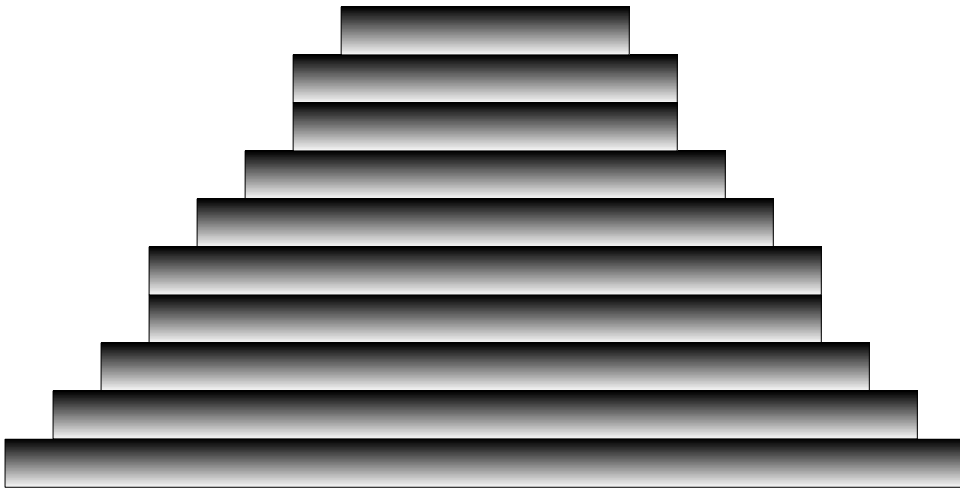
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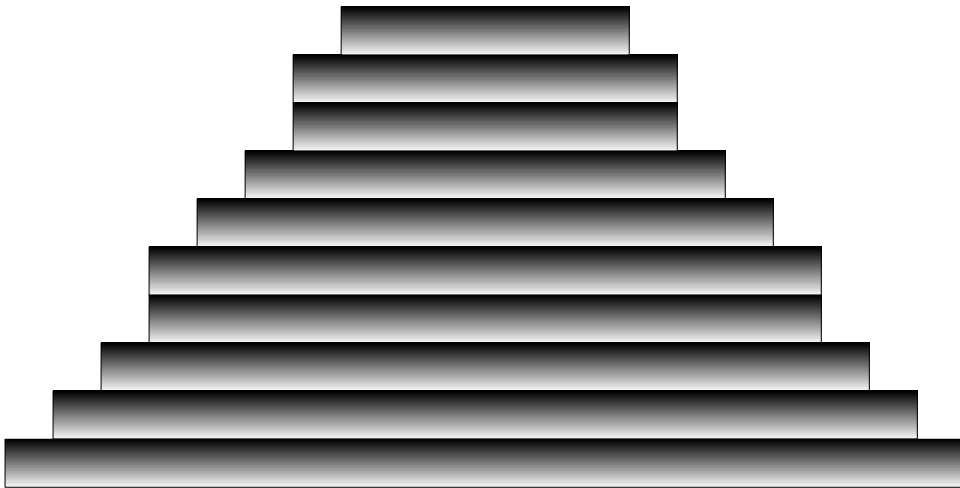
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# Pancake Sort

Algorithm: find largest that is not yet sorted, flip to top, flip to bottom

The *one and only* well-known published paper of Bill Gates describes an efficient pancake sort algorithm!



# Stooge Sort

43 66 12 88 3 81 72 94 38



# Stooge Sort

43 66 12 88 3 81 72 94 38



Compare last and first numbers  
and swap if out of order

# Stooge Sort

38 66 12 88 3 81 72 13 43



Compare last and first numbers  
and swap if out of order

# Stooge Sort

38 66 12 88 3 81 72 13 43

Sort the 1<sup>st</sup> two thirds of the list



# Stooge Sort

3 12 38 66 81 88 72 13 43

Sort the 1<sup>st</sup> two thirds of the list



# Stooge Sort

3 12 38 66 81 88 72 13 43

Sort the last two thirds of the list



# Stooge Sort

3 12 38 13 43 66 72 81 88

Sort the last two thirds of the list



# Stooge Sort

3 12 38 13 43 66 72 81 88

Sort the 1<sup>st</sup> two thirds of the list



# Stooge Sort

3 12 13 38 43 66 72 81 88

Sort the 1<sup>st</sup> two thirds of the list





# Bogo Sort

# Bogo Sort

**Given:** 9 23 8 92 3 45 7 16 88 19

# Bogo Sort

**Given:** 9 23 8 92 3 45 7 16 88 19

Roll dice

# Bogo Sort

**Given:** 9 23 8 92 3 45 7 16 88 19

Roll dice

7 8 88 19 16 45 92 9 23 3

# Bogo Sort

**Given:** 9 23 8 92 3 45 7 16 88 19

Roll dice

7 8 88 19 16 45 92 9 23 3

Average complexity:

Assume  $n$  items to sort

Let  $X$  be r.v. with value  $i$  in the event it takes  $i$  rolls to sort

$$Pr(X=i) = (1-1/n!)^{i-1}(1/n!)$$

$$E\{X\} = Pr(X>0) + Pr(X>1) + Pr(X>2) + \dots$$

$$\begin{aligned} E\{X\} &= 1 + (1-1/n!) + (1-1/n!)^2 + (1-1/n!)^3 + \dots \\ &= 1/(1-(1-1/n!)) = n! \end{aligned}$$

# Digression

$$E\{X\} = Pr(X=1) + 2Pr(X=2) + 3Pr(X=3) + \dots$$

$$\begin{aligned} E\{X\} &= Pr(X=1) + Pr(X=2) + Pr(X=3) + \dots &&= Pr(X>0) \\ &+ Pr(X=2) + Pr(X=3) + \dots &&= Pr(X>1) \\ &+ Pr(X=3) + \dots &&= Pr(X>2) \end{aligned}$$